

1. (b, c)

$$V = \frac{kr^2}{2} \Rightarrow F = -\frac{dV}{dr} = -kr$$

$$\therefore \frac{mv^2}{r} = kr \Rightarrow v = \sqrt{\frac{k}{m}}R$$

$$\text{Angular momentum } L = mvr = m\sqrt{\frac{k}{m}}R^2 = \sqrt{mk}R^2$$

2. (a, c)

$$\vec{a} = t\hat{i} + jm/s^2$$

$$\Rightarrow \vec{v} = \frac{t^2}{2}\hat{i} + tjm/s$$

$$\Rightarrow \vec{r} = \frac{t^3}{6}\hat{i} + \frac{t^2}{2}jm$$

$$\text{so, } \vec{\tau} = \vec{r} \times \vec{F} = \left(\frac{t^3}{2} - \frac{t^3}{6}\right)(-k) = \frac{t^3}{3}(-k)Nm$$

3. (a, c)

$$h = \frac{2\sigma \cos \theta}{r\rho g_{eff}} \quad (\rho \text{ is density of water})$$

4. (b, d)

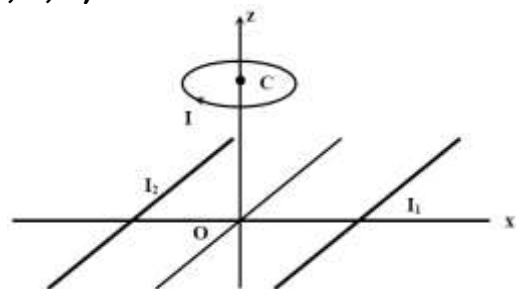
$$I = \frac{V}{R} \left(1 - e^{-\frac{Rt}{L}}\right) - \frac{V}{R} \left(1 - e^{-\frac{RT}{2L}}\right)$$

For $I_{\max}$

$$\frac{dI}{dt} = 0$$

$$\therefore t = \frac{2L}{R} \ln 2 \text{ b and } I_{\max} = \frac{V}{4R}$$

5. (a, b, d)



(a) If $I_1 = I_2$, magnetic field due to infinite wires is equal to zero. So there must be a non-zero magnetic field at O due to the current carrying loop.

(b) If $I_1 > 0$ & $I_2 < 0$, magnetic field due to straight lines are along positive z-axis and due to loop it is along negative z-axis.

(c) If $I_1 < 0$ & $I_2 > 0$ magnetic field due to straight wires are along negative z-axis and due to the loop it is also along negative z-axis.

$$(d) \quad \vec{B}_C = \frac{\mu_0 I}{2R}(-k)$$

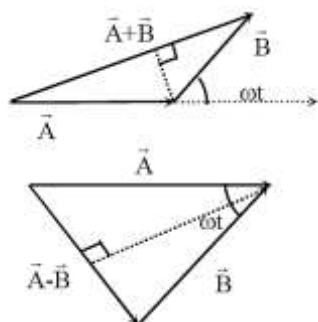
(along z axis)

6. (b, c, d) Process II is an isothermal expansion

Process IV is an isothermal compression

In isobaric process, volume is directly proportional to temperature.

7. 2.00

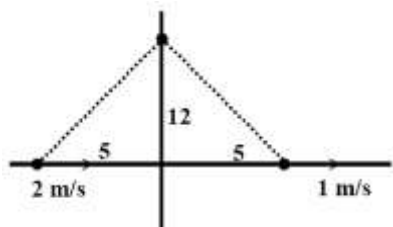


$$\therefore 2a \cos \frac{\omega t}{2} = \sqrt{3} (2a) \sin \frac{\omega t}{2}$$

$$\therefore \tan \frac{\omega t}{2} = \frac{1}{\sqrt{3}}$$

$$\text{for the first time} \Rightarrow \frac{\pi t}{12} = \frac{\pi}{6} \Rightarrow t = 2 \text{ sec}$$

8. 5.00



$$\Delta f = f_0 \left(\frac{330}{330 - 2 \cos \theta} - \frac{330}{330 + 1 \cos \theta} \right)$$

$$= f_0 \left(\frac{330}{330 - \frac{10}{13}} - \frac{330}{330 + \frac{5}{13}} \right)$$

$$= f_0 \left(1 + \frac{10}{13 \times 330} - 1 + \frac{5}{13 \times 330} \right)$$

$$= \frac{15}{13 \times 330} \times 1430 = 5 \text{ Hz}$$

9. 0.75

$$\frac{h}{\sin \theta} = \frac{1}{2} \frac{g \sin \theta}{1 + \frac{I}{mR^2}} t^2$$

$$\therefore t = \frac{1}{\sin \theta} \sqrt{\frac{2h}{g} \left(1 + \frac{I}{mR^2} \right)}$$

$$\therefore \frac{2 - \sqrt{3}}{\sqrt{10}} = \frac{2}{\sqrt{3}} \sqrt{\frac{2h}{10} \left(\sqrt{2} - \sqrt{\frac{3}{2}} \right)}$$

$$\therefore h = 0.75 \text{ m}$$

10. 2.09

For collision:

using com $\rightarrow 1 \times 2 = 1 \times u + 2 \times v$

Using e $\rightarrow 2 = -u + v$

$$u = \frac{-2}{3} \text{ m/s} \quad v = \frac{4}{3} \text{ m/s}$$

time taken for the block to come to the unstretched position of spring for the first time after the collision

$$= \pi \sqrt{\frac{m}{k}} = \pi \text{ sec}$$

$$\text{distance between blocks} = \frac{2\pi}{3} m = 2.09 \text{ m (taking } \pi \approx 3.14)$$

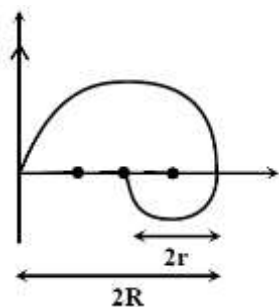
11. 1.50

After S_1 is closed, C_3 has charge $8 \mu\text{C}$. when S_1 opened and S_2 closed, C_3 has charge $5 \mu\text{C}$. so remaining $3 \mu\text{C}$ resides on C_1 and C_2

$$\frac{1}{C_{eq}} = \frac{1}{\epsilon_r} + \frac{1}{1} = \frac{5}{3} \left[\frac{1}{C} = \frac{V}{q} \right]$$

$$\Rightarrow \epsilon_r = \frac{3}{2} = 1.5$$

12. 2.00

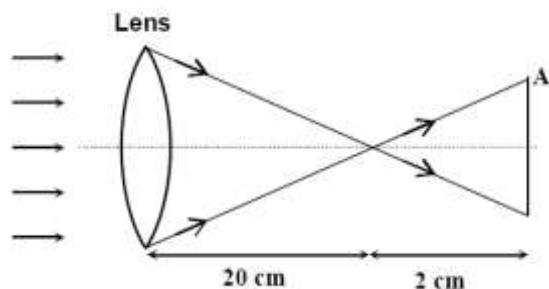


Avg. speed along x-axis

$$= \frac{\text{total distance travelled along x - axis}}{\text{total time taken}}$$

$$= \frac{2R + 2r}{\frac{\pi R}{V_0} + \frac{\pi r}{V_0}} = \frac{2V_0}{\pi} = 2m/s$$

13. 130.00



The area of A over which the light falls satisfy: Lens

$$\frac{A}{A_{\text{lens}}} = \left(\frac{2}{20} \right)^2 = \frac{1}{100}$$

so intensity at A = $100 \times 1.3 = 130 \text{ kW/m}^2$.

14. 4.00

In steady state, heat current in both material is same

$$\frac{K_1(300 - 200)A}{L} = \frac{K_2(200 - 100)4A}{L}$$

$$\Rightarrow \frac{K_1}{K_2} = 4$$

15. (i) (c)

$$E = \frac{F}{q}; F = qvB$$

$$E = BV; [E] = [B][L][T]^{-1}$$

(ii) (d)

$$\epsilon_0 \mu_0 = \frac{1}{C^2}$$

$$\mu_0 = [\epsilon_0]^{-1} [L]^2 [T]^2$$

16. (i) (b)

$$r + \Delta r = \frac{1 - (a + \Delta a)}{1 + (a + \Delta a)}$$

$$\Delta r = \frac{1 - (a + \Delta a)}{1 + (a + \Delta a)} - \frac{1 - a}{1 + a} = \frac{[1 - (a + \Delta a)](1 + a) - [1 + (a + \Delta a)][1 - a]}{(1 + a + \Delta a)(1 + a)}$$

$$|\Delta r| = \left| \frac{-2\Delta a}{(1 + a)^2} \right|$$

alternate:

$$\Delta r = \frac{1 - a}{1 + a} \left[\frac{\Delta a}{1 - a} + \frac{\Delta a}{1 + a} \right]$$

$$\Delta r = \frac{2\Delta a}{(1 + a)^2}$$

(ii) (c)

$$N_d = N_0 (1 - e^{-\lambda t})$$

$$1000 = 3000 (1 - e^{-\lambda t}) \Rightarrow e^{\lambda} = \frac{3}{2}$$

$$\Delta N_d = N_0 e^{-\lambda t} \Delta \lambda$$

$$40 = 3000 \times \frac{2}{3} \times \Delta \lambda$$

$$\Delta \lambda = 0.02$$

alternate:

$$N = N_0 e^{-\lambda t}$$

$$N + \Delta N = N_0 e^{-(\lambda + \Delta \lambda)t}$$

$$\Delta N = N_0 (e^{-(\lambda + \Delta \lambda)t} - e^{-\lambda t})$$

$$\Delta N = N_0 (e^{-\lambda t} e^{-\Delta \lambda t} - e^{-\lambda t})$$

$$\Delta N = N_0 e^{-\lambda t} [e^{-\Delta \lambda t} - 1]$$

$$\Delta N \approx N [\Delta \lambda t]$$

$$\Delta \lambda = 0.02$$

17. (b, c)

(a) $NH_4NO_3 \xrightarrow{\Delta} N_2O + 2H_2O$ (N_2O can further decompose to N_2 and O_2 at temperature above $300^\circ C$)

(b) $(NH_4)_2Cr_2O_7 \xrightarrow{\Delta} N_2 + Cr_2O_3 + 4H_2O$

(c) $Ba(N_3)_2 \xrightarrow{\Delta} 3N_2 + Ba$

(d) Mg_3N_2 does not decompose at any temperature.

18. (b, c)

(a) Electronic configuration of central metal atom in both cases is $[Ar] 3d^{10}4s^24p^6$ (8 electrons in outermost shell and 18 valence electrons respectively).

(b) Low spin complex because CO is a strong field ligand.

(c) Metal-carbon bond strengthens when the oxidation state of metal is lowered.

(d) The carbonyl C - O bond becomes stronger when the oxidation state is increased.

19. (a, b, c)

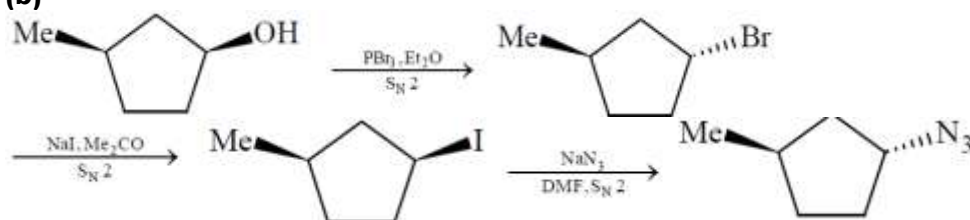
Bi_2O_5 is more basic than N_2O_5 .

NF_3 is more covalent than BiF_3 .

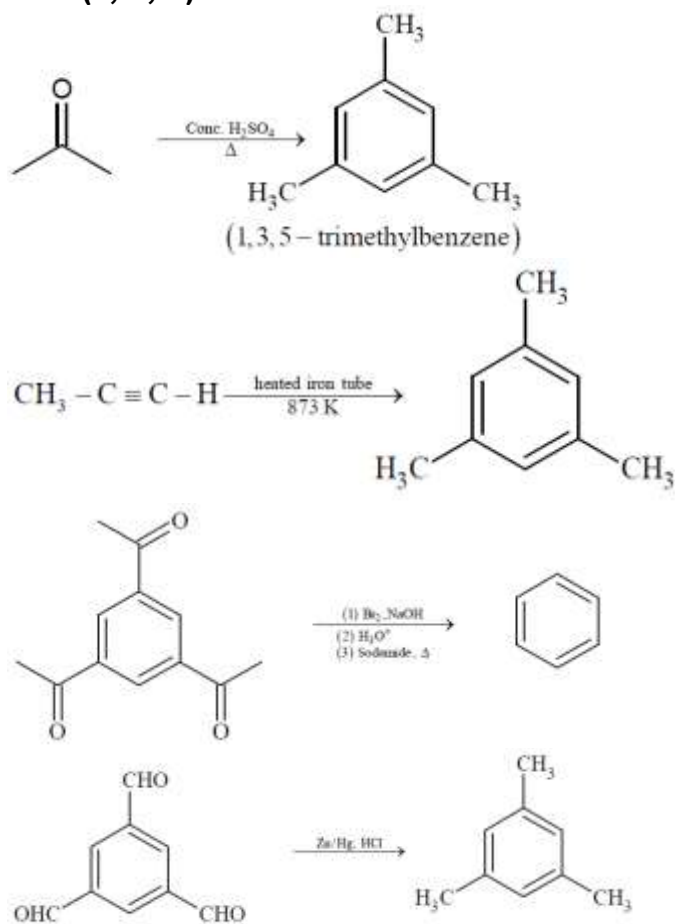
PH_3 boils at lower temperature than NH_3 .

N - N single bond is weaker than P - P single bond.

20. (b)



21. (a, b, d)



22. (b, c)

$$\Delta H_{AC} + \Delta H_{CB} + \Delta H_{BA} = 0$$

$$\Delta H_{BA} = 0 \text{ (Temperature is constant)}$$

$$\Delta H_{AC} = \Delta H_{BC} \dots (1)$$

We know that $q_p = \Delta H$ (In path BC, $P = \text{constant}$)

$$\text{Hence } q_{BC} = \Delta H_{BC}$$

From Eq. (1)

$$q_{BC} = \Delta H_{AC}$$

$$(b) q_{BC} = -P_2(V_1 - V_2) = P_2(V_2 - V_1)$$

$$(c) \Delta H_{CA} = nC_p(T_1 - T_2) = -nC_p(T_2 - T_1)$$

$$\Delta U_{CA} = nC_v(T_1 - T_2) = -nC_v(T_2 - T_1)$$

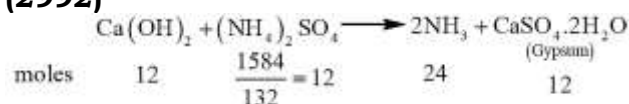
As, $C_p > C_v$

$$\text{So, } \Delta H_{CA} < \Delta U_{CA}$$

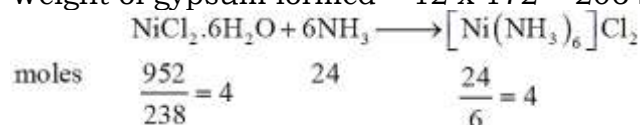
23. (1) Paramagnetic: HNO_2 monomer O_2^- (superoxide), S_2 (Vapour), $[\text{Mn}_3\text{O}_4]$ is mixed oxide of Mn^{+2} and Mn^{+3} ,

$(\text{NH}_4)_2[\text{FeCl}_4]$, $(\text{NH}_4)_2[\text{NiCl}_4]$, K_2MnO_4 Diamagnetic: K_2CrO_4

24. (2992)



Weight of gypsum formed = $12 \times 172 = 2064 \text{ g}$



Mass of $[\text{Ni}(\text{NH}_3)_6]\text{Cl}_2$ formed = $4 \times 232 = 928 \text{ g}$

Total weight = $2064 + 928 = 2992 \text{ g}$.

25. (3)

X^- = Octahedral void

M^+ = FCC point

M^+

X^-

(i) 4

$$4 - 3 = 1$$

(ii) $4 - 6 \times \frac{1}{2}$

$$1 + 6 \times \frac{1}{2}$$

(iii) 1 - 1

$$3 + 1 = 4$$

(iv) 0 + 1

$$4 - 1 = 3$$

$$\text{Hence } \frac{\text{anion}}{\text{cation}} = \frac{3}{1} = 3$$

26. (10)

Case I:

$$E_{\text{cell}} = E_{\text{cell}}^0 - \frac{RT}{2F} \ln \frac{1}{1}$$

$$= 2.1 - 0 = 2.7 \text{ V}$$

Case II:

$$E_{\text{cell}} = E_{\text{cell}}^0 - \frac{RT}{2F} \ln \frac{x}{1}$$

$$2.67 = 2.7 - \frac{R \times 300}{2F} \ln x$$

$$-0.03 = \frac{R \times 300}{2F} \ln x$$

$$\ln x = \frac{0.03 \times 2 \times F}{300 \times R} = 2.3$$

$$x = 10$$

27. (2.22)

As in fig 2, the system attains equilibrium, so,

$$P_A = P_B \text{ and } T_A = T_B$$

$$\frac{P_A V_A}{R n_A T_A} = \frac{P_B V_B}{R n_B T_B}$$

$$\frac{V_A}{V_B} = \frac{n_A}{n_B}$$

$$n_A = \frac{5}{400R}$$

$$n_B = \frac{3}{300R}$$

Due to sliding of piston vol. of A will be increased by x and that of B will be decreased by x.

$$V_A = 1 + x$$

$$V_B = 3 - x$$

$$\frac{1+x}{3-x} = \frac{\frac{5}{400R}}{\frac{3}{300R}}$$

$$4(1+x) = 5(3-x)$$

$$4x + 5x = 11 \Rightarrow x = \frac{11}{9}$$

Hence volume of container A will be

$$V_A = 1 + \frac{11}{9} = \frac{20}{9} = 2.22$$

28. (19)

$$x_A = \frac{1}{2}, x_B = \frac{1}{2}$$

$$P_T = P_A^0 \frac{1}{2} + P_B^0 \times \frac{1}{2}$$

(Given $P_A^0 = 20$)

$$90 = 45 \times 2 = P_A^0 + P_B^0 \dots (1)$$

$$P_B^0 = 90 - 20 = 70$$

$$22.5 = P_A^0 x_A + P_B^0 (1 - x_A)$$

$$= 20x_A + 70(1 - x_A)$$

$$22.5 = 20x_A + 70 - 70x_A$$

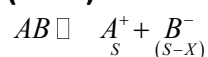
$$= 70 - 50x_A$$

$$x_A = \frac{47.5}{50} = \frac{19}{20}$$

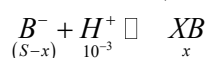
$$x_B = \frac{1}{20}$$

$$\frac{x_A}{x_B} = \frac{\frac{19}{20}}{\frac{1}{20}} = 19$$

29. (4.47)



$$2 \times 10^{-10} = S(S-x) \dots (1)$$



$$\frac{1}{10^{-8}} = \frac{x}{(S-x) \times 10^{-3}}$$

$$\frac{x}{S-x} = 10^5 \dots (2)$$

Multiply equation (1) and (2).

$$S \cdot x = 2 \times 10^{-5}$$

From Eq. (1)

$$S^2 = Sx = 2 \times 10^{-10}$$

$$S^2 - 2 \times 10^{-5} = 2 \times 10^{-10}$$

$$S^2 = 2 \times 10^{-5} + 2 \times 10^{-10} \approx 2 \times 10^{-5}$$

$$S = 4.47 \times 10^{-3}$$

$$y = 4.47$$

30. (0.05)

$$2 = 2xK_{b(x)}m$$

$$1 = 2K_{b(y)}m$$

$$\frac{K_{b(x)}}{K_{b(y)}} = 2$$

$$\Delta T_{b(x)} = \left(1 - \frac{\alpha_1}{2}\right) K_{b(x)} m \quad \frac{2S}{1-\alpha} \square \quad \frac{S_2}{\frac{\alpha}{2}}$$

$$\Delta T_{b(y)} = \left(1 - \frac{\alpha^2}{2}\right) K_{b(y)} m \quad i = 1 - \alpha + \frac{\alpha}{2}$$

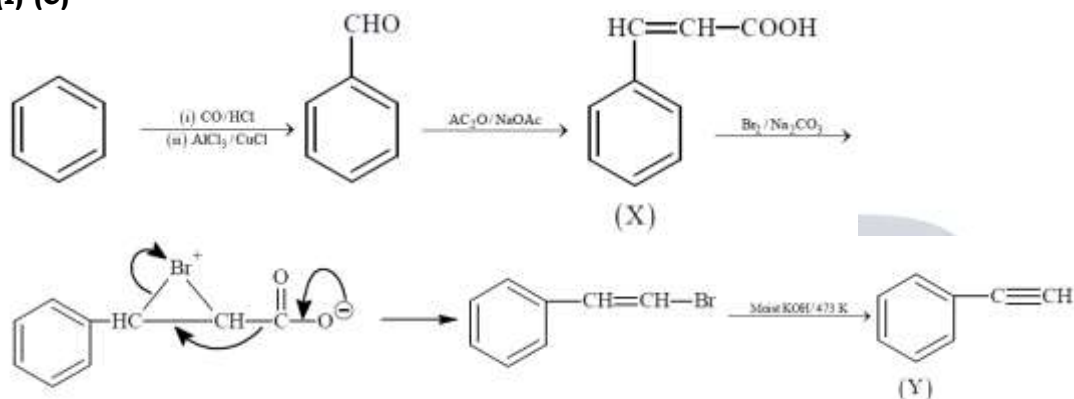
$$3 = \frac{\Delta T_{b(x)}}{\Delta T_{b(y)}} = \frac{\left(1 - \frac{\alpha_1}{2}\right) K_{b(x)}}{\left(1 - \frac{0.7}{2}\right) K_{b(y)}} \quad i = 1 - \frac{\alpha}{2}$$

$$3 = \frac{\left(1 - \frac{\alpha_1}{2}\right) \times 2}{\left(1 - \frac{0.7}{2}\right)}$$

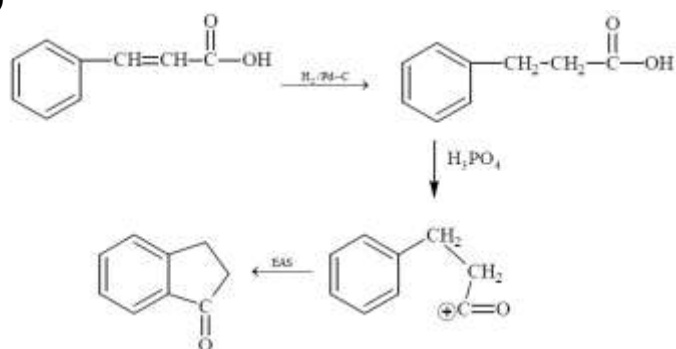
$$\left(1 - \frac{\alpha_1}{2}\right) = \frac{3 \times 0.65}{2} = 1.5 \times 0.65$$

$$\alpha_1 = 0.05$$

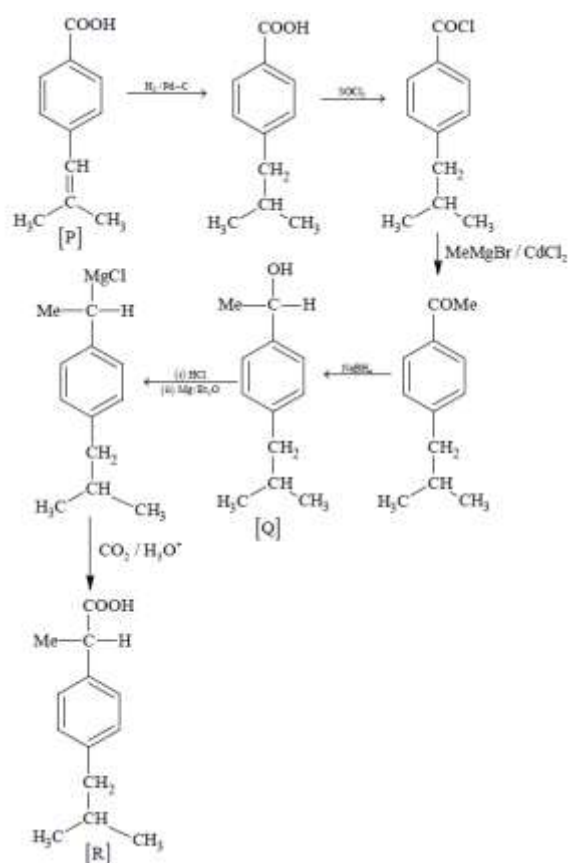
31. (i) (c)



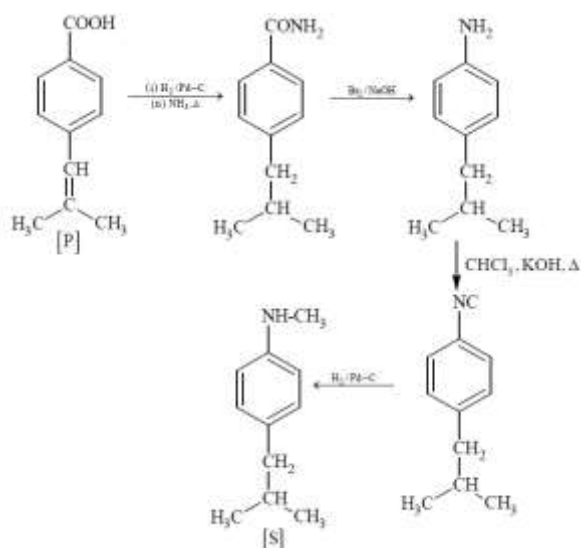
(ii) (a)



32. (i) (a)



(ii) (b)



33. (a, b, d)

(a) $\text{Arg}(-1-i) = -\frac{3\pi}{4}$

(b) $\text{Arg}(-1+it) = \begin{cases} \pi - \tan^{-1}(t) & \text{if } t \geq 0 \\ \tan^{-1}(t) - \pi & \text{if } t < 0 \end{cases}$

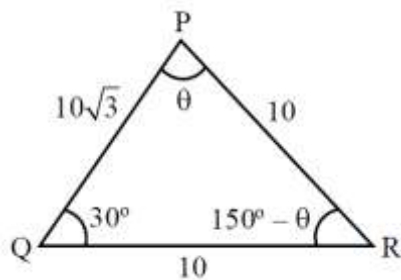
Not continuous at $t = 0$

(c) $\text{Arg}\left(\frac{z_1}{z_2}\right) - \arg(z_1) + \arg(z_2) = 0$

(d) $\text{Arg}\left(\frac{z-z_1}{z_2-z_1}\right) + \text{Arg}\left(\frac{z_2-z_3}{z-z_3}\right) = \pi$

$\Rightarrow z, z_1, z_2, z_3$ form a cyclic quadrilateral Hence locus of z is circle

34. (b, c, d)



$$(a) \frac{10}{\sin \theta} = \frac{10\sqrt{3}}{\sin(150^\circ - \theta)}$$

$$\Rightarrow \frac{\cos \theta}{2} + \frac{\sqrt{3}}{2} \sin \theta = \sqrt{3} \sin \theta$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \tan \theta \Rightarrow \theta = 30^\circ$$

$$(b) \Delta = \frac{1}{2} 10 \cdot 10\sqrt{3} \sin 30^\circ = 25\sqrt{3}, \angle QRP = 120^\circ$$

$$(c) r = \frac{\Delta}{s} = \frac{25\sqrt{3}}{10 + 5\sqrt{3}} = \frac{25\sqrt{3}(10 - 5\sqrt{3})}{25} = 10\sqrt{3} - 15$$

$$(d) \text{Area} = \pi R^2 = \frac{\pi}{4} \left(\frac{10}{1/2} \right)^2 = 100\pi$$

35. (c, d)

(a) Direction ratios of line of intersection are given by

$$(2\hat{i} + \hat{j} - \hat{k}) \times (\hat{i} + 2\hat{j} + \hat{k}) = 3\hat{i} - 3\hat{j} + 3\hat{k} \Rightarrow dr = (1, -1, 1)$$

$$(b) \vec{a} \cdot \vec{b} = (\hat{i} - \hat{j} + \hat{k}) \cdot (3\hat{i} - 3\hat{j} + 3\hat{k}) = 3 + 3 + 3 = 9 \neq 0$$

$$(c) \text{Angle between } P_1, P_2 = \cos^{-1} \left| \frac{2+2-1}{\sqrt{6} \cdot \sqrt{6}} \right| = \cos^{-1} \left(\frac{1}{2} \right) = 60^\circ$$

$$(d) P_3 : x - y + z = 0$$

$$\text{Distance of } (2, 1, 1) \text{ from the plane} = \frac{2}{\sqrt{3}}$$

36. (a, b, d)

L.M.V.T. in $[-4, 0]$

$$\frac{f(0) - f(-4)}{4} = f'(x_0)$$

$$|f'(x_0)| \leq \frac{|f(0)| + |f(-4)|}{4} \leq 1$$

If $f(x)$ periodic then $\lim_{x \rightarrow \infty} f(x) \neq 1$

Similarly, $|f'(x_1)| \leq 1$ for some $x_1 \in (0, 4)$

$$g(x) = (f(x))^2 + (f'(x))^2$$

$$g(x_0) \leq 5, g(x_1) \leq 5$$

$g(0) = 85$ it has a local maximum having value ≥ 85

Say α

$$g'(\alpha) = 0, g''(\alpha) < 0$$

$$2f(\alpha)f'(\alpha) + 2f''(\alpha)f'(\alpha) = 0$$

$$f(\alpha)(f(\alpha) + f''(\alpha)) = 0$$

as $f'(\alpha) \neq 0$

37. (b, c)

$$f'(x) = e^{f(x)-g(x)} \cdot g'(x) \text{ given } f(1) = g(2) = 1$$

$$\int -f'(x) \cdot e^{-f(x)} dx = \int -e^{-g(x)} \cdot g'(x) dx$$

$$\int d(e^{-f(x)}) = \int d(e^{-g(x)}) + C$$

$$e^{-f(x)} = e^{-g(x)} + C$$

$$\text{Put } x=1 \Rightarrow C = \frac{1}{e} - \frac{1}{e^{g(1)}}$$

$$x=2 \Rightarrow e^{f(2)} = \frac{e^{1+g(1)}}{2e^{g(1)} - e}$$

$$\Rightarrow g(1) > 1 - \log_e 2 \text{ \& } f(2) > 1 - \log_e 2$$

38. (b, c)

$$f(x) = 1 - 2x + e^x \int_0^x e^{-t} f(t) dt$$

$$\Rightarrow f'(x) = -2 + e^x \int_0^x e^{-t} f(t) dt + f(x)$$

$$\Rightarrow f'(x) = -2 + f(x) - 1 + 2x + f(x)$$

$$\Rightarrow f'(x) - 2f(x) = 2x - 3$$

$$f(x)e^{-2x} = \frac{2xe^{-2x}}{-2} - \frac{2e^{-2x}}{4} - \frac{3e^{-2x}}{-2} + C$$

$$\text{put } x=0, f(0)=1 \Rightarrow C=0$$

$$f(x)e^{-2x} = -xe^{-2x} + e^{-2x}$$

$$\Rightarrow f(x) = 1 - x$$

which passes through (2, -1)

$$\text{area} = \frac{\pi}{4} - \frac{1}{2} = \frac{\pi-2}{4}$$

$$39. (8) (\log_2 9)^{2 \log_{\log_2 9} 2} \times (\sqrt{7})^{\log_7 4} = 2^2 \times 4^{1/2} = 8$$

40. (625) Divisible by 4 $\Rightarrow$ last 2 digits divisible by 4 $\Rightarrow$ ends in 12, 24, 32, 44 or 52
 $\therefore 5^3 \times 5 = 625$

41. (3748)

$$n(X \cup Y) = n(X) + n(Y) - n(X \cap Y)$$

1, 6, 11, ..., 2018 term

$$T_n = 1 + (n-1)5 = 5n - 4$$

$$U_K = 9 + (K-1)7 = 7K + 2$$

for common terms

$$5n - 4 = 7K + 2$$

$$\Rightarrow n = \frac{7K+6}{5} \leq 2018, K \leq 1440$$

$$K = 2, 7, \dots, r$$

$$2 + (r-1)5 \leq 1440$$

$$\therefore r_{\max} = 288$$

$$\therefore \text{number of common term} = 288 = n(X \cap Y)$$

$$n(X \cup Y) = 2018 + 2018 - 288 = 3748.$$

42. (2)

$$\sin^{-1} \left(\frac{x^2}{1-x} - \frac{x \left(\frac{x}{2} \right)}{1 - \frac{x}{2}} \right) = \frac{\pi}{2} - \cos^{-1} \left(\frac{-x/2}{1 + \frac{x}{2}} - \frac{(-x)}{1+x} \right)$$

$$\Rightarrow \sin^{-1}\left(x^2\left(\frac{1}{1-x}-\frac{1}{2-x}\right)\right) = \frac{\pi}{2} - \cos^{-1}\left(x\left(\frac{1}{1+x}-\frac{1}{2+x}\right)\right)$$

$$\sin^{-1}\left[\frac{x^2}{(1-x)(2-x)}\right] = \frac{\pi}{2} - \cos^{-1}\left[\frac{x}{(1+x)(2+x)}\right] = \sin^{-1}\left[\frac{x}{(1+x)(2+x)}\right]$$

$$\Rightarrow x\left[\frac{x}{(1-x)(2-x)} - \frac{1}{(1+x)(2+x)}\right] = 0$$

$$x = 0 \text{ or } x^3 + 3x^2 + 2x = x^2 - 3x + 2$$

$$\Rightarrow x^3 + 2x^2 + 5x - 2 = 0$$

increasing function $\forall x$

$$f(0) = -2, f(1/2) > 0$$

$$\Rightarrow \text{one root between } \left(0, \frac{1}{2}\right)$$

$$\Rightarrow \text{total number of solutions} = 2$$

43. (1)

$$\ln(L) = \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{r=1}^n \ln\left(\frac{n+r}{n}\right)$$

$$= \int_0^1 \ln(1+x) dx$$

$$= \left[x \ln(1+x)\right]_0^1 - \left[x - \ln(1+x)\right]_0^1$$

$$= \ln 2 - (1 - \ln 2)$$

$$= \ln(4/e)$$

$$\Rightarrow L = 4/e \Rightarrow [L] = 1$$

44. (3)

$$\vec{c} \cdot \vec{a} = x \Rightarrow 2 \cos \alpha = x$$

$$\vec{c} \cdot \vec{b} = y \Rightarrow 2 \cos \alpha = y$$

$$\therefore |\vec{c}| = 2$$

$$\therefore x^2 + y^2 + 1 = 4 \Rightarrow 8 \cos^2 \alpha = 3$$

($\therefore \vec{a}, \vec{b}, \vec{a} \times \vec{b}$ all are $\perp$ to each other & are unit vectors)

45. (0.5)

$$\sqrt{3}a \cos x + 2b \sin x = c$$

$$\sqrt{3}a \cos\left(\frac{\pi}{3} - x\right) + 2b \sin\left(\frac{\pi}{3} - x\right) = c$$

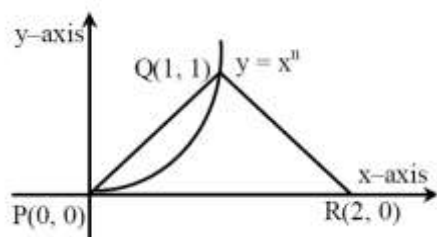
$$\Rightarrow \sqrt{3}a \left(\cos x \cdot \frac{1}{2} + \frac{\sin x \sqrt{3}}{2}\right) + 2b \left(\frac{\sqrt{3}}{2} \cos x - \frac{1}{2} \sin x\right) = c$$

$$\Rightarrow \left(\frac{\sqrt{3}}{2}a + \sqrt{3}b\right) \cos x + \left(\frac{3}{2}a - b\right) \sin x = c$$

$$\left(\sqrt{3}b - \frac{\sqrt{3}}{2}a\right) \cos x + \left(\frac{3}{2}a - 3b\right) \sin x = 0$$

$$\Rightarrow \frac{b}{a} = \frac{1}{2}$$

46. (4)



Area (ΔPQR) = 1 sq. unit

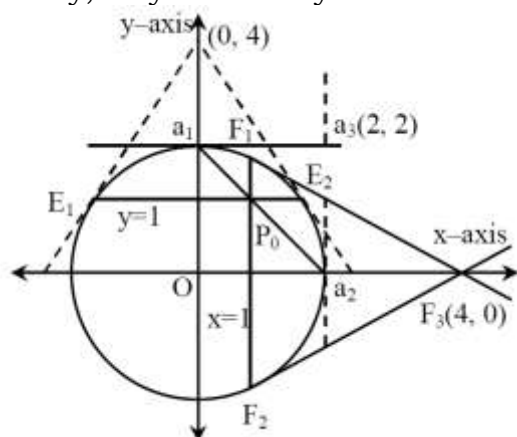
$$\Delta = \frac{1}{2} - \int_0^1 x^n dx = \frac{3}{10}$$

$$\Rightarrow \frac{1}{n+1} = \frac{1}{5}$$

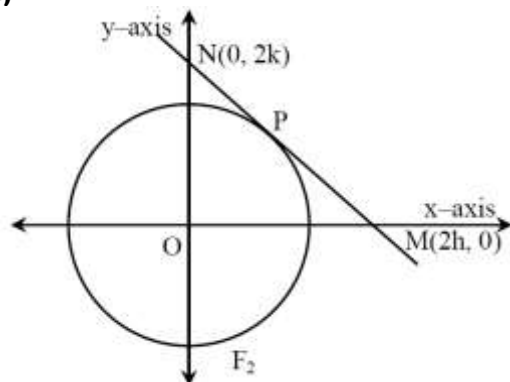
$$\Rightarrow n = 4.$$

47. (i) (a)

Clearly, they lie on $x + y = 4$



(ii) (d)



$$\frac{x}{2h} + \frac{y}{2k} = 1 \text{ and } \frac{xx_1}{4} + \frac{yy_1}{4} = 1 \text{ are same}$$

$$\Rightarrow x_1 = \frac{2}{h}, y_1 = \frac{2}{k}$$

$$\Rightarrow \frac{4}{h^2} + \frac{4}{k^2} = 4 \Rightarrow x^2 + y^2 = x^2 y^2$$

48. (i) (a)

$$P = \frac{D_4}{5!} = \frac{9}{120} = \frac{3}{40}$$

(ii)(c)

S_1	S_3	S_5	S_2	S_4
S_2	S_4	S_1	S_3	S_5
S_3	S_5	S_1	S_4	S_2
S_3	S_5	S_2	S_4	S_1
S_4	S_1	S_3	S_5	S_2
S_4	S_2	S_5	S_1	S_3
S_5	S_2	S_4	S_1	S_3

Same number of ways in reverse order

$$P(E) = \frac{n(E)}{n(S)} = \frac{7 \times 2}{5!} = \frac{7}{60}$$

