

PART-I PHYSICS

SECTION-A

1. A physical quantity P is given as

$$P = \frac{a^2 b^3}{c \sqrt{d}}$$

The percentage error in the measurement of a , b , c and d are 1%, 2%, 3% and 4% respectively. The percentage error in the measurement of quantity P will be

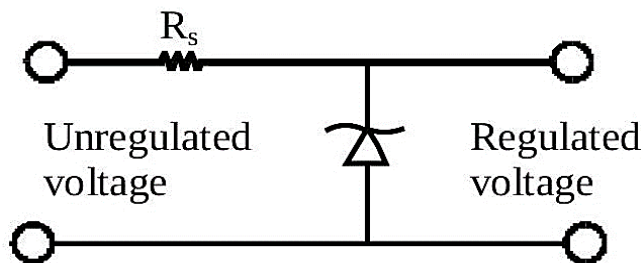
- (a) 13% (b) 14%
(c) 12% (d) 16%

2. Assuming the earth to be a sphere of uniform mass density, the weight of a body at a depth $d = \frac{R}{2}$ from the surface of earth, if its weight on the surface of earth is 200 N, will be:

(Given R = Radius of earth)

- (a) 400 N (b) 500 N
(c) 300 N (d) 100 N

3. A zener diode of power rating 1.6 W is to be used as voltage regulator. If the zener diode has a breakdown of 8 V and it has to regulate voltage fluctuating between 3 V and 10 V. The value of resistance R_s for safe operation of diode will be:



- (a) 13.3Ω (b) 12Ω
(c) 10Ω (d) 13Ω

4. The range of the projectile projected at an angle of 15° with horizontal is 50 m. If the projectile is projected with same velocity at an angle of 45° with horizontal, then its range will be:
(a) 50 m (b) $50\sqrt{2}$ m
(c) 100 m (d) $100\sqrt{2}$ m
5. A carrier wave of amplitude 15 V is modulated by a sinusoidal base band signal of amplitude 3 V. The ratio of maximum amplitude to minimum amplitude in an amplitude modulated wave is:
(a) 2 (b) $\frac{3}{2}$
(c) 5 (d) 1
6. The angular momentum for the electron in Bohr's orbit is L . If the electron is assumed to revolve in second orbit of hydrogen atom, then the change in angular momentum will be:
(a) $\frac{L}{2}$ (b) zero
(c) L (d) $2L$
7. A particle of mass m moving with velocity v collides with a stationary particle of mass $2m$. After collision, they stick together and continue to move together with velocity

- (a) v (b) $\frac{v}{2}$
(c) $\frac{v}{3}$ (d) $\frac{v}{4}$

8. Given below are two statement:

Statement I: If the number of turns in the coil of a moving coil galvanometer is doubled then the current sensitivity becomes double.

Statement II: Increasing current sensitivity of a moving coil galvanometer by only increasing the number of turns in the coil will also increase its voltage sensitivity in the same ratio:

In the light of the above statement, choose the correct answer from the options given below:

- (a) Statement I is false but Statement II is true
(b) Both Statement I and Statement II are true
(c) Both Statement I and Statement II are false
(d) Statement I is true but Statement II is false

9. Match List I with List II :

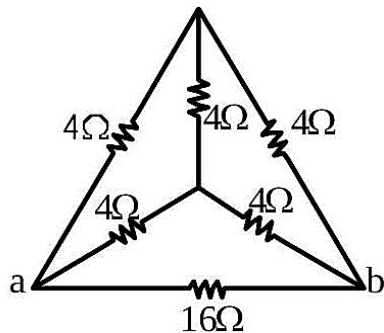
List-I		List II	
(A)	3 Translational degrees of freedom	(I)	Monoatomic gases
(B)	3 Translational, 2 rotational degrees of freedoms	(II)	Polyatomic gases
(C)	3 Translational, 2 rotational and 1 vibrational degrees of freedom	(III)	Rigid diatomic gases
(D)	3 Translational, 3 rotational and more than one vibrational degrees of freedom	(IV)	Nonrigid diatomic gases

Choose the correct answer from the options given below:

- (a) (A) - (IV), (B) - (III), (C) - (II), (D) - (I)
(b) (A) - (IV), (B) - (II), (C) - (I), (D) - (III)
(c) (A) - (I), (B) - (III), (C) - (IV), (D) - (II)

(d) (A) - (I), (B) - (IV), (C) - (III), (D) - (II)

10. The equivalent resistance of the circuit shown below between points a and b is :



- (a) 24Ω (b) 3.2Ω
(c) 20Ω (d) 16Ω

11. Consider two containers A and B containing monoatomic gases at the same Pressure (P), Volume (V) and Temperature (T). The gas in A is compressed isothermally to $\frac{1}{8}$ of its original volume while the gas B is compressed adiabatically to $\frac{1}{8}$ of its original volume. The ratio of final pressure of gas in B to that of gas in A is:

- (a) 8 (b) $8^{\frac{3}{2}}$
(c) $\frac{1}{8}$ (d) 4

12. Given below are two statements:

Statement I: Maximum power is dissipated in a circuit containing an inductor, a capacitor and a resistor connected in series with an AC source, when resonance occurs

Statement II: Maximum power is dissipated in a circuit containing pure resistor due to zero phase difference between current and voltage.

In the light of the above statements, choose the correct answer from the options given below:

- (a) Statement I is false but Statement II is true
(b) Statement I is true but Statement II is false
(c) Both Statement I and Statement II are true
(d) Both Statement I and Statement II are false

13. Two satellites of masses m and $3m$ revolve around the earth in circular orbits of radii r & $3r$ respectively. The ratio of orbital speeds of the satellites respectively is:

- (a) 1:1 (b) 3:1
(c) $\sqrt{3}$:1 (d) 9:1

14. Given below are two statements:

Statement I: Pressure in a reservoir of water is same at all points at the same level of water.

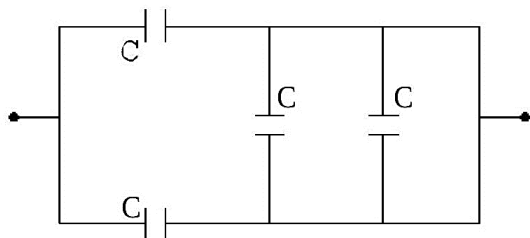
Statement II: The pressure applied to enclosed water is transmitted in all directions equally.

In the light of the above statements, choose the correct answer from the options given below:

- (a) Statement I is false but Statement II is true
(b) Both Statement I and Statement II are true

- (c) Statement I is true but Statement II is false
 (d) Both Statement I and Statement II are false

15. The equivalent capacitance of the combination shown is



- (a) $\frac{C}{2}$ (b) $4C$
 (c) $2C$ (d) $\frac{5}{3}C$

16. The energy of an electromagnetic wave contained in a small volume oscillates with

- (a) zero frequency
 (b) half the frequency of the wave
 (c) double the frequency of the wave
 (d) the frequency of the wave

17. An object is placed at a distance of 12 cm in front of a plane mirror. The virtual and erect image is formed by the mirror. Now the mirror is moved by 4 cm towards the stationary object. The distance by which the position of image would be shifted, will be:

- (a) 4 cm towards mirror (b) 8 cm towards mirror
 (c) 8 cm away from mirror (d) 2 cm towards mirror

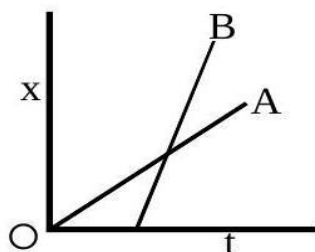
18. The de Broglie wavelength of a molecule in a gas at room temperature (300 K) is λ_1 . If the temperature of the gas is increased to 600 K, then the de Broglie wavelength of the same gas molecule becomes

- (a) $\frac{1}{\sqrt{2}}\lambda_1$ (b) $2\lambda_1$
 (c) $\frac{1}{2}\lambda_1$ (d) $\sqrt{2}\lambda_1$

19. A particle executes S.H.M. of amplitude A along x -axis. At $t = 0$, the position of the particle is $x = \frac{A}{2}$ and it moves along positive x -axis the displacement of particle in time t is $x = A\sin(\omega t + \delta)$, then the value δ will be:

- (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{3}$
 (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{2}$

20. The position-time graphs for two students A and B returning from the school to their homes are shown in figure:



(A) A lives closer to the school

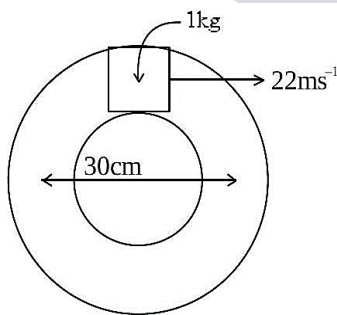
- (B) B lives closer to the school
(C) A takes lesser time to reach home
(D) A travels faster than B
(E) B travels faster than A

Choose the correct answer from the options given below:

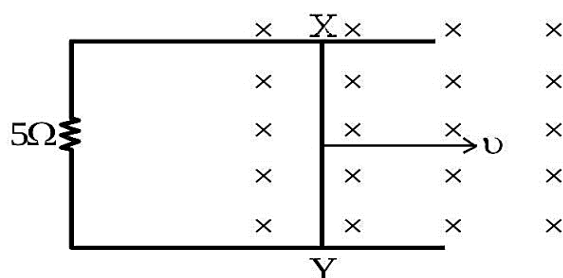
- (a) (A) and (E) only (b) (B) and (E) only
(c) (A), (C) and (E) only (d) (A), (C) and (D) only

SECTION-B

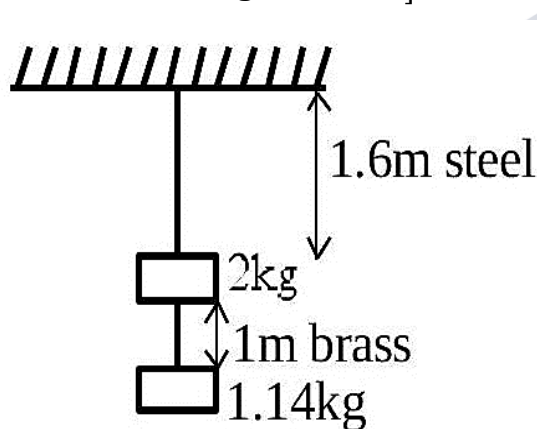
21. Unpolarised light of intensity 32Wm^{-2} passes through the combination of three polaroids such that the pass axis of the last polaroid is perpendicular to that of the pass axis of first polaroid. If intensity of emerging light is 3Wm^{-2} , then the angle between pass axis of first two polaroids is
22. A closed circular tube of average radius 15 cm, whose inner walls are rough, is kept in vertical plane. A block of mass 1 kg just fit inside the tube. The speed of block is 22 m/s, when it is introduced at the top of tube. After completing five oscillations, the block stops at the bottom region of tube. The work done by the tube on the block is ___ J. [Given $g = 10\text{ m/s}^2$]



23. If the earth suddenly shrinks to $\frac{1}{64}$ th of its original volume with its mass remaining the same, the period of rotation of earth becomes $\frac{24}{x}$ h. The value of x is ___
24. The current required to be passed through a solenoid of 15 cm length and 60 turns in order to demagnetise a bar magnet of magnetic intensity $2.4 \times 10^3\text{Am}^{-1}$ is ___ A.
25. A 1 m long metal rod XY completes the circuit as shown in figure. The plane of the circuit is perpendicular to the magnetic field of flux density 0.15 T. If the resistance of the circuit is 5Ω , the force needed to move the rod in direction, as indicated, with a constant speed of 4 m/s will be ___ 10^{-3} N.



26. A transverse harmonic wave on a string is given by $y(x, t) = 5\sin(6t + 0.003x)$ where x and y are in cm and t in sec. The wave velocity is $__\text{ms}^{-1}$.
27. The decay constant for a radioactive nuclide is $1.5 \times 10^{-5} \text{ s}^{-1}$. Atomic of the substance is 60 g mole $^{-1}$, ($N_A = 6 \times 10^{23}$). The activity of $1.0\mu\text{g}$ of the substance is $__\times 10^{10} \text{ Bq}$.
28. Three concentric spherical metallic shells X, Y and Z of radius a, b and c respectively [$a < b < c$] have surface charge densities $\sigma, -\sigma$ and σ , respectively. The shells X and Z are at same potential. If the radii of X&Y are 2 cm and 3 cm, respectively. The radius of shell Z is $__\text{cm}$.
29. 10 resistors each of resistance 10Ω can be connected in such as to get maximum and minimum equivalent resistance. The ratio of maximum and minimum equivalent resistance will be $__\$
30. Two wires each of radius 0.2 cm and negligible mass, one made of steel and other made of brass are loaded as shown in the figure. The elongation of the steel wire is $__\times 10^{-6} \text{ m}$. [Young's modulus for steel = $2 \times 10^{11} \text{ Nm}^{-2}$ and $g = 10 \text{ ms}^{-2}$]



PART-II CHEMISTRY

SECTION-A

31. Using column chromatography, mixture of two compounds 'A' and 'B' was separated. 'A' eluted first, this indicates 'B' has
- low R_f , weaker adsorption
 - high R_f , stronger adsorption
 - high R_f , weaker adsorption
 - low R_f , stronger adsorption
32. Prolonged heating is avoided during the preparation of ferrous ammonium sulphate to
- prevent oxidation
 - prevent reduction
 - prevent hydrolysis
 - prevent breaking

33. Lime reacts exothermally with water to give 'A' which has low solubility in water. Aqueous solution of 'A' is often used for the test of CO_2 , a test in which insoluble B is formed. If B is further reacted with CO_2 then soluble compound is formed 'A' is

- (a) Quick lime (b) Slaked lime
(c) Lime water (d) White lime

34. The pair from the following pairs having both compounds with net non-zero dipole moment is

- (a) Benzene, anisidine
(b) 1,4-Dichlorobenzene, 1,3-Dichlorobenzene
(c) CH_2Cl_2 , CHCl_3
(d) cis-butene, trans-butene

35. Match List-I with List-II

List-I

Industry

(A) Steel plants

(B) Thermal power plants

(C) Fertilizer industries

(D) Paper mills

List-II

Waste Generated

(I) Gypsum

(II) Fly ash

(III) Slag

(IV) Bio-degradable Wastes

Choose the correct answer from the options given below:

- (a) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
(b) (A)-(II), (B)-(III), (C)-(IV), (D)-(I)
(c) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)
(d) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

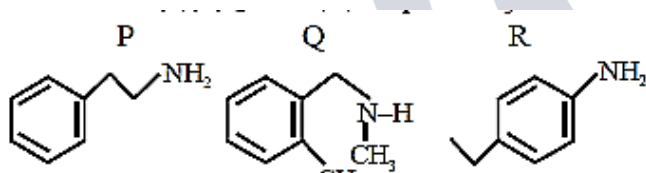
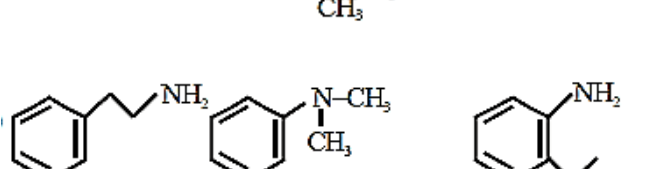
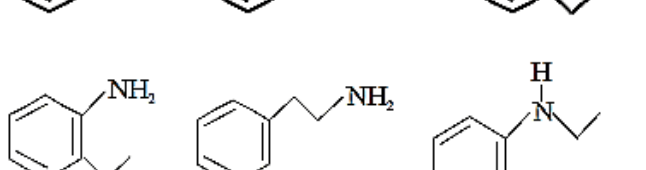
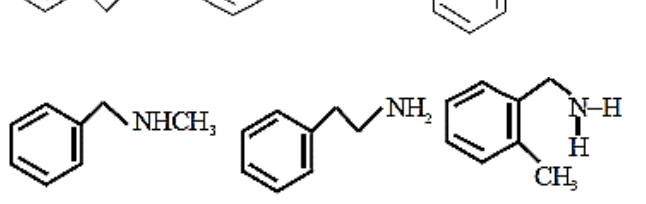
36. Isomeric amines with molecular formula $\text{C}_8\text{H}_{11}\text{N}$ give the following tests

Isomer (P) $\Rightarrow$ Can be prepared by Gabriel phthalimide synthesis

Isomer (Q) $\Rightarrow$ Reacts with Hinsberg's reagent to give solid insoluble in NaOH

Isomer (R) $\Rightarrow$ Reacts with HONO followed by β -naphthol in NaOH to give red dye.

Isomers (P), (Q) and (R) respectively are

- (a) 
(b) 
(c) 
(d) 

37. Given below are two statements

Statement I: Aqueous solution of $K_2Cr_2O_7$ is preferred as a primary standard in volumetric analysis over $Na_2Cr_2O_7$ aqueous solution

Statement II: $K_2Cr_2O_7$ has a higher solubility in water than $Na_2Cr_2O_7$

In the light of the above statements, choose the correct answer from the options given below:

- (a) Both Statement I and Statement II are true
- (b) Both Statement I and Statement II are false
- (c) Both Statement I is true but Statement II is false
- (d) Both Statement I is false but Statement II is true

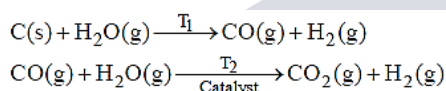
38. The one that does not stabilize 2° and 3° structures of proteins is

- (a) H-bonding
- (b) -S-S-linkage
- (c) -O-O-linkage
- (d) van der Waals forces

39. Given below are two reactions, involved in the commercial production of dihydrogen (H_2).

The two reactions are carried out at temperature " T_1 " and " T_2 " respectively

The temperature T_1 and T_2 are correctly related as



- (a) $T_1 > T_2$
- (b) $T_1 = T_2$
- (c) $T_1 = 100 \text{ K}, T_2 = 1270 \text{ K}$
- (d) $T_1 < T_2$

40. Which of the following statements are correct?

- (A) The M^{3+}/M^{2+} reduction potential for iron is greater than manganese
- (B) The higher oxidation states of first row d-block elements get stabilized by oxide ion.
- (C) Aqueous solution of Cr^{2+} can liberate hydrogen from dilute acid.
- (D) Magnetic moment of V^{2+} is observed between 4.4-5.2 BM

Choose the correct answer from the options given below:

- (a) (B), (C) only
- (b) (D) only
- (c) (A), (B), (D) only
- (d) (B) only

41. Which of the following is used as a stabilizer during the concentration of sulphide ores?

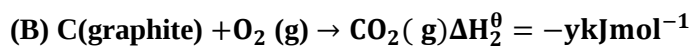
- (a) Pine oils
- (b) Xanthates
- (c) Fatty acids
- (d) Cresols

42. The octahedral diamagnetic low spin complex among the following is

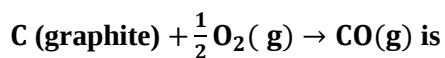
- (a) $[NiCl_4]^{2-}$
- (b) $[CoCl_6]^{3-}$
- (c) $[CoF_6]^{3-}$
- (d) $[Co(NH_3)_6]^{3+}$

43. Given





The ΔH^θ for the reaction



- (a) $\frac{x-2y}{2}$ (b) $\frac{x+2y}{2}$
(c) $\frac{2x-y}{2}$ (d) $2y - x$

44. The compound which does not exist is

- (a) NaO_2 (b) $(\text{NH}_4)_2\text{BeF}_4$
(c) BeH_2 (d) PbEt_4

45. Match List I with List II

List-I Polymer	List-II Type/Class
(A) Nylon-2-Nylon-6	(I) Thermosetting Polymer
(B) Buna-N	(II) Biodegradable polymer
(C) Urea-formaldehyde	(III) Synthetic rubber resin
(D) Dacron	(IV) Polyester

Choose the correct answer from the options given below:

- (a) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)
(b) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)
(c) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)
(d) (A)-(II), (B)-(III), (C)-(I), (D)-(IV)

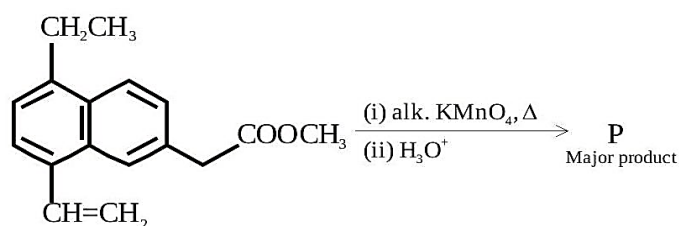
46. The number of molecules and moles in 2.8375 litres of O_2 at STP are respectively

- (a) 7.527×10^{22} and 0.250 mol
(b) 1.505×10^{23} and 0.250 mol
(c) 7.527×10^{23} and 0.125 mol
(d) 7.527×10^{22} and 0.125 mol

47. The enthalpy change for the adsorption process and micelle formation respectively are

- (a) $\Delta H_{\text{ads}} < 0$ and $\Delta H_{\text{mic}} > 0$
(b) $\Delta H_{\text{ads}} < 0$ and $\Delta H_{\text{mic}} < 0$
(c) $\Delta H_{\text{ads}} > 0$ and $\Delta H_{\text{mic}} < 0$
(d) $\Delta H_{\text{ads}} > 0$ and $\Delta H_{\text{mic}} > 0$

48. The major product 'P' formed in the given reaction is



- (a)
- (b)
- (c)
- (d)

49. Suitable reaction condition for preparation of Methyl phenyl ether is

- (a) $\text{Ph} - \text{Br}, \text{MeO}^- \text{Na}^+$ (b) $\text{PhO}^- \text{Na}^+, \text{MeOH}$
 (c) $\text{PhO}^- \text{Na}^+, \text{MeBr}$ (d) Benzene, MeBr

50. Identify the correct order of reactivity for the following pairs towards the respective mechanism

- (A) $\text{S}_{\text{N}}2$ $>$
- (B) $\text{S}_{\text{N}}1$ $>$
- (C) Electrophilic substitution $>$

- (D) Nucleophilic substitution $>$

Choose the correct answer from the options given below:

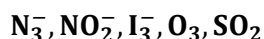
- (a) (A), (B) and (D) only (b) (A), (B), (C) and (D)
 (c) (A), (C) and (D) only (d) (B), (C) and (D) only

SECTION-B

51. The number of correct statement/s involving equilibria in physical process from the following is

- (A) Equilibrium is possible only in a closed system at a given temperature
- (B) Both the opposing processes occur at the same rate.
- (C) When equilibrium is attained at a given temperature, the value of all its parameters became equal
- (D) For dissolution of solids in liquids, the solubility is constant at a given temperature

52. The number of bent-shaped molecule/s from the following is___

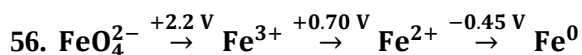
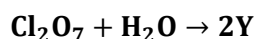
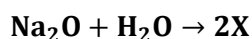


53. A molecule undergoes two independent first order reactions whose respective half-lives are 12 min and 3 min. If both the reactions are occurring then the time taken for the 50% consumption of the reactant is ___min. (Nearest integer)

54. number of incorrect statement/s about the black body from the following is

- (A) Emit or absorb energy in the form of electromagnetic radiation
- (B) Frequency distribution of the emitted radiation depends on temperature
- (C) At a given temperature, intensity vs frequency curve passes through a maximum value
- (D) The maximum of the intensity vs frequency curve is at a higher frequency at higher temperature compared to that at lower temperature

55. In the following reactions, the total number of oxygen atoms in X and Y is___



$E^\theta_{\text{FeO}_4^{2-}/\text{Fe}^{2+}}$ is $x \times 10^{-3} \text{ V}$. The value of x is___

57. If the degree of dissociation of aqueous solution of weak monobasic acid is determined to be 0.3 , then the observed freezing point will be___ % higher than the expected/theoretical freezing point. (Nearest integer)

58. In potassium ferrocyanide, there are ___pairs of electrons in the t_{2g} set of orbitals

59. At constant temperature a gas is at a pressure of 940.3 mmHg. The pressure at which its volume decreases by 40% is ___mm Hg. (Nearest Integer)

60. The sum of lone pairs present on the central atom of the interhalogen IF_5 and IF_7 is_

PART-III MATHEMATICS

SECTION-A

61. Let O be the origin and the position vector of the point P be $-\hat{i} - 2\hat{j} + 3\hat{k}$. If the position vectors of the points A, B and C are $-2\hat{i} + \hat{j} - 3\hat{k}$, $2\hat{i} + 4\hat{j} - 2\hat{k}$ and $-4\hat{i} + 2\hat{j} - \hat{k}$ respectively then the projection of the vector $\overrightarrow{OP}$ on a vector perpendicular to the vectors $\overrightarrow{AB}$ and $\overrightarrow{AC}$ is
- (a) 3 (b) $\frac{8}{3}$
(c) $\frac{10}{3}$ (d) $\frac{7}{3}$
62. Let the ellipse $E: x^2 + 9y^2 = 9$ intersect the positive x - and y -axes at the points A and B respectively. Let the major axis of E be a diameter of the circle C . Let the line passing through A and B meet the circle C at the point P . If the area of the triangle which vertices A, P and the origin O is $\frac{m}{n}$, where m and n are coprime, then $m - n$ is equal to
- (a) 18 (b) 16
(c) 17 (d) 15
63. If $f(x) = \frac{(\tan 1^\circ)x + \log_e(123)}{x \log_e(1234) - (\tan 1^\circ)}$, $x > 0$, then the least value of $f(f(x)) + f\left(f\left(\frac{4}{x}\right)\right)$ is
- (a) 8 (b) 4
(c) 2 (d) 0
64. A square piece of tin of side 30 cm is to be made into a box without top by cutting a square from each corner and folding up the flaps to form a box. If the volume of the box is maximum, then its surface area (in cm^2) is equal to
- (a) 675 (b) 1025
(c) 800 (d) 900
65. Let f be a differentiable function such that $x^2 f(x) - x = 4 \int_0^x t f(t) dt$, $f(a) = \frac{2}{3}$. Then $18f(c)$ is equal to
- (a) 160 (b) 210
(c) 180 (d) 150
66. A line segment AB of length λ moves such that the points A and B remain on the periphery of a circle of radius λ . Then the locus of the point, that divides the line segment AB in the ratio 2:3, is a circle of radius
- (a) $\frac{3}{5}\lambda$ (b) $\frac{\sqrt{19}}{7}\lambda$
(c) $\frac{2}{3}\lambda$ (d) $\frac{\sqrt{19}}{5}\lambda$
67. Let the complex number $z = x + iy$ be such that $\frac{2z-3i}{2z+i}$ is purely imaginary. If $x + y^2 = 0$, then $y^4 + y^2 - y$ is equal to:
- (a) $\frac{3}{2}$ (b) $\frac{4}{3}$
(c) $\frac{2}{3}$ (d) $\frac{3}{4}$
68. $96 \cos \frac{\pi}{33} \cos \frac{2\pi}{33} \cos \frac{4\pi}{33} \cos \frac{8\pi}{33} \cos \frac{16\pi}{33}$ equal to
- (a) 3 (b) 2
(c) 4 (d) 1

69. If A is a 3×3 matrix and $|A| = 2$, then $|3\text{adj}(|3A|A^2)|$ is equal to

- (a) $3^{11} \cdot 6^{10}$ (b) $3^{12} \cdot 6^{10}$
(c) $3^{10} \cdot 6^{11}$ (d) $3^{12} \cdot 6^{11}$

70. The slope of tangent at any point (x, y) on a curve $y = y(x)$ is $\frac{x^2+y^2}{2xy}$, $x > 0$. If $y(b) = 0$, then a value of $y(8)$ is

- (a) $-2\sqrt{3}$ (b) $4\sqrt{3}$
(c) $2\sqrt{3}$ (d) $-4\sqrt{2}$

71. For the system of linear equations

$$2x - y + 3z = 5$$

$$3x + 2y - z = 7$$

$$4x + 5y + \alpha z = \beta$$

Which of the following is NOT correct?

- (a) The system has infinitely many solutions for $\alpha = -5$ and $\beta = 9$
(b) The system has a unique solution for $\alpha \neq -5$ and $\beta = 8$
(c) The system has infinitely many solutions for $\alpha = -6$ and $\beta = 9$
(d) The system is inconsistent for $\alpha = -5$ and $\beta = 8$

72. Let N denotes the sum of the numbers obtained when two dice are rolled. If the probability that $2^N < N!$ is $\frac{m}{n}$, where m and n are coprime, then $4m - 3n$ is equal to

- (a) 8 (b) 16
(c) 10 (d) 12

73. Let P be the point of intersection of the line $\frac{x+3}{3} = \frac{y+2}{1} = \frac{1-z}{2}$ and the plane $x + y + z = 2$. If the distance of the point P from the plane $3x - 4y + 12z = 32$ is q , then q and $2q$ are the roots of the equation

- (a) $x^2 - 18x - 72 = 0$ (b) $x^2 + 18x + 72 = 0$
(c) $x^2 - 18x + 72 = 0$ (d) $x^2 + 18x - 72 = 0$

74. The negation of the statement $(p \vee q) \wedge (q \vee (\sim r))$ is

- (a) $((\sim p) \vee r) \wedge (\sim q)$ (b) $((\sim p) \vee (\sim q)) \wedge (\sim r)$
(c) $((\sim p) \vee (\sim q)) \vee (\sim r)$ (d) $(p \vee r) \wedge (\sim q)$

75. If the coefficient of x^7 in $\left(ax - \frac{1}{bx^2}\right)^{13}$ and the coefficient of x^{-5} in $\left(ax + \frac{1}{bx^2}\right)^{13}$ are equal, then a^4b^4 is equal to:

- (a) 44 (b) 22
(c) 11 (d) 33

76. Let two vertices of triangle ABC be $(2, 4, 6)$ and $(0, -2, -5)$, and its centroid be $(2, 1, -1)$. If the image of third vertex in the plane $x + 2y + 4z = 11$ is (α, β, γ) , then $\alpha\beta + \beta\gamma + \gamma\alpha$ is equal to

- (a) 72 (b) 74
(c) 76 (d) 70

77. The shortest distance between the lines $\frac{x+2}{1} = \frac{y}{-2} = \frac{z-5}{2}$ and $\frac{x-4}{1} = \frac{y-1}{2} = \frac{z+3}{0}$ is

- (a) 6 (b) 9
(c) 7 (d) 8

78. If $I(x) = \int e^{\sin^2 x} (\cos x \sin 2x - \sin x) dx$ and $I(0) = 1$, then $I\left(\frac{\pi}{3}\right)$ is equal to

- (a) $-\frac{1}{2}e^{\frac{3}{4}}$ (b) $e^{\frac{3}{4}}$
(c) $\frac{1}{2}e^{\frac{3}{4}}$ (d) $-e^{\frac{3}{4}}$

79. Let the first term a and the common ratio r of a geometric progression be positive integers. If the sum of its squares of first three terms is 33033, then the sum of these three terms is equal to

- (a) 231 (b) 210
(c) 220 (d) 241

80. An arc PQ of a circle subtends a right angle at its centre O. The mid point of the arc PQ is R. If $\overrightarrow{OP} = \vec{u}$, $\overrightarrow{OR} = \vec{v}$ and $\overrightarrow{OQ} = \alpha\vec{u} + \beta\vec{v}$, then α, β^2 are the roots of the equation

- (a) $x^2 - x - 2 = 0$ (b) $3x^2 + 2x - 1 = 0$
(c) $x^2 + x - 2 = 0$ (d) $3x^2 - 2x - 1 = 0$

SECTION-B

81. The coefficient of x^7 in $(1 - x + 2x^3)^{10}$ is

82. Let $f: (-2, 2) \rightarrow \mathbb{R}$ be defined by

$$f(x) = \begin{cases} x[x] & , -2 < x < 0 \\ (x-1)[x] & , 0 \leq x < 2 \end{cases}$$

Where $[x]$ denotes the greatest integer function. If m and n respectively are the number of points in $(-2, 2)$ at which $y = |f(x)|$ is not continuous and not differentiable, then $m + n$ is equal to__

83. The sum of all those terms, of the arithmetic progression 3, 8, 13, ... 373, which are not divisible by 3, is equal to__

84. Let a common tangent to the curves $y^2 = 4x$ and $(x-4)^2 + y^2 = 16$ touch the curves at the points P and Q. Then $(PQ)^2$ is equal to__

85. The number of permutations, of the digits 1, 2, 3, ..., 7 without repetition, which neither contain the string 153 nor the string 2467, is__

86. Let a, b, c be three distinct positive real numbers such that $(2a)^{\log_e a} = (bc)^{\log_e b}$ and $b^{\log_e 2} = a^{\log_e c}$. Then $6a + 5bc$ is equal to__

87. Let $y = p(x)$ be the parabola passing through the points $(-1, 0)$, $(0, 1)$ and $(1, 0)$. If the area of the region $\{(x, y): (x+1)^2 + (y-1)^2 \leq 1, y \leq p(x)\}$ is A, then $12(\pi - 4A)$ is equal to__

88. If the mean of the frequency distribution

Class :	0-10	10-20	20-30	30-40	40-50
Frequency	2	3	x	5	4

is 28, then its variance is

89. Some couples participated in a mixed doubles badminton tournament. If the number of matches played, so that no couple played in a match, is 840, then the total numbers of persons, who participated in the tournament, is__

90. The number of elements in the set $\{n \in \mathbb{Z} : |n^2 - 10n + 19| < 6\}$ is__

