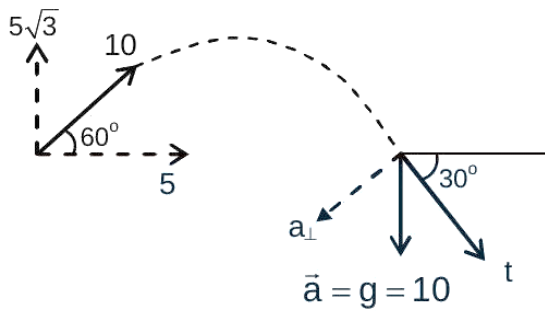


1. (b)



at $t = 1$

$$u_x = 5, u_y = 5\sqrt{3}$$

$$v_y = 5\sqrt{3} - 10; v_x = 5$$

$$\tan \theta = -(2 - \sqrt{3}) \Rightarrow \theta = -30^\circ$$

$$R = \frac{v^2}{a_{\perp}} = \frac{10^2}{(10 \cos 30^\circ)}$$

$$= \frac{10}{\sqrt{3}} \times 2 = \frac{20}{\sqrt{3}} \text{ m}$$

$$\frac{5^2 + (10 - 5\sqrt{3})^2}{10 \cos \theta} = \frac{200 - 100\sqrt{3}}{10 \times 0.965} = 2.8 \text{ m}$$

2. (c) Energy supplied

$$E = \frac{12400}{900} = 12.65 \text{ eV}$$

$$\therefore E_n - E_1 = 12.65$$

$$\Rightarrow (13.6) \left(1 - \frac{1}{n^2}\right) = 12.65$$

$$\Rightarrow n^2 \approx 14.3$$

$$\Rightarrow n \approx 4$$

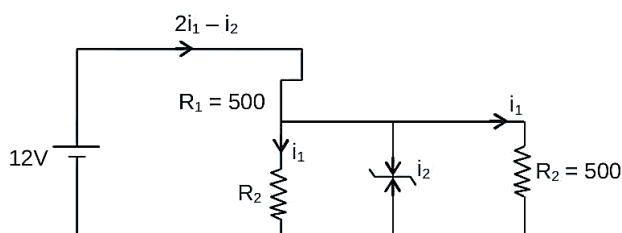
$$r \propto n^2$$

3. (a) $12 - 500(2i_1 + i_2) - 10 = 0$

$$\Rightarrow 2i_1 + i_2 = \frac{2}{500} = \frac{1}{250}$$

$< i_1$ when zenor has break down.

So, $i_2 = 0$.



4. (d) $\frac{M}{L} = \frac{\mu_0 n n_1 n_2 n_1^2 \ell}{\mu_0 \pi n_1^2 r_1^2 \ell}$

$$= \frac{n_2}{n_1}$$

5. (d) $K = \frac{1}{2}mv^2; U = \frac{1}{2}kx^2 = \frac{1}{2}m^2x^2$

$$\begin{aligned} \therefore \frac{k}{U} &= \frac{v^2}{\omega^2 x^2} = \left(\frac{\cos(wt)}{\sin(wt)} \right)^2 \\ &= \cot^2 \left(\frac{\pi}{90} \times 210 \right) \\ &= \cot^2 \left(2\pi + \frac{\pi}{3} \right) \\ &= \left(\frac{1}{\sqrt{3}} \right)^2 = \frac{1}{3}. \end{aligned}$$

6. (d) $\Delta v = v_f - v_i$

$$\begin{aligned} &= \sqrt{\frac{2gMe}{R_e}} - \sqrt{\frac{gMe}{R_e}} \\ &= (\sqrt{2} - 1)\sqrt{gR_e} \end{aligned}$$

7. (b) Power of e should be dimensionless.

$$\begin{aligned} \text{So, } [\lambda] &= (\alpha T k) \\ \Rightarrow L^2 &= [\alpha](ML^2 T^{-2}) \\ \Rightarrow (\alpha) &= (M^{-1} T^2) \\ \Rightarrow E &= \frac{1}{2}KT \\ \Rightarrow (ML^2 T^{-2}); (E) &= [KT] \\ \Rightarrow (\alpha\beta) &= (F) \\ \Rightarrow (M^{-1} T^2)(\beta) &= (MLT^{-2}) \end{aligned}$$

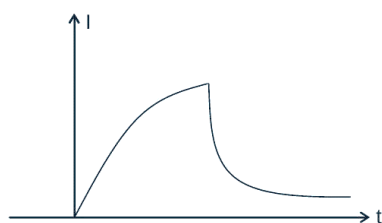
8. (b)

$$\Delta x = \frac{\lambda}{8}$$

$$\text{Phase } |\Delta P| = \frac{2\pi}{\lambda} \times \frac{\lambda}{8} = \frac{\pi}{4}$$

$$\begin{aligned} \therefore I_{\text{res}} &= I + I + 2I \cos\left(\frac{R}{4}\right) \\ &= 2I \left(1 + \frac{1}{\sqrt{2}} \right) = 2I \times 1.7 \\ \therefore \frac{I_{\text{res}}}{I_{\text{man}}} &= \frac{2I \times 1.7}{4I} = 0.85 \end{aligned}$$

9. (b)



Above is the correct graph for growth and decay of current.

$$10. (b) U_{\text{Total}} = \frac{kQq}{a} + \frac{kq^2}{a} + \frac{kQq}{a\sqrt{2}} = 0$$

$$\Rightarrow Q = \frac{-q}{\left(1 + \frac{1}{\sqrt{2}}\right)}$$

11. (a) Prism formula

$$D_m = S_m = (n - 1)A \text{ (for thin prism)}$$

12. (a) $I \propto m\ell^2$ (let σ = mass per unit area)

$$\therefore I_1 \propto \ell^4$$

$$\text{and } I_2 \propto \left(\frac{\ell}{2}\right)^4$$

$$\text{So, } I_2 = \frac{1}{16}$$

$$\text{Moment of inertia of remaining sheet} = 1 - \frac{1}{16}$$

$$= \frac{15}{16}$$

13. (b)

$$\vec{\tau}_0 = \vec{\tau}_1 + \vec{\tau}_2$$

$$\begin{aligned} &= (6\hat{i}) \times \left(-\frac{F}{2}\hat{i} + \frac{F\sqrt{3}}{2}\hat{j}\right) + (2\hat{i} + 3\hat{j}) \times (F\hat{k}) \\ &= -3F\hat{k}(-2F\hat{j} + 3F\hat{i}) \\ &= F(3\hat{i} - 2\hat{j} - 3\hat{k}) \end{aligned}$$

14. (d)

$$\times 0.5 \times 20 + (m - 20) \times 80$$

$$= 50 \times 1 \times 40$$

$$\Rightarrow 90m - 1600 = 2000$$

$$\Rightarrow 90m = 3600$$

$$\Rightarrow m = 40\text{gm}$$

$$15. (d) \Delta \vec{v} = 2v \sin\left(\frac{\theta}{2}\right)$$

$$= 2 \times 10 \times \sin(30^\circ)$$

$$= 10 \text{ m/s}$$

$$16. (c) f_{so} = f_c \pm f_m$$

$$= \frac{\omega_c \pm \omega_m}{2\pi}$$

$$= \frac{(5.5 \pm 0.22) \times 10^5}{2 \times \frac{22}{7}}$$

$$= 89.25, 85.75$$

17. (d) $\frac{1}{v} - \frac{1}{-20} = \frac{1}{30}$

$$\Rightarrow \frac{1}{V} = \frac{1}{0.30} - \frac{1}{20} = + \frac{200 - 3}{60} = \frac{197}{60}$$

$$\Rightarrow -\frac{dV}{dtV^2} + \frac{du}{dtu^2} = 0$$

$$\Rightarrow \frac{dV}{dt} = \frac{V^2}{u^2} \frac{du}{dt} = \left(\frac{3}{197}\right)^2 \times (-5) = -0.00116 \text{ m/s}$$

18. (a) $U_{\text{total}} = U_{\text{O}_2} + U_{\text{Ar}}$

$$= \frac{3 \times 5 \times RT}{2} + \frac{5 \times 3 \times RT}{2}$$

$$= 15RT$$

19. (b) Assuming constant voltage supply

$$P = 60 = \frac{V^2}{R_1 + R_2}$$

$$\text{And } P' = \frac{V^2}{R_1} + \frac{V^2}{R_2} = \frac{2V^2}{R_1} = 4P = 4 \times 60$$

$$= 240 \text{ W}$$

20. (b)

$$0.5 = \frac{6}{(2 + \lambda L)} \lambda x$$

$$E_2 = \frac{6}{(6 + \lambda L)} \lambda x$$

So dividing equation (1) and (2)

$$\frac{E_2}{0.5} = \frac{2 + 4}{6 + 4} = \frac{3}{5}$$

$$\Rightarrow E_2 = 0.3 \text{ volt.}$$

21. (d) $\frac{E_i}{B_i} = C$

$$\frac{E_f}{B_f} = \frac{c}{n}$$

$$\Rightarrow \frac{E_i B_f}{E_f B_i} = \frac{1}{n}$$

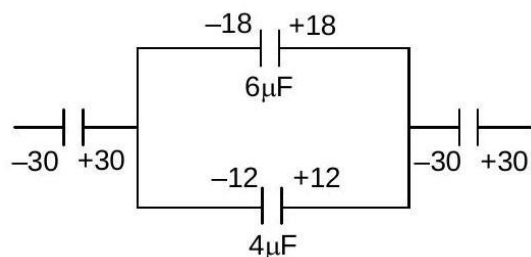
$$\Rightarrow \frac{E_i}{E_f} = \frac{1}{n} \frac{B_i}{B_f}$$

$$\left(\because n = \frac{1}{\sqrt{\mu_0 \epsilon_r}} \right)$$

$$\frac{1}{\sqrt{n}} : \sqrt{n}$$

22. (d) $4V + 6V = 30$

$$\Rightarrow V = 3$$



23. (b) Equation of adiabatic process

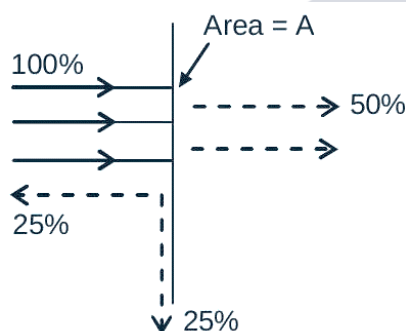
$$TV^{2/f} = \text{constant}$$

$$\therefore \frac{2}{f} = \frac{2}{5} = x$$

24. (b)

$$F = \frac{1}{4} \times \rho A v^2 + \frac{1}{4} 2 \rho a v^2$$

$$\Rightarrow \frac{F}{A} = \frac{3}{4} \rho A v^2 = \rho$$



25. (d) $\lambda_e = \lambda_{\text{photon}} \times 10^{-3}$

$$\Rightarrow \frac{h}{mv} = \frac{c}{v} \times 10^{-3} \text{ s}$$

$$\Rightarrow v = \frac{hv}{mC \times 10^{-3}}$$

$$= \frac{6.62 \times 10^{-34} \times 6 \times 10^{14}}{9.1 \times 10^{-31} \times 3 \times 10^8 \times 10^{-3}}$$

$$= 1.45 \times 10^6$$

26. (b) The potential inside a uniformly charged shell is constant, while it decrease hyperbolically outside.

27. (c) $y = 0.03 \sin \left[450 \left(t - \frac{9x}{450} \right) \right]$

So, $v = \frac{450}{9} = 50 \text{ m/s}$

Also, $v = \sqrt{\frac{T}{\lambda}}$

$$\Rightarrow 50 = \sqrt{\frac{T}{5 \times 10^{-3}}}$$

$$\Rightarrow T = 2500 \times 5 \times 10^{-3} = 12.5 \text{ N}$$

$$28. (d) k_e = \frac{p^2}{2M_e} = 500e$$

$$\& R = \frac{p}{\hbar k} = \frac{1000 \text{ m}_e e}{\hbar k} = \frac{1010 \times 9.1 \times 10^{-31}}{1.6 \times 10^{-19}}$$

$$= 100 \times 7.541 \times 10^{-6}$$

$$29. (b) v = \sqrt{2 \times 10 \times 100}$$

$$= 20\sqrt{5}$$

$$\text{COLM} \rightarrow v_p = \frac{1 \times 20\sqrt{5}}{4}$$

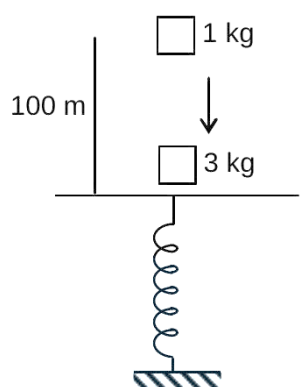
$$= 5\sqrt{5}$$

$$\frac{1}{2} \times 4 \times (5\sqrt{5})^2 + \frac{1}{2} \cdot 1.25 \times 10^6 \left(\frac{30}{k}\right)^2$$

$$= -4 \times 10 \times \left(n - \frac{30}{k}\right) + \frac{1}{2} k n^2$$

$$\Rightarrow 250 + \frac{900}{2 \times 1.25 \times 10^6} = -40x + \frac{1200}{k} + \frac{1}{2} k x^2$$

$$\Rightarrow x \simeq 2 \text{ cm}$$



30. (d)

$$\frac{P}{Q} = \frac{400}{S}$$

$$\text{and } \frac{Q}{P} = \frac{405}{5}$$

$$\text{Solving } S^2 = 400 \times 405$$

$$\Rightarrow S = 402.5\Omega$$

31. (b)

32. (b)

33. (a) $b \rightarrow$ antiaromatic

d → Non aromatic (no cyclic conjugation)

$$34. (c) \text{ Density} = \frac{Z \times M}{N_{AV} \times a^3}$$

$$\text{Here } Z = 4, a = 200\sqrt{2}$$

$$N_{AV} = 6.02 \times 10^{23}, d = 9 \times 10^3 \frac{\text{Kg}}{\text{m}^3}$$

35. (a)

36. (b)

37. (c)

38. (c) NaH is an example of saline hydride.

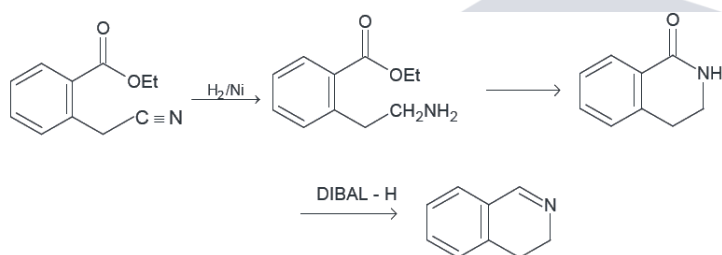
39. (c) Sc^{3+} has noble gas configuration hence only +3 exists.

40. (b) An example of solid sol is gem stones.

41. (c) In cold water, dissolved oxygen can reach a concentration upto 10ppm

42. (d)

43. (d)



$$44. (b) 0.5\alpha \frac{1}{2}, 0.2\alpha \frac{1}{x}$$

$$\text{Here } \frac{0.5}{0.2} = \frac{x}{2}; x = 5, \text{ hence 3 cup}$$

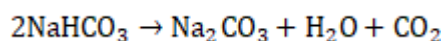
$$45. (d) \ln K = -\frac{E_a}{RT} + \ln A$$

$$\therefore \text{Slope} = -E_a = -y$$

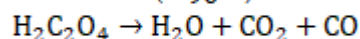
46. (c) Let $\text{NaHCO}_3 = x \text{ gm}$

Then, $\text{H}_2\text{C}_2\text{O}_4 = (10 - x) \text{ gm}$

$$\therefore n_{\text{NaHCO}_3} = \frac{x}{84}$$



$$n_{\text{H}_2\text{C}_2\text{O}_4} = \left(\frac{10 - x}{90} \right)$$



$$\therefore n_{\text{CO}_2} = \left(\frac{10 - x}{90} \right)$$

$$\therefore n_{\text{CO}_2} = \frac{x}{168}$$

$$\text{Total } \text{CO}_2 = \frac{x}{168} + \frac{10-x}{90} = \frac{0.25}{25}$$

On solving 'x'

$$\% = \frac{x}{10} \times 100 = 10x$$

47. (a) Be – O – H

Both bond has same dissociation energy.

48. (d)

49. (a)

50. (c) $\text{CO}_2 = 6$ mole, $\text{N}_1 = 1$ mole

$$C_{\text{atom}} = 6, N_{\text{atom}} = 2$$

Hence $\text{C}_6\text{H}_8\text{N}_2$

51. (a) $\text{N}_2 + 3\text{H}_2 \rightleftharpoons 2\text{NH}_3$

$$\text{equ}^m \times 3x P_1$$

$$P_T = 4xK_p = \frac{P_1^2}{x \times 27 \times 3}$$

$$x = \left(\frac{P}{4}\right)$$

$$P_1 = \sqrt{27x^4 K_p}$$

$$\sqrt{27}(K_p)^{1/2} \left(\frac{P_T}{4}\right)^2 = \frac{3^{3/2} K_p^{1/2} p^2}{16}$$

52. (b)



53. (a) $\Delta S_{\text{Total}} = C_p \ln \frac{(T_1+T_2)}{2 T_1} + C_p \ln \frac{(T_1+T_2)}{2 T_2}$

54. (a) $\text{Co} \rightarrow \text{Vitamin } B_{12}$

Zn $\rightarrow$ Carbonic anhydrase

Rh $\rightarrow$ Wilkinson catalyst

Mg $\rightarrow$ Chlorophyll

55. (d) $\Delta G^\circ = \left(120 - \frac{3}{8} T\right) = 0$

Then $T = 320 \text{ K}$

Hence $T > 320 \text{ K}$ formed

$T < 320 \text{ K}$ X formed

56. (b)

Siderite $\rightarrow$ Iron

Kaolinite $\rightarrow$ Aluminium

Malachite $\rightarrow$ Copper

Calamine $\rightarrow$ Zinc

57. (a) [i] $900 \text{ nm} = 9000 \text{ \AA}$

It is in far infra-red region hence paschen.

58. (b)

59. (a)

60. (c)

61. (b) $2x + 2y + 3z = a$

$3x - y + 5z = b$

$x - 3y + 2z = c$

$(2x + 2y + 3z) + (x - 3y + 2z) - (3x - y + 5z) = 0$

$\Rightarrow a + c - b = 0$

62. (a) $F_4(x) = \frac{\sin^4 x + \cos^4 x}{4} = \frac{1 - 2\sin^2 x \cdot \cos^2 x}{4} = \frac{1}{4} - \frac{1}{2} \sin^2 x \cdot \cos^2 x$

$F_6(x) = \frac{\sin^6 x + \cos^6 x}{6} = \frac{1 - 3\sin^2 x \cdot \cos^2 x (\sin^2 x + \cos^2 x)}{6}$

$= \frac{1}{6} - \frac{1}{2} \sin^2 x \cdot \cos^2 x$

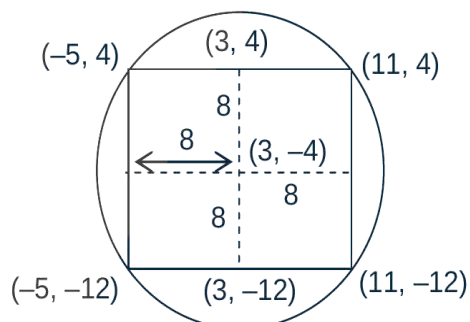
$F_4(x) - F_6(x) = \frac{1}{4} - \frac{1}{6} = \frac{6 - 4}{24} = \frac{2}{24} = \frac{1}{12}$

63. (c) Centre $(3, -4)$

Radius $= \sqrt{9 + 16 + 103} = \sqrt{128} = 8\sqrt{2}$

$\therefore (-5, 4)$ will be nearer to the $(0, 0)$

$\therefore \text{Ans. } \sqrt{5^2 + 4^2} = \sqrt{25 + 16} = \sqrt{41}$



64. (b)

65. (b) $x^2 = 4y$

$x + 2 = 4y$

Solve (1) and (2)

$x + 2 = x^2$

$\Rightarrow x^2 - x - 2 = 0$

$\Rightarrow (x - 2)(x + 1) = 0 \Rightarrow x = 2, -1$

$$\begin{aligned} \text{Area} &= \int_{-1}^2 \left(\frac{x+2}{4} - \frac{x^2}{4} \right) dx \\ &= \frac{1}{4} \left[\frac{x^2}{2} + 2x - \frac{x^3}{3} \right]_{-1}^2 \\ &= \frac{1}{4} \left[\left(2 + 4 - \frac{8}{3} \right) - \left(\frac{1}{2} - 2 + \frac{1}{3} \right) \right] \\ &= \frac{1}{4} \left[\frac{10}{3} - \frac{3 - 12 + 2}{6} \right] = \frac{1}{4} \left[\frac{10}{3} + \frac{7}{6} \right] \\ &= \frac{1}{4} \times \frac{27}{6} = \frac{9}{8} \end{aligned}$$

66. (a) $\int_0^2 \left(\frac{\sin^2 x}{\frac{1}{2} + \left[\frac{x}{\pi} \right]} + \frac{\sin^2 x}{\frac{1}{2} + \left[-\frac{x}{\pi} \right]} \right) dx$

$$= \int_0^2 \left(\frac{\sin^2 x}{1 + \left[\frac{x}{\pi} \right]} + \frac{\sin^2 x}{\frac{1}{2} - 1 - \left[\frac{x}{\pi} \right]} \right) dx = \int_0^2 dx = 0$$

67. (d) Variance remains same if same number is subtracted from each observation. (subtract 10 from each observation)

$$\therefore \frac{10(-d)^2 + 10(0)^2 + 10(d)^2}{30} - \left(\frac{10(-d) + 10(0) + 10(d)}{30} \right)^2 = \frac{4}{3}$$

$$\frac{20d^2}{30} = \frac{4}{3}$$

$\Rightarrow d^2 = 2$

68. (d) Equation of required plane is

$a(x - 3) + b(y + 2) + c(z - 1) = 0$

[as it contains the point (3, -2, 1)]

$2a - b + 3c = 0$

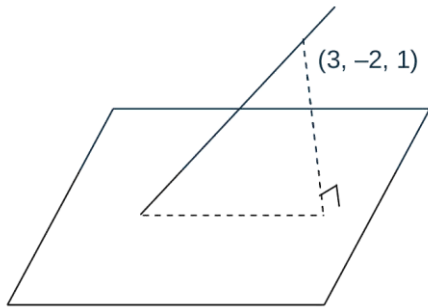
$2a + 3b - c = 0$

$\Rightarrow \frac{a}{-8} = \frac{b}{8} = \frac{c}{8}$

$\Rightarrow \frac{a}{+1} = \frac{b}{-1} = \frac{c}{1}$

∴ equation of plane is

$$x - 3 - y - 2 - z + 1 = 0$$



$$\Rightarrow x - y - z = 4$$

69. (c)

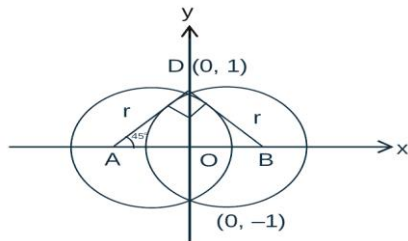
$$P = \frac{\text{both number is even}}{\text{number of ways selecting two numbers such that their sum is even.}}$$

$$= \frac{{}^5C_2}{{}^5C_2 + {}^6C_2} = \frac{10}{10 + 15} = \frac{10}{25} = \frac{2}{5}$$

70. (b) The two circle will be orthogonal $OD = 1$

$$\therefore OA = OB = OD = 1$$

$$\Rightarrow AB = 2$$



71. (b)

$${}^{20}C_r \cdot {}^{20}C_0 + {}^{20}C_{r-1} \cdot {}^{20}C_1 + \dots + {}^{20}C_0 \cdot {}^{20}C_r =$$

Selecting r student from 20 boys and 20 girls = ${}^{40}C_r$

${}^{40}C_r$ will be maximum if $r = 20$.

72. (c)

Equation of tangent is

$$\frac{x}{a} \cos \theta + \frac{y}{b} \sin \theta = 1$$

$$A \text{ is } \left(\frac{a}{\cos \theta}, 0 \right)$$

$$B \text{ is } \left(0, \frac{b}{\sin \theta} \right)$$

Let $P(h, k)$ is mid point

$$2h = \frac{a}{\cos \theta}$$

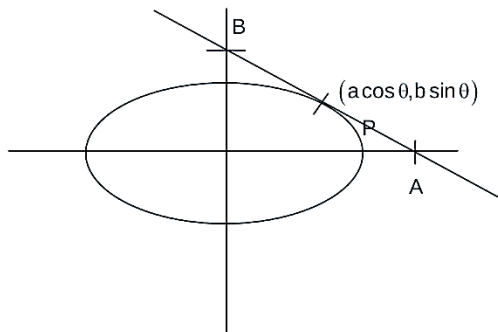
$$2k = \frac{b}{\sin \theta}$$

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$\Rightarrow \frac{a^2}{4h^2} + \frac{b^2}{4k^2} = 1$$

$$\Rightarrow \frac{2}{4x^2} + \frac{1}{4y^2} = 1$$

$$\Rightarrow \frac{1}{2x^2} + \frac{1}{4y^2} = 1$$



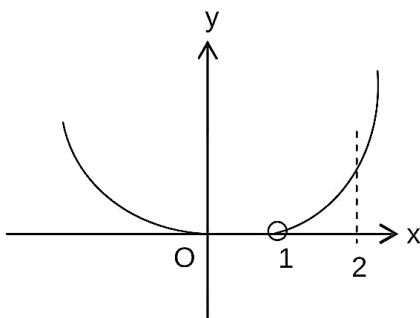
73. (d) $|f(x)| = \begin{cases} 1 & -2 \leq x < 0 \\ |x^2 - 1| & 0 \leq x \leq 2 \end{cases}$

$$f(|x|) = \begin{cases} -1 & -2 \leq |x| < 0 \\ x^2 - 1 & 0 \leq |x| \leq 2 \end{cases}$$

$$\Rightarrow f(|x|) = \{x^2 - 1 \mid -2 \leq x \leq 2\}$$

$$g(x) = |f(x)| + f(|x|) = \begin{cases} 1 + x^2 - 1 & -2 \leq x < 0 \\ |x^2 - 1| + x^2 - 1 & 0 \leq x \leq 2 \end{cases}$$

$$g(x) = \begin{cases} x^2 & -2 < x < 0 \\ 0 & 0 \leq x < 1 \\ 2(x^2 - 1) & 1 \leq x < 2 \end{cases}$$



$\therefore g(x)$ is not differentiable at $x = 1$

74. (b) $x \cdot \frac{1}{\ln x} \cdot \frac{1}{x} + \log_e(\log_e x) - 2x + 2y \cdot \frac{dy}{dx} = 0$

Put $x = e$

$$1 - 2e + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{2e - 1}{2y}$$

Put $x = e$ in original equation

$$0 - e^2 + y^2 = 4$$

$$y^2 = 4 + e^2$$

Now put in (i)

$$\frac{dy}{dx} = \frac{2e - 1}{2\sqrt{4 + e^2}}$$

75. (a)

76. (a)

$$\lim_{x \rightarrow 0} \frac{\tan(\pi \sin^2 x)}{\pi \sin^2 x} \cdot \frac{\pi \sin^2 x}{x^2} + \left(\frac{|x| - \sin(x[x])}{|x|} \right)^2$$

$$1(\pi) \cdot (1)^2 + \lim_{x \rightarrow 0} \left(1 - \frac{\sin x[x]}{x[x]} \cdot \frac{x[x]^2}{|x|} \right)$$

$$\lim_{x \rightarrow 0^-} \frac{x[x]}{|x|} = \frac{x}{-x} (-1) = 1$$

$$\lim_{x \rightarrow 0^+} \frac{x[x]}{[x]} = \frac{x(0)}{x} = 0$$

Put in equation (i)

∴ Limit does not exist.

77. (c)

$$x^2 - 11x + 30 \leq 0$$



$$(x - 6)(x - 5) \leq 0$$

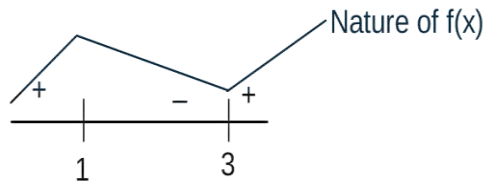
$$f(x) = 3x^3 - 18x^2 + 27x - 40$$

$$5 \leq x \leq 6$$

$$f'(x) = 9x^2 - 36x + 27$$

$$= 9(x^2 - 4x + 3) = 9(x - 3)(x - 1)$$

∴ $f(x)$ will be maximum when $x = 6$



$$f(6) = 3(6)^3 - 18(6)^2 + 27(6) - 40$$

$$= 36(18 - 18) + 162 - 40 = 122$$

78. (a) $y = \frac{x}{x^2+1}$

$$yx^2 - x + y = 0$$

$$D \geq 0$$

$$\Rightarrow 1 - 4y^2 \geq 0$$

$$\Rightarrow y^2 \leq \frac{1}{4}$$

$$y \in \left[-\frac{1}{2}, \frac{1}{2}\right]$$

79. (b) $\frac{a}{1-r} = 3$

Cube both sides

$$\frac{a^3}{(1-r)^3} = 27$$

and $\frac{a^3}{1-r^3} = \frac{27}{19}$

$$(1) / (2) \text{ gives } \frac{1-r^3}{(1-r)^3} = 19$$

$$r = \frac{2}{3}$$

80. (a)

Equation of circle $x(x-1) + \left(y-\frac{1}{2}\right)y = 0$

$$x^2 + y^2 - x - \frac{y}{2} = 0$$

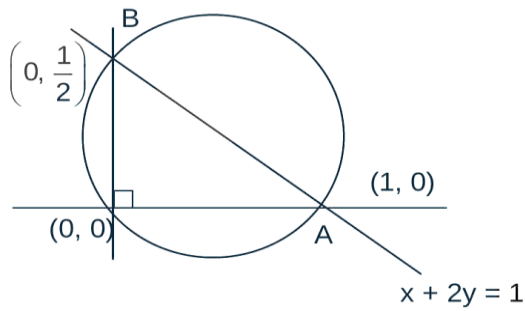
Equation of tangent at (0,0)

$$x \cdot 0 + y \cdot 0 - \frac{x+0}{2} - \frac{y+0}{2 \times 2} = 0$$

$$2x + y = 0$$

Sum of distance of A and B from Line (i) is

$$\frac{2}{\sqrt{5}} + \frac{\frac{1}{2}}{\sqrt{5}} = \frac{5}{2\sqrt{5}} = \frac{\sqrt{5}}{2}$$



81. (b)

$$x^2 - c^2 = y$$

$$(a + b)^2 - c^2 = ab$$

$$a^2 + b^2 - c^2 = -ab$$

$$\frac{a^2 + b^2 - c^2}{2ab} = -\frac{1}{2}$$

$$\cos c = -\frac{1}{2}$$

$$c = \frac{2\pi}{3}$$

$$\sin C = \frac{\sqrt{3}}{2}$$

$$\frac{c}{\sin c} = 2R \Rightarrow R = \frac{c}{2\sin c} = \frac{c}{\sqrt{3}}$$

82. (c) Equation of tangent to parabola $y^2 = 4x$ is $y = mx + \frac{1}{m}$

Now solve it with $xy = 2$

$$\left(mx + \frac{1}{m}\right)x = 2$$

$$\Rightarrow mx^2 + \frac{1}{m}x - 2 = 0$$

For common tangent $D = 0$

$$\Rightarrow \frac{1}{m^2} + 8m = 0$$

$$m = -\frac{1}{2}$$

Put it in equation (i) $y = -\frac{1}{2}x - 2$

$$\Rightarrow 2x + y + 4 = 0$$

83. (a) 5th term will be the middle term.

$$t_{4+1} = {}^8C_4 \left(\frac{x^3}{3}\right)^4 \left(\frac{3}{x}\right)^4 = 5670$$

$$= {}^8C_4 \cdot x^8 = 5670$$

$$= \frac{8 \times 7 \times 6 \times 5}{4 \times 3 \times 2} x^8 = 5670$$

$$= x^8 = \frac{567}{7} = 81$$

$$= x^8 - 81 = 0$$

$$\Rightarrow \text{Real value of } x = \pm\sqrt[3]{3}$$

$$84. (a) \frac{a_3}{a_1} = \frac{a_1 r^2}{a_1} = r^2$$

$$\Rightarrow r^2 = 25$$

$$\text{Now } \frac{a_9}{a_5} = \frac{a_1 r^8}{a_1 r^4} = r^4 = (25)^2 = 5^4$$

$$85. (c) A \text{ is orthogonal matrix}$$

$$\therefore 4q^2 + r^2 = p^2 + q^2 + r^2 = 1$$

$$p^2 - q^2 - r^2 = 0$$

$$\text{and } 2q^2 - r^2 = 0$$

Solving (1), (2) and (3)

$$p^2 = \frac{1}{2}$$

$$|p| = \frac{1}{\sqrt{2}}$$

$$86. (b) \text{ I.F.} = e^{\int (2 + \frac{1}{x}) dx} = e^{2x} \cdot x$$

$$\text{Solution will be } y(xe^{2x}) = \int e^{-2x} \cdot xe^{2x} \cdot dx + c$$

$$xye^{2x} = \frac{x^2}{2} + c$$

$$1 \left(\frac{1}{2} e^{-2} \right) \cdot e^2 = \frac{1}{2} + c \quad (\text{Put } x = 1 \text{ and } y = \frac{1}{2} e^{-2})$$

$$c = 0$$

$$\therefore y = \frac{x}{2} e^{-2x}$$

$$\frac{dy}{dx} = \frac{-2xe^{-2x} + e^{-2x}}{2} = \frac{e^{-2x}}{2} (1 - 2x)$$

$$\frac{dy}{dx} = 0 \Rightarrow x = \frac{1}{2}$$

$$\frac{dy}{dx} < 0 \text{ if } x \in \left(\frac{1}{2}, 1 \right)$$

87. (b, c)

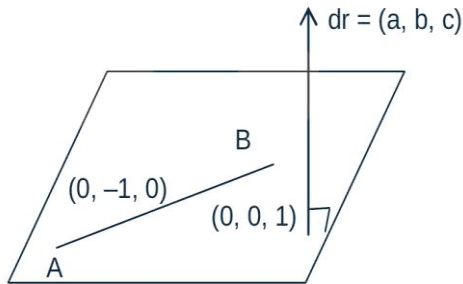
d. r. of AB

$$= (0, 1, 1)$$

$$a \cdot 0 + b \cdot 1 + c \cdot 1 = 0$$

$$b + c = 0$$

$$b + c = 0$$



$$\cos \frac{\pi}{4} = \frac{a \cdot 0 + b(1) + c(-1)}{\sqrt{a^2 + b^2 + c^2} \cdot \sqrt{2}}$$

$$\frac{1}{\sqrt{2}} = \frac{b - c}{\sqrt{a^2 + b^2 + c^2}} \cdot \sqrt{2}$$

$$= b^2 + c^2 - 2bc$$

$$\Rightarrow a^2 = -2bc$$

$$\Rightarrow a^2 = -2b(-b)$$

$$a^2 = 2b^2 \Rightarrow a = \pm \sqrt{2}b$$

$$\frac{a}{\sqrt{2}} = \frac{b}{1}$$

$$\text{From (i)} \frac{a}{\sqrt{2}} = \frac{b}{1} = \frac{c}{-1}$$

$$\text{OR } \frac{a}{-\sqrt{2}} = \frac{b}{1}$$

$$\Rightarrow \frac{a}{-\sqrt{2}} = \frac{b}{1} = \frac{c}{-1} \text{ from (i)}$$

$$\frac{a}{\sqrt{2}} = \frac{b}{-1} = \frac{c}{1}$$

dr. will be $(\sqrt{2}, 1, -1)$ or $(\sqrt{2}, -1, 1)$

88. (d)

$$[\vec{a} \quad \vec{b} \quad \vec{c}] = 0$$

$$\begin{vmatrix} 1 & 2 & 4 \\ 1 & \lambda & 4 \\ 2 & 4 & \lambda^2 - 1 \end{vmatrix}_{R_3 \rightarrow R_3 - 2R_1} = 0$$

$$\begin{vmatrix} 1 & 2 & 4 \\ 1 & \lambda & 4 \\ 0 & 0 & \lambda^2 - 9 \end{vmatrix} = 0$$

$$(\lambda^2 - 9)(\lambda - 2) = 0$$

$$\Rightarrow \lambda = 2 \text{ OR } \lambda^2 = 9$$

$$\vec{a} \times \vec{c} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 4 \\ 2 & 4 & \lambda^2 - 1 \end{vmatrix}$$

$$= \hat{i}(2\lambda^2 - 2 - 16) - \hat{j}(\lambda^2 - 1 - 8)$$

$$= (\lambda^2 - 9)(2\hat{i} - \hat{j}) = -5(2\hat{i} - \hat{j}) \text{ (put } \lambda = 2)$$

89. (d) $\alpha + \alpha^3 = -\frac{K}{81}$

$$\alpha^4 = \frac{256}{81}$$

$$\alpha = \pm \frac{4}{3}$$

From (1) and (2)

$$\frac{4}{3} + \frac{64}{27} = \frac{-K}{81}$$

$$K = -300$$

90. (a)

$$\left(-2 - \frac{i}{3}\right)^3 = \left(\frac{x + iy}{27}\right)$$

$$(-1)^3 \left(2^3 + \frac{i^3}{27} + 3(2)\frac{i^2}{9} + 3(2)^2 \cdot \frac{i}{3}\right) = \frac{x - iy}{27}$$

$$-\left[8 - \frac{i}{27} - \frac{2}{3} + 4i\right] = \frac{x + iy}{27}$$

$$\Rightarrow \frac{x}{27} = -8 + \frac{2}{3}$$

and $\frac{y}{27} = \frac{1}{27} - 4$

$$\frac{y - x}{27} = \frac{1}{27} - 4 + 8 - \frac{2}{3}$$

$$= \frac{1 + 27 \times 4 - 18}{27}$$

$$= \frac{109 - 18}{27}$$

$$= \frac{91}{27}$$

$$\Rightarrow y - x = 91$$

