

1. (c)

$$R = R_0 e^{-\lambda t}$$

$$\therefore \frac{R_B}{R_A} = \frac{R_0 e^{-\lambda_B t}}{R_0 e^{-\lambda_A t}} = e^{-(\lambda_B - \lambda_A)t} = e^{-3t}$$

$$\Rightarrow \lambda_B - \lambda_A = 3$$

$$\Rightarrow \frac{\ell n^2}{T_B} - \frac{\ell n 2}{\ell n 2} = 3.$$

$$\Rightarrow T_B = \frac{\ell n 2}{4}$$

2. (b)  $P_s = \eta P_p$

$$\Rightarrow E_s i_s = \eta E_i i_p$$

$$\Rightarrow i_s = \frac{(0.9)(2300)(5)}{(230)} = 45 \text{ A.}$$

3. (d)  $B = \frac{E}{c}$

$$\Rightarrow U_E = \frac{1}{2} \epsilon_0 E^2$$

$$U_B = \frac{B^2}{2\mu_0} = \frac{E^2}{2\mu_0 C^2} = \frac{E^2}{2\mu_0} (\mu_0 \epsilon_0) = U_E$$

4. (d)

$$x = 3t^2 + 5$$

$$\Rightarrow v = 6t$$

$$\Rightarrow \Delta W = \Delta k$$

$$= \frac{1}{2} (2)(30)^2 - \frac{1}{2} 2(0)^2$$

$$= 900 \text{ J}$$

5. (d)

$$eE = evB$$

$$\Rightarrow E = \left( \frac{eBr}{m} \right) B$$

$$\Rightarrow m = \frac{eB^2 r}{E}$$

$$\Rightarrow m = \frac{(1.6 \times 10^{-19})(0.5)^2(0.5 \times 10^{-2})}{100} = 2 \times 10^{-24} \text{ kg}$$

6. (a)

$$\vec{E} = \frac{kq_1}{r_1^3} \vec{r}_1 + \frac{kq_2}{r_2^3} \vec{r}_2 = k \times 10^{-6} \left[ \frac{\sqrt{10}}{10\sqrt{10}} (-\hat{i} + 3\hat{j}) + \frac{(-25)}{125} (-4\hat{i} + 3\hat{j}) \right]$$

$$= (9 \times 10^3) \left[ \frac{1}{10} (-\hat{i} + 3\hat{j}) - \frac{1}{5} (-4\hat{i} + 3\hat{j}) \right]$$

$$= (9 \times 10^3) \left[ \left( -\frac{1}{10} + \frac{4}{5} \right) \hat{i} + \left( \frac{3}{10} - \frac{3}{5} \right) \hat{j} \right] = 9000 \left( \frac{7}{10} \hat{i} - \frac{3}{10} \hat{j} \right)$$

$$= (63\hat{i} - 27\hat{j})(100)$$

7. (c)  $t = G^a h^b C^c$

$$\Rightarrow M^0 L^0 T^1 = (M^{-1} L^3 T^{-2})^a (M^2 T^{-1})^b (L^{-1})^c$$

$$\Rightarrow -a + b = 0 \Rightarrow a = b$$

$$\Rightarrow 3a + 2b + c = 0$$

$$\Rightarrow c = -5a$$

$$\Rightarrow -2a - b - c = 1$$

$$\Rightarrow a = \frac{1}{2}; b = \frac{1}{2}; c = -\frac{5}{2}$$

8. (d)

9. (b)  $\frac{dV}{dt} = Av \Rightarrow \frac{dV}{dt} = A\sqrt{2gh}$

$$\Rightarrow \frac{0.74}{60} = (3.14) \left( \frac{2}{100} \right)^2 \sqrt{2(9.8)h}$$

$$\Rightarrow h = 4.92 \text{ m}$$

10. (b)  $E_1 = -\frac{GMm}{R+h} - \left( -\frac{GMm}{R} \right)$

$$E_2 = \frac{1}{2} m \left( \sqrt{\frac{GM}{R+h}} \right)^2 = \frac{GMm}{2(R+h)}$$

$$E_1 = E_2; h = \frac{R}{2}$$

11. (d)  $W_1 = W_2$

$$\Rightarrow 600 - T_2 = T_2 - 400$$

$$\Rightarrow T_2 = 500 \text{ K}$$

12. (c)  $E = Pt = \frac{E^2}{Z^2} Rt = \frac{(24)^2}{60^2 + (8.33\pi - 2\pi)^2} (60)(60) = 518 \text{ J}$

13. (c) PE = KE

$$\Rightarrow \frac{1}{2} m \omega^2 (A^2 - x^2) = \frac{1}{2} m \omega^2 x^2$$

$$\Rightarrow x = \frac{A}{\sqrt{2}}$$

14. (d)  $T \cos 45^\circ = mg$

$$T \sin 45^\circ = F$$

$$\Rightarrow F = mg = 100 \text{ N.}$$

15. (c)  $\Delta Q = \frac{f}{2} n R \Delta T$

$$= \frac{5}{2} \left( \frac{15}{28} \right) (8.3) (1200 - 300) = 10000 \text{ J.}$$

16. (d)

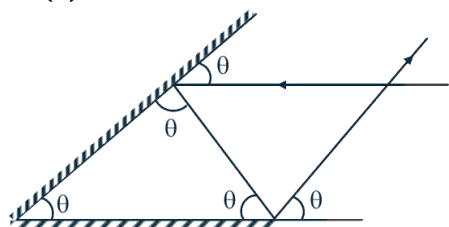
$$\Delta X_{\max} = d \sin \theta = 0.32 \sin 30 = 0.16 \text{ mm}$$

$$\therefore n = \frac{\Delta X_{\max}}{\lambda} = \frac{0.16 \times 10^{-3}}{500 \times 10^{-9}}$$

$$= \frac{0.16 \times 10^6}{500} = \frac{1600}{5} = 320$$

$$\therefore \text{Number of BFs} = (2n + 1) = 641$$

17. (b)



$$\theta = 60^\circ$$

18. (b)  $mg \frac{\ell}{2} \left( \frac{1}{2} \right) = \frac{1}{2} \left( \frac{m\ell^2}{3} \right) \omega^2$

$$\Rightarrow \omega = \sqrt{\frac{3g}{2\ell}} = \sqrt{30}$$

19. (a)  $R = 530 \text{ k}\Omega \pm 5\%$

20. (d)  $B_L = \frac{\mu_0 i}{2R}$

$$B_C = \frac{\mu_0 N i}{2(R/N)}$$

$$\therefore \frac{B_L}{B_C} = \frac{1}{N^2}$$

21. (c)

$$f = \frac{1}{2\pi} \sqrt{\frac{C}{\left( \frac{ML^2}{3} \right)}} \& 0.8f = \frac{1}{2\pi} \sqrt{\frac{C}{\left( \frac{ML^2}{3} + \frac{mL^2}{2} \right)}}$$

$$\Rightarrow \frac{25}{16} = \frac{\frac{ML^2}{3} + \frac{mL^2}{2}}{\frac{ML^2}{3}}$$

$$\Rightarrow \frac{25}{16} = 1 + \frac{3m}{2M}$$

$$\Rightarrow \frac{9}{16} = \frac{3m}{2M}$$

$$\Rightarrow \frac{m}{M} = \frac{3}{8} = 0.37$$

22. (b)

23. (BONUS)

24. (c) Zero error =  $0 + 3 \times \frac{0.5 \text{ mm}}{100} = 0.015 \text{ mm}$

$$MSR = 5.5 + 48 \times \frac{0.5}{100}$$

$$= 5.74 \text{ mm.}$$

$$\therefore \text{Thickness} = 5.74 - 0.015 = 5.725 \text{ mm}$$

25. (a)  $f = \frac{2}{2\ell} v_s = \frac{330}{0.5} = 660 \text{ Hz}$

$$\therefore f' = f \left( \frac{v_s + v}{v_s} \right) = (660) \left( \frac{330 + \frac{50}{18}}{330} \right) = 660 \left( 1 + \frac{50}{18 \times 330} \right)$$

$$= 666 \text{ Hz}$$

26. (c)  $\sqrt{\frac{2\ell}{a_2}} - \sqrt{\frac{2\ell}{a_1}} = t \Rightarrow \frac{\sqrt{2\ell}}{t} = \frac{\sqrt{a_1 a_2}}{\sqrt{a_1} - \sqrt{a_2}}$

$$\sqrt{2a_1\ell} - \sqrt{2a_2\ell} = v \Rightarrow \frac{\sqrt{2\ell}}{v} = \frac{1}{\sqrt{a_1} - \sqrt{a_2}}$$

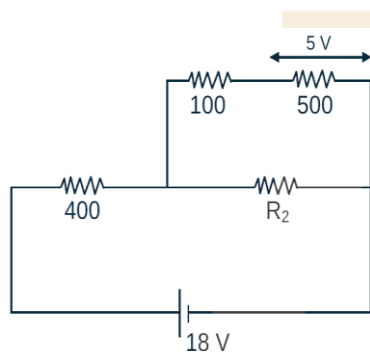
$$\Rightarrow \frac{v}{t} = \sqrt{a_1 a_2} \Rightarrow v = (\sqrt{a_1 a_2}) t$$

27. (d)  $KE_{\max} = h\nu_{\max} - \phi$

$$= \frac{(6.6 \times 10^{-34})(6.28 \times 10^7)(3 \times 10^8)}{1.6 \times 10^{-19} \times 2 \times 3.14} - 4.7$$

$$= 12.37 - 4.7 = 7.67 \text{ eV}$$

28. (a)



$$\frac{12}{400} = \frac{6}{600} + \frac{6}{R_2}$$

$$\Rightarrow \frac{1}{200} = \frac{1}{600} + \frac{1}{R_2}$$

$$\Rightarrow R_2 = 300\Omega$$

$$29. (c) f = \frac{c}{\lambda} = \frac{3 \times 10^8}{8 \times 10^{-7}} = \frac{3}{8} \times 10^{15} \text{ Hz}$$

$$\therefore n = \frac{(0.01)f}{6 \times 10^6} = \frac{\frac{3}{8} \times 10^{13}}{6 \times 10^6} = \frac{1}{16} \times 10^7 = 6.25 \times 10^5$$

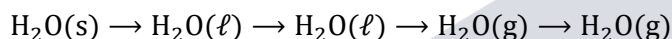
$$30. (a) v_x = \frac{dx}{dt} = -a\omega \sin \omega t$$

$$v_y = \frac{dy}{dt} = a\omega \cos \omega t$$

$$v_z = \frac{dz}{dt} = a\omega$$

$$\therefore v = \sqrt{v_x^2 + v_y^2 + v_z^2} = a\omega\sqrt{2}$$

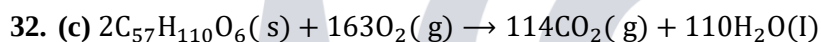
31. (d)



|          |          |                   |
|----------|----------|-------------------|
| 1 kg     | 1 kg     | 1 kg              |
| at 273 K | at 273 K | at 373 K at 373 K |

$$\Delta S = \Delta S_1 + \Delta S_2 + \Delta S_3 + \Delta S_4$$

$$= \frac{334}{273} + 4.2 \ln \frac{373}{273} + \frac{2491}{373} + 2 \ln \frac{383}{373} = 9.267 \text{ kJ Kg}^{-1} \text{ K}^{-1}$$

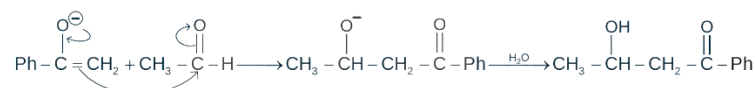
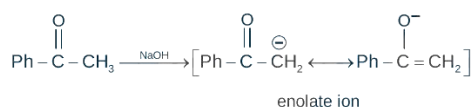


$$\frac{\text{Moles of C}_{57}\text{H}_{110}\text{O}_6}{2} = \frac{\text{Moles of H}_2\text{O}}{110}$$

$$\frac{445}{890} = \frac{\text{Mass of H}_2\text{O}}{18} \times \frac{110}{110}$$

$$\text{Mass of H}_2\text{O} = 495 \text{ g}$$

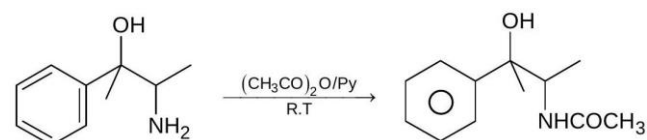
33. (c)



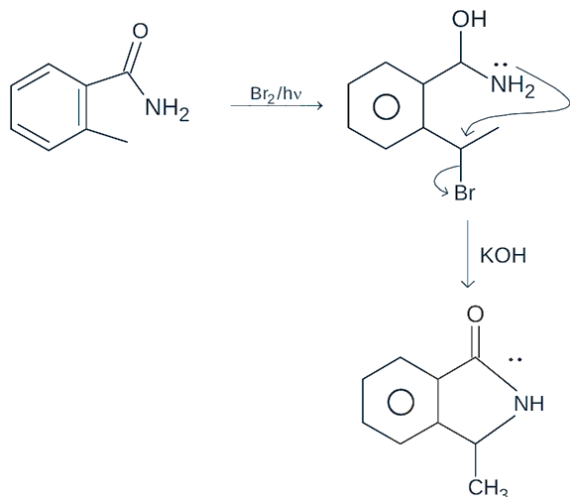
34. (c)

35. (b)

36. (d) Nucleophilicity of  $\text{NH}_2 > \text{OH}$



37. (c)



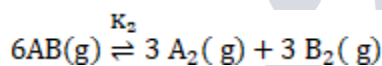
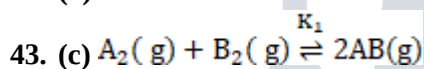
38. (d)

39. (b) The only alkali metal which forms nitride by reacting directly with  $N_2$  is 'Li'.

40. (b)  $As_2S_3$  is a negatively charged sol. so  $AlCl_3$  will be most effective.

41. (d) As  $CN^-$  is a strong field ligand.  $K_3[Co(CN)_6]$  will have maximum ' $\Delta$ '.

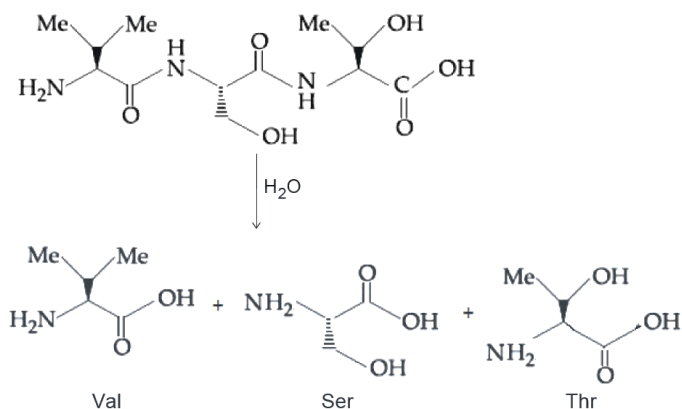
42. (a)



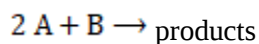
Reaction (2) =  $-3 \times$  reaction (1)

$$\therefore K_2 = \left(\frac{1}{K_1}\right)^3 \Rightarrow K_2 = K_1^{-3}$$

44. (a)



45. (b)



$$\text{Rate} = K[A]^x[B]^y$$

$$r = K[A]^x[B]^y$$

$$0.3 = K[A]^x[B]^y$$

$$2.4 = K[2A]^x[2B]^y$$

$$0.6 = K[2A]^x[B]^y$$

From (1), (2) & (3)

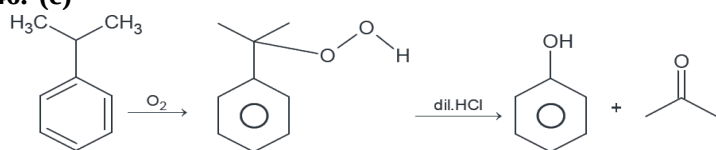
$$x = 1, y = 2$$

$$\text{Overall order} = 2 + 1 = 3$$

$$\text{Order w.r.t A} = 1$$

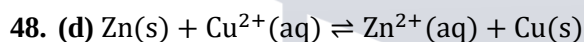
$$\text{Order w.r.t B} = 2$$

46. (c)



47. (b)  $\text{COCH}_3$  is present it will show both 2,4-DNP & iodoform test.

Due to steric inhibition of resonance, I.P of 'N' is not involved in delocalization so coupling reaction will not take place.



$$-nFE_{\text{cell}} = -RT \ln K$$

$$\ln K = \frac{2 \times 96500 \times 2}{8 \times 300} = 160.83$$

$$K = e^{160}$$

49. (c)

50. (a)

|                                           |                                              |
|-------------------------------------------|----------------------------------------------|
| $\text{NO} \longrightarrow \text{NO}^+$   | $\text{N}_2 \longrightarrow \text{N}_2^+$    |
| B.O 0.5      3                            | B.O 3      2.5                               |
| Para      Dia                             | Dia      Para                                |
| $\text{O}_2 \longrightarrow \text{O}_2^+$ | $\text{O}_2 \longrightarrow \text{O}_2^{2-}$ |
| B.O 2      2.5                            | B.O 2      1                                 |
| Para      Para                            | Para      Dia                                |

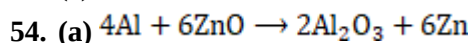
51. (c)

52. (a)



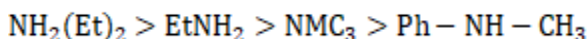
is anti aromatic

53. (c)



$\Delta H$  for the above reaction is -ve.

55. (b) Due to weak metallic bonding  
56. (b) Correct order of basic strength is



57. (d)  $2^{\text{nd}}$  electron gain enthalpy of oxygen is positive.

$$58. (d) d = \frac{ZM}{N_a a^3}$$

$$= \frac{4 \times 63.55}{6.023 \times 10^{23} \times (x \times 10^{-8})^3} = \frac{422}{x^3} \text{ gm/cm}^3$$

59. (c) Let moles of  $\text{H}_2\text{O}$  separated as ice = xgm

$$\Delta T_f = iK_f m$$

$$10 = 1 \times 1.86 \frac{\frac{62}{250 - x}}{\frac{1000}{1000}}$$

$$x = 64 \text{ gm}$$

60. (d)

61. (a)

$$T_n = \frac{(3 + (n-1) \times 3)(1^2 + 2^2 + \dots + n^2)}{(2n+1)}$$

$$T_n = \frac{3 \cdot \frac{n^2(n+1)(2n+1)}{6}}{2n+1} = \frac{n^2(n+1)}{2}$$

$$S_{15} = \frac{1}{2} \sum_{n=1}^{15} (n^3 + n^2) = \frac{1}{2} \left[ \left( \frac{15(15+1)}{2} \right)^2 + \frac{15 \times 16 \times 31}{6} \right]$$

$$= 7820$$

$$62. (a) \lim_{x \rightarrow 0^+} \frac{x([x] + |x|)\sin[x]}{|x|}$$

$$x \rightarrow 0^-$$

$$\left. \begin{array}{l} [x] = -1 \\ |x| = -x \end{array} \right\} \Rightarrow \lim_{x \rightarrow 0^-} \frac{x(-x-1)\sin(-1)}{-x} = -\sin 1$$

$$63. (b) f(xy) = f(x) \cdot f(y)$$

$$f(0) = 1 \text{ as } f(0) \neq 0$$

$$\Rightarrow f(x) = 1$$

$$\frac{dy}{dx} = f(x) = 1$$

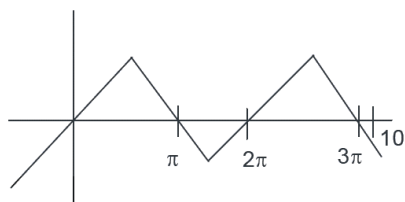
$$\Rightarrow y = x + c$$

$$\text{At, } x = 0, y = 1 \Rightarrow c = 1$$

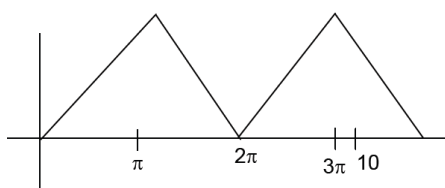
$$y = x + 1$$

$$\Rightarrow y\left(\frac{1}{4}\right) + y\left(\frac{3}{4}\right) = \frac{1}{4} + 1 + \frac{3}{4} + 1 = 3$$

64. (a)



$$x = \sin^{-1}(\sin 10) = 3\pi - 10$$



$$y = \cos^{-1}(\cos 10) = 4\pi - 10$$

$$y - x = \pi$$

65. (a)  $\sin x - \sin 2x + \sin 3x = 0$

$$\Rightarrow (\sin x + \sin 3x) - \sin 2x = 0$$

$$\Rightarrow 2\sin x \cdot \cos x - \sin 2x = 0$$

$$\Rightarrow \sin 2x(2\cos x - 1) = 0$$

$$\Rightarrow \sin 2x = 0 \text{ or } \cos x = \frac{1}{2} \Rightarrow x = 0, \frac{\pi}{3}$$

66. (a)  $z_0 = \omega \text{ or } \omega^2$  (where  $\omega$  is a non-real cube root of unity)

$$z = 3 + 6i(\omega)^{81} - 3i(\omega)^{93}$$

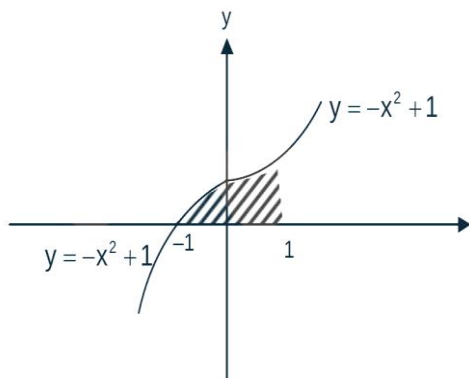
$$z = 3 + 3i$$

$$\Rightarrow \arg z = \frac{\pi}{4}$$

67. (c) The graph is as follows

$$\int_{-1}^0 (-x^2 + 1)dx + \int_0^1 (x^2 + 1)dx = 2$$

68. (b)  $P_1 = x - 4y + 7z - g = 0$



$$P_2 = 3x - 5y - h = 0$$

$$P_3 = -2x + 5y - 9z - k = 0$$

$$\text{Here } \Delta = 0$$

$$2P_1 + P_2 + P_3 = 0 \text{ when } 2g + h + k = 0$$

$$69. (b) (1 - t^6)^3(1 - t)^{-3}$$

$$(1 - t^{18} - 3t^6 + 3t^{12})(1 - t)^{-3}$$

$$\Rightarrow \text{coefficient of } t^4 \text{ in } (1 - t)^{-3} \text{ is } {}^{3+4-1}C_4 = {}^6C_2 = 15$$

70. (BONUS)

71. (d) Let  $A(\alpha, 0)$  and  $B(0, \beta)$  be the vertices of the given triangle  $AOB$

$$\Rightarrow |\alpha\beta| = 100$$

$\Rightarrow$  Number of triangles

$$= 4 \times (\text{number of divisors of } 100)$$

$$= 4 \times 9 = 36$$

$$72. (b) a = A + 6d$$

$$b = A + 10d$$

$$c = A + 12d$$

$a, b, c$  are in G.P.

$$\Rightarrow (A + 10d)^2 = (A + 6d)(A + 12d)$$

$$\Rightarrow \frac{A}{d} = -14$$

$$\frac{a}{c} = \frac{A + 6d}{A + 12d} = \frac{6 + \frac{A}{d}}{12 + \frac{A}{d}} = \frac{6 - 14}{12 - 14} = 4$$

73. (a)

$$[\sim (\sim p \vee q) \wedge (p \wedge r)] \cap (\sim q \wedge r)$$

$$\equiv [(p \wedge \sim q) \vee (p \wedge r)] \wedge (\sim q \wedge r)$$

$$\equiv [p \wedge (\sim q \vee r)] \wedge (\sim q \wedge r)$$

$$\equiv p \wedge (\sim q \wedge r)$$

$$\equiv (p \wedge r) \sim q$$

74. (b) Vector along the normal to the plane containing the lines  $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$  and  $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$  is  $(8\hat{i} - \hat{j} - 10\hat{k})$ .

Vector perpendicular to the vectors  $2\hat{i} + 3\hat{j} + 4\hat{k}$  and  $8\hat{i} - \hat{j} - 10\hat{k}$  is  $26\hat{i} - 52\hat{j} + 26\hat{k}$  So, required plane is  $26x - 52y + 26z = 0 \Rightarrow x - 2y + z = 0$

75. (b)  $\sum (x_i + 1)^2 = 9n$

$$\sum (x_i - 1)^2 = 5n$$

$$(1) + (2) \Rightarrow \sum (x_i^2 + 1) = 7n$$

$$\Rightarrow \frac{\sum x_i^2}{n} = 6$$

$$(1) \cdot (2) \Rightarrow 4\sum x_i = 4n$$

$$\Rightarrow \sum x_i = n$$

$$\Rightarrow \frac{\sum x_i}{n} = 1$$

$$\Rightarrow \text{variance} = 6 - 1 = 5$$

$$\Rightarrow \text{standard deviation} = \sqrt{5}$$

76. (c)

$$|A| = e^{-t} \begin{vmatrix} 1 & \cos t & \sin t \\ 1 & -\cos t - \sin t & -\sin t + \cos t \\ 1 & 2\sin t & -2\cos t \end{vmatrix}$$

$$= e^{-t} [5\cos^2 t + 5\sin^2 t] \forall t \in \mathbb{R}$$

$$= 5e^{-t} \neq 0 \forall t \in \mathbb{R}$$

77. (d)  $\int \frac{5x^8 + 7x^6}{(x^2 + 1 + 2x^7)^2} dx$

$$= \int \frac{5x^{-6} + 7x^{-8}}{\left(\frac{1}{x^7} + \frac{1}{x^5} + 2\right)^2} dx = \frac{1}{2 + \frac{1}{x^5} + \frac{1}{x^7}} + C$$

$$\text{As } f(0) = 0, f(x) = \frac{x^7}{2x^7 + x^2 + 1}$$

$$f(1) = \frac{1}{4}$$

78. (d)  $|f(x) - f(y)| \leq 2|x - y|^{3/2}$

divide both side by  $|x - y|$

$$\left| \frac{f(x) - f(y)}{x - y} \right| \leq 2 \cdot |x - y|^{1/2}$$

Apply limit  $x \rightarrow y$

$$|f'(y)| \leq 0 \Rightarrow f'(y) = 0 \Rightarrow f(y) = c \Rightarrow f(x) = 1$$

$$\int_0^1 1 \cdot dx = 1$$

79. (d)  $\frac{dx}{dt} = 3\sec^2 t$

$$\frac{dy}{dt} = 3\sec t \tan t$$

$$\frac{dy}{dx} = \frac{\tan t}{\sec t} = \sin t$$

$$\frac{d^2y}{dx^2} = \cos t \frac{dt}{dx}$$

$$= \frac{\cos t}{3\sec^2 t} = \frac{\cos^3 t}{3} = \frac{1}{3 \cdot 2\sqrt{2}} = \frac{1}{6\sqrt{2}}$$

80. (b)

81. (b)  $x^2 + y^2 - 16x - 20y + 164 = r^2$

$$A(8,10), R_1 = r$$

$$(x - 4)^2 + (y - 7)^2 = 36$$

$$B(4,7), R_2 = 6$$

$$|R_1 - R_2| < AB < R_1 + R_2$$

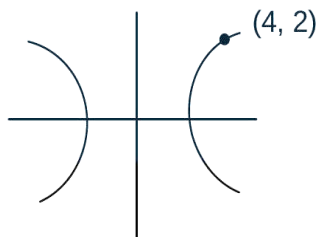
$$\Rightarrow 1 < r < 11$$

82. (a) Given hyperbola is

$$\frac{x^2}{4} - \frac{y^2}{b^2} = 1$$

Satisfying the point (4,2)

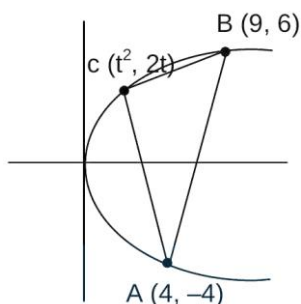
$$\Rightarrow b^2 = \frac{4}{3}$$



$$\Rightarrow e = \frac{2}{\sqrt{3}}$$

83. (d) For maximum area, tangent at the point  $C$  must be parallel to chord  $BC$ .

$$\therefore t = \frac{1}{2}$$



84. (d) Equation of  $AB$  is  $3x - 2y + 6 = 0$

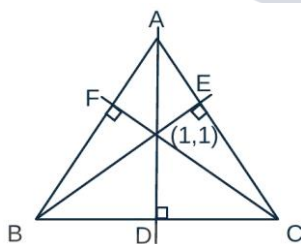
Equation of  $AC$  is  $4x + 5y - 20 = 0$ .

Equation of  $BE$  is  $2x + 3y - 5 = 0$

Equation of  $CF$  is  $5x - 4y - 1 = 0$

$\Rightarrow$  Equation of  $BC$  is

$$26x - 122y = 1675$$



85. (b)  $E_1$  : Event of drawing a Red ball and placing a green ball in the bag

$E_2$  : Event of drawing a green ball and placing a red ball in the bag

$E$  : Event of drawing a red ball in second draw  $P(E) = P(E_1) \times P\left(\frac{E}{E_1}\right) + P(E_2) \times P\left(\frac{E}{E_2}\right) = \frac{5}{7} \times \frac{4}{7} + \frac{2}{7} \times \frac{6}{7} = \frac{32}{49}$

86. (b)

Line  $x = ay + b, z = cy + d$

$$\Rightarrow \frac{x-b}{a} = \frac{y}{1} = \frac{z-d}{c}$$

Line  $x = a'z + b', y = c'z + d'$

$$\Rightarrow \frac{x-b'}{a'} = \frac{y-d'}{c'} = \frac{z}{1}$$

Given both the lines are perpendicular

$$\Rightarrow aa' + c' + c = 0$$

87. (d) Projection of  $\vec{b}$  on  $\vec{a} = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}|} = |\vec{a}|$

$$\Rightarrow b_1 + b_2 = 2$$

$$\text{and } (\vec{a} + \vec{b}) \perp \vec{c} \Rightarrow (\vec{a} + \vec{b}) \cdot \vec{c} = 0$$

$$\Rightarrow 5b_1 + b_2 = -10$$

$$\text{from (1) and (2)} \Rightarrow b_1 = -3 \text{ and } b_2 = 5$$

$$\text{then } |\vec{b}| = \sqrt{b_1^2 + b_2^2 + 2} = 6$$

88. (c)  $D$  must be perfect square

$$\Rightarrow 121 - 24\alpha = \lambda^2$$

$\Rightarrow$  maximum value of  $\alpha$  is 5

$$\alpha = 1 \Rightarrow \lambda \notin I$$

$$\alpha = 2 \Rightarrow \lambda \notin I$$

$$\alpha = 3 \Rightarrow \lambda \in I \Rightarrow 3 \text{ integral values}$$

$$\alpha = 4 \Rightarrow \lambda \in I$$

$$\alpha = 5 \Rightarrow \lambda \in I$$

89. (a)  $f(x) = 2\left(1 + \frac{1}{x-1}\right)$

$$f'(x) = -\frac{2}{(x-1)^2}$$

$\Rightarrow f$  is one - one but not onto

90. (a)

$$\frac{1}{\sqrt{2k}} \int_0^{\pi/3} \frac{\tan \theta}{\sqrt{\sec \theta}} d\theta = \frac{1}{\sqrt{2k}} \int_0^{\pi/3} \frac{\sin \theta}{\sqrt{\cos \theta}} d\theta$$

$$= -\frac{1}{\sqrt{2k}} 2\sqrt{\cos \theta} \Big|_0^{\pi/3} = -\frac{\sqrt{2}}{\sqrt{k}} \left(\frac{1}{\sqrt{2}} - 1\right)$$

$$\Rightarrow k = 2$$