

## PART -A (PHYSICS)

1. A particle of mass  $m$  is moving along a trajectory given by

$$x = x_0 + a \cos \omega_1 t$$

$$y = y_0 + b \sin \omega_2 t$$

The torque, acting on the particle about the origin, at  $t = 0$  is:

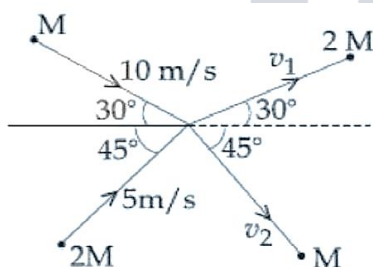
- (a)  $my_0 a \omega_1^2 \hat{k}$
- (b)  $m(-x_0 b + y_0 a) \omega_1^2 \hat{k}$
- (c)  $-m(-x_0 b \omega_2^2 - y_0 a \omega_1^2) \hat{k}$
- (d) Zero

2. A stationary source emits sound waves of frequency 500 Hz. Two observers moving along a line passing through the source detect sound to be of frequencies 480 Hz and 530 Hz. Their respective speeds are, in  $\text{ms}^{-1}$  (Given speed of sound = 300 m/s)

- (a) 16,14
- (b) 12,16
- (c) 8,18
- (d) 12,18

3. Two particles, of masses  $M$  and  $2M$ , moving as shown, with speeds of 10 m/s and 5 m/s, collide elastically at the origin. After the collision, they move along the indicated directions with speeds  $v_1$  and  $v_2$  respectively. The value of  $v_1$  and  $v_2$  are nearly:

- (a) 3.2 m/s and 12.6 m/s
- (b) 6.5 m/s and 6.3 m/s
- (c) 6.5 m/s and 3.2 m/s
- (d) 3.2 m/s and 6.3 m/s



4. Given below in the left column are different modes of communication using the kinds of waves given in the right column.

A. Optical Fibre Communication

P. Ultrasound

B. Radar

Q. Infrared Light

C. Sonar

R. Microwaves

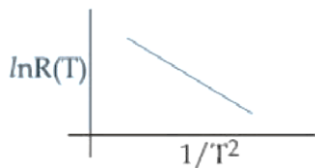
D. Mobile Phones

S. Radio Waves

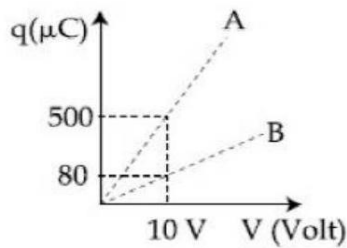
From the options given below, find the most appropriate match between entries in the left and the right column.

- (a) A - S, B - Q, C - R, D - P
- (b) A - Q, B - S, C - P, D - R
- (c) A - R, B - P, C - S, D - Q
- (d) A - Q, B - S, C - R, D - P

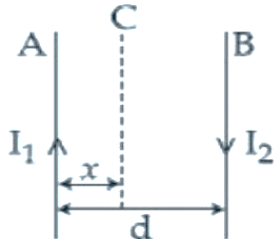
5. In an experiment, the resistance of a material is plotted as a function of temperature (in some range). As shown in the figure, it is a straight line. One may conclude that:



- (a)  $R(T) = R_0 e^{T^2/T_0^2}$  (b)  $R(T) = \frac{R_0}{T^2}$
- (c)  $R(T) = R_0 e^{T^2/T_0^2}$  (d)  $R(T) = R_0 e^{-T_0^2/T^2}$
6. A cylinder with fixed capacity of 67.2 lit contains helium gas at STP. The amount of heat needed to raise the temperature of the gas by  $20^\circ\text{C}$  is: [Given that  $R = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$ ]
- (a) 350 J (b) 700 J
- (c) 748 J (d) 374 J
7. A ball is thrown upward with an initial velocity  $V_0$  from the surface of the earth. The motion of the ball is affected by a drag force equal to  $m\gamma v^2$  (where  $m$  is mass of the ball,  $v$  is its instantaneous velocity and  $\gamma$  is a constant). Time taken by the ball to rise to its zenith is:
- (a)  $\frac{1}{\sqrt{\gamma g}} \ln \left( 1 + \sqrt{\frac{\gamma}{g}} V_0 \right)$
- (b)  $\frac{1}{\sqrt{\gamma g}} \tan^{-1} \left( \sqrt{\frac{\gamma}{g}} V_0 \right)$
- (c)  $\frac{1}{\sqrt{\gamma g}} \sin^{-1} \left( \sqrt{\frac{\gamma}{g}} v_0 \right)$
- (d)  $\frac{1}{\sqrt{2\gamma g}} \tan^{-1} \left( \sqrt{\frac{2\gamma}{g}} v_0 \right)$
8. A thin disc of mass  $M$  and radius  $R$  has mass per unit area  $\sigma(r) = kr^2$  where  $r$  is the distance from its centre. Its moment of inertia about an axis going through its centre of mass and perpendicular to its plane is:
- (a)  $\frac{MR^2}{2}$  (b)  $\frac{MR^2}{3}$
- (c)  $\frac{MR^2}{6}$  (d)  $\frac{2MR^2}{3}$
9. Two coaxial discs, having moments of inertia  $I_1$  and  $\frac{I_1}{2}$ , are rotating with respectively angular velocities  $\omega_1$  and  $\frac{\omega_1}{2}$ , about their common axes. They are brought in contact with each other and thereafter they rotate with a common angular velocity. If  $E_f$  and  $E_i$  are the final and initial total energies, then  $(E_f - E_i)$  is:
- (a)  $\frac{I_1 \omega_1^2}{6}$  (b)  $\frac{3}{8} I_1 \omega_1^2$
- (c)  $-\frac{I_1 \omega_1^2}{12}$  (d)  $-\frac{I_1 \omega_1^2}{24}$
10. The ratio of surface tensions of mercury and water is given to be 7.5 while the ratio of their densities is 13.6. Their contact angles, with glass, are close to  $135^\circ$  and  $0^\circ$ , respectively. It is observed that mercury gets depressed by an amount  $h$  in a capillary tube of radius  $r_1$ , while water rises by the same amount  $h$  in a capillary tube of radius  $r_2$ . The ratio,  $(r_1/r_2)$ , is then close to:
- (a) 3/5 (b) 4/5
- (c) 2/3 (d) 2/5
11. Figure shows charge ( $q$ ) versus voltage ( $V$ ) graph for series and parallel combination of two given capacitors. The capacitances are:
- (a)  $40\mu\text{F}$  and  $10\mu\text{F}$  (b)  $50\mu\text{F}$  and  $30\mu\text{F}$
- (c)  $60\mu\text{F}$  and  $40\mu\text{F}$  (d)  $20\mu\text{F}$  and  $30\mu\text{F}$



12. Two wires A and B are carrying currents  $I_1$  and  $I_2$  as shown in the figure. The separation between them is  $d$ . A third wire C carrying a current  $I$  is to be kept parallel to them at a distance  $x$  from A such that the net force acting on it is zero. The possible values of  $x$  are:



- (a)  $x = \left(\frac{I_1}{I_1 - I_2}\right) d$  and  $x = \frac{I_2}{(I_1 + I_2)} d$   
 (b)  $x = \pm \frac{I_1 d}{(I_1 - I_2)}$   
 (c)  $x = \left(\frac{I_2}{I_1 + I_2}\right) d$  and  $x = \left(\frac{I_2}{I_1 - I_2}\right) d$   
 (d)  $x = \left(\frac{I_1}{I_1 + I_2}\right) d$  and  $x = \left(\frac{I_2}{I_1 - I_2}\right) d$

13. A proton, an electron, and a Helium nucleus, have the same energy. They are in circular orbitals in a plane due to magnetic field perpendicular to the plane. Let  $r_p, r_e$  and  $r_{He}$  be their respective radii, then,

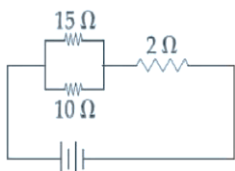
- (a)  $r_e > r_p = r_{He}$  (b)  $r_e > r_p > r_{He}$   
 (c)  $r_e < r_p < r_{He}$  (d)  $r_e < r_p = r_{He}$

14. The value of acceleration due to gravity at Earth's surface is  $9.8 \text{ ms}^{-2}$ . The altitude above its surface at which the acceleration due to gravity decreases to  $4.9 \text{ ms}^{-2}$ , is close to: (Radius of earth =  $6.4 \times 10^6 \text{ m}$ )

- (a)  $6.4 \times 10^6 \text{ m}$  (b)  $9.0 \times 10^6 \text{ m}$   
 (c)  $2.6 \times 10^6 \text{ m}$  (d)  $1.6 \times 10^6 \text{ m}$

15. In the given circuit, an ideal voltmeter connected across the  $10\Omega$  resistance reads 2 V. The internal resistance  $r$ , of each cell is:

- (a)  $1\Omega$  (b)  $0.5\Omega$   
 (c)  $1.5\Omega$  (d)  $0\Omega$



1.5 V, 1.5 V

$r\Omega$   $r\Omega$

16. The electric field of a plane electromagnetic wave is given by

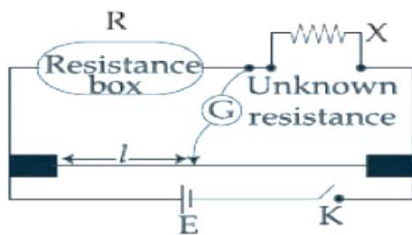
$$\vec{E} = E_0 \hat{i} \cos(kz) \cos(\omega t)$$

The corresponding magnetic field  $\vec{B}$  is then given by:

- (a)  $\vec{B} = \frac{E_0}{c} \hat{j} \sin(kz) \cos(\omega t)$

- (b)  $\vec{B} = \frac{E_0}{c} \hat{k} \sin(kz) \cos(\omega t)$   
(c)  $\vec{B} = \frac{E_0}{c} \hat{j} \cos(kz) \sin(\omega t)$   
(d)  $\vec{B} = \frac{E_0}{c} \hat{j} \sin(kz) \sin(\omega t)$

17. An npn transistor operates as a common emitter amplifier, with a power gain of 60 dB. The input circuit resistance is  $100\Omega$  and the output load resistance is  $10k\Omega$ . the common emitter current gain  $\beta$  is:  
(a)  $6 \times 10^2$  (b)  $10^2$   
(c) 60 (d)  $10^4$
18. In a meter bridge experiment, the circuit diagram and the corresponding observation table are shown in figure.

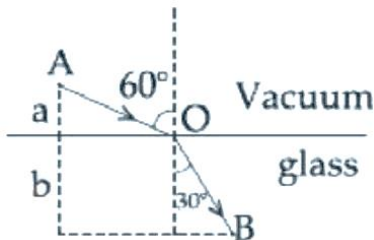


| Sl. No. | R( $\Omega$ ) | I (cm) |
|---------|---------------|--------|
| 1.      | 1000          | 60     |
| 2.      | 100           | 13     |
| 3.      | 10            | 1.5    |
| 4.      | 1             | 1.0    |

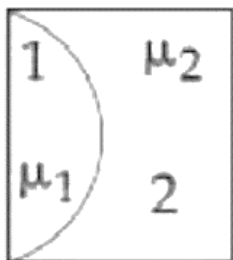
Which of the readings is inconsistent?

- (a) 4 (b) 3  
(c) 2 (d) 1
19. A transformer consisting of 300 turns in the primary and 150 turns in the secondary gives output power of 2.2 kW. If the current in the secondary coils is 10 A, then the input voltage and current in the primary coil are:  
(a) 440 V and 5 A (b) 440 and 20 A  
(c) 220 V and 20 A (d) 220 V and 10 A
20. A uniformly charged ring of radius  $3a$  and total charge  $q$  is placed in  $xy$ -plane centered at origin. A point charge  $q$  is moving towards the ring along the  $z$ -axis and has speed  $v$  at  $z = 4a$ . The minimum value of  $v$  such that it crosses the origin is:  
(a)  $\sqrt{\frac{2}{m} \left( \frac{1}{5} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$  (b)  $\sqrt{\frac{2}{m} \left( \frac{1}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$   
(c)  $\sqrt{\frac{2}{m} \left( \frac{4}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$  (d)  $\sqrt{\frac{2}{m} \left( \frac{2}{15} \frac{q^2}{4\pi\epsilon_0 a} \right)^{1/2}}$
21. A current of 5 A passes through a copper conductor (resistivity =  $1.7 \times 10^{-8} \Omega m$ ) of radius of cross-section 5 mm. Find the mobility of the charges if their drift velocity is  $1.1 \times 10^{-3} m/s$ .  
(a)  $1.8 m^2/Vs$  (b)  $1.0 m^2/Vs$   
(c)  $1.3 m^2/Vs$  (d)  $1.5 m^2/Vs$
22.  $n$ -moles of an ideal gas with constant volume heat capacity  $C_V$  undergo an isobaric expansion by certain volume. The ratio of the work done in the process, to the heat supplied is  
(a)  $\frac{nR}{C_V - nR}$  (b)  $\frac{nR}{C_V + nR}$   
(c)  $\frac{4nR}{C_V + nR}$  (d)  $\frac{4nR}{C_V - nR}$

23. A message signal of frequency 100MHz and peak voltage 100 V is used to execute amplitude modulation on a carrier wave of frequency 300GHz and peak voltage 400 V. The modulation index and difference between the two side band frequencies are:
- (a)  $4; 2 \times 10^8$  Hz (b)  $4; 1 \times 10^8$  Hz  
(c)  $0.25; 1 \times 10^8$  Hz (d)  $0.25; 2 \times 10^8$  Hz
24. A ray of light  $AO$  in vacuum is incident on a glass slab at angle  $60^\circ$  and refracted at angle  $30^\circ$  along  $OB$  as shown in the figure. The optical path length of light ray from  $A$  to  $B$  is :



- (a)  $2a + \frac{2b}{\sqrt{3}}$  (b)  $2a + \frac{2b}{3}$   
(c)  $\frac{2\sqrt{3}}{a} + 2b$  (d)  $2a + 2b$
25. The displacement of a damped harmonic oscillator is given by  $x(t) = e^{-0.1t} \cos(10\pi t + \phi)$ . Here  $t$  is in seconds. The time taken for its amplitude of vibration to drop to half of its initial value is close to:
- (a) 13 s (b) 27 S  
(c) 4 s (d) 7 s
26. Two radioactive materials  $A$  and  $B$  have decay constants  $10\lambda$  and  $\lambda$ , respectively. If initially they have the same number of nuclei, then the ratio of the number of nuclei of  $A$  to that of  $B$  will be  $1/e$  after a time:
- (a)  $\frac{1}{11\lambda}$  (b)  $\frac{1}{10\lambda}$   
(c)  $\frac{1}{9\lambda}$  (d)  $\frac{11}{10\lambda}$
27. A  $25 \times 10^{-3} \text{ m}^3$  volume cylinder is filled with 1 mol of  $\text{O}_2$  gas at room temperature ( 300 K). The molecular diameter of  $\text{O}_2$ , and its root mean square speed, are found to be 0.3 nm and 200 m/s, respectively. What is the average collision rate (per second) for an  $\text{O}_2$  molecule?
- (a)  $\sim 10^{10}$  (b)  $\sim 10^{11}$   
(c)  $\sim 10^{12}$  (d)  $\sim 10^{13}$
28. In a photoelectric effect experiment the threshold wavelength of incident light is 260 nm, the maximum kinetic energy of emitted electrons will be: Given  $E$  (in eV) =  $\frac{1237}{\lambda(\text{ in nm})}$
- (a) 15.1eV (b) 1.5eV  
(c) 4.5eV (d) 3.0eV
29. One plano-convex and one plano-concave lens of same radius of curvature '  $R$  ' but of different materials are joined side by side as shown in the figure. If the refractive index of the material of 1 is  $\mu_1$  and that of 2 is  $\mu_2$ , then the focal length of the combination is



- (a)  $\frac{R}{2(\mu_1 - \mu_2)}$  (b)  $\frac{2R}{\mu_1 - \mu_2}$   
(c)  $\frac{R}{\mu_1 - \mu_2}$  (d)  $\frac{R}{2 - (\mu_1 - \mu_2)}$

30. A moving coil galvanometer allows a full -scale current of  $10^{-4}$  A. A series resistance of  $2\text{M}\Omega$  is required to convert the above galvanometer into a voltmeter of range 0 – 5 V. Therefore, the value of shunt resistance required to convert the above galvanometer into an ammeter of range 0 – 10 mA is:
- (a)  $200\Omega$  (b)  $100\Omega$   
(c)  $10\Omega$  (d)  $500\Omega$

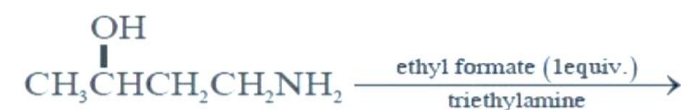
## PART -B (CHEMISTRY)

31. The species that can have a trans-isomer is:

(en = ethane-1,2-diamine, ox = oxalate )

- (a)  $[\text{Pt}(\text{en})\text{Cl}_2]$  (b)  $[\text{Pt}(\text{en})_2\text{Cl}_2]^{2+}$   
(c)  $[\text{Cr}(\text{en})_2(\text{ox})]^+$  (d)  $[\text{Zn}(\text{en})\text{Cl}_2]$

32. The major product of the following reaction is



- (a)  $\text{CH}_3\overset{\text{OH}}{\underset{|}{\text{CH}}}-\text{CH}=\text{CH}_2$  (b)  $\text{CH}_3\overset{\text{O}}{\underset{|}{\text{C}}}=\text{CH}-\text{CH}_2\text{CH}_2\text{NH}_2$   
(c)  $\text{CH}_3\text{CH}=\text{CH}-\text{CH}_2\text{NH}_2$   
(d)  $\text{CH}_3\overset{\text{OH}}{\underset{|}{\text{CH}}}\text{CH}_2\text{CH}_2\text{NHCHO}$

33. The synonym for water gas when used in the production of methanol is

- (a) syn gas (b) natural gas  
(c) fuel gas (d) laughing gas

34. The regions of the atmosphere, where clouds form and where we live, respectively, are:

- (a) Troposphere and Stratosphere  
(b) Troposphere and Troposphere  
(c) Stratosphere and Stratosphere  
(d) Stratosphere and Troposphere

35. Consider the hydrated ions of  $\text{Ti}^{2+}$ ,  $\text{V}^{2+}$ ,  $\text{Ti}^{3+}$  and  $\text{Sc}^{3+}$ . The correct order of their spin-only magnetic moments is:

- (a)  $\text{Ti}^{3+} < \text{V}^{2+} < \text{Sc}^{3+} < \text{Ti}^{2+}$   
(b)  $\text{Sc}^{3+} < \text{Ti}^{3+} < \text{Ti}^{2+} < \text{V}^{2+}$   
(c)  $\text{V}^{2+} < \text{Ti}^{2+} < \text{Ti}^{3+} < \text{Sc}^{3+}$   
(d)  $\text{Sc}^{3+} < \text{Ti}^{3+} < \text{V}^{2+} < \text{Ti}^{2+}$

36. Amylopectin is composed of

- (a)  $\alpha$ -D-glucose,  $\text{C}_1 - \text{C}_4$  and  $\text{C}_2 - \text{C}_6$  linkages  
(b)  $\beta$ -D-glucose,  $\text{C}_1 - \text{C}_4$  and  $\text{C}_2 - \text{C}_6$  linkages  
(c)  $\alpha$ -D-glucose,  $\text{C}_1 - \text{C}_4$  and  $\text{C}_1 - \text{C}_6$  linkages  
(d)  $\beta$ -D-glucose,  $\text{C}_1 - \text{C}_4$  and  $\text{C}_1 - \text{C}_6$  linkages

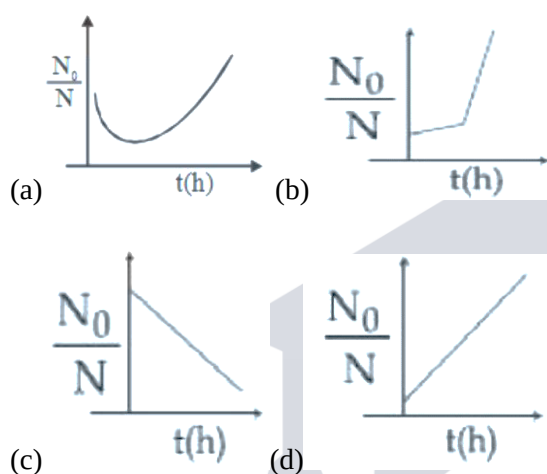
37. A gas undergoes physical adsorption on a surface and follows the given Freundlich adsorption isotherm equation

$$\frac{x}{m} = k p p^{0.5}$$

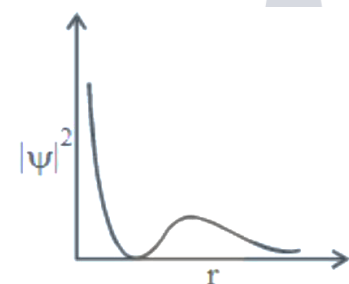
Adsorption of the gas increases with:

- (a) Increase in  $p$  and decrease in  $T$
- (b) Increase in  $p$  and increase in  $T$
- (c) Decrease in  $p$  and increase in  $T$
- (d) Decrease in  $p$  and decrease in  $T$

38. A bacterial infection in an internal wound grows as  $N'(t) = N_0 \exp(t)$ , where the time  $t$  is in hours. A dose of antibiotic, taken orally, needs 1 hour to reach the wound. Once it reaches there, the bacterial population goes down as  $\frac{dN}{dt} = -5N^2$ . What will be the plot of  $\frac{N_0}{N}$  vs.  $t$  after 1 hour?



39. The graph between  $|\psi|^2$  and  $r$  (radial distance) is shown below. This represents:



- (a) 1 s orbital
- (b) 3 s orbital
- (c) 2 s orbital
- (d) 2 p orbital

40. Consider the following table:

| Gas | $a/(\text{kPa dm}^3 \text{ mol}^{-1})$ | $b/(\text{dm}^3 \text{ mol}^{-1})$ |
|-----|----------------------------------------|------------------------------------|
| A   | 642.32                                 | 0.05196                            |
| B   | 155.21                                 | 0.04136                            |
| C   | 431.91                                 | 0.05196                            |
| D   | 155.21                                 | 0.4382                             |

**a and b a van der Waals constants. The correct statement about the gases is:**

- (a) Gas C will occupy more volume than gas A ; gas B will be lesser compressible than gas D
- (b) Gas C will occupy lesser volume than gas A ; gas B will be more compressible than gas D.
- (c) Gas C will occupy lesser volume than gas A; gas B will be lesser compressible than gas D
- (d) Gas C will occupy more volume than gas A; gas B will be more compressible than gas D.

**41. During the change of  $O_2$  to  $O_2^-$ , the incoming electron goes to the orbital:**

- (a)  $\pi 2p_y$  (b)  $\pi * 2p_x$
- (c)  $\sigma * 2p_z$  (d)  $\sigma * 2p_x$

**42. The principle of column chromatography is**

- (a) Differential absorption of the substances on the solid phase.
- (b) Differential adsorption of the substances on the solid phase.
- (c) Gravitational force.
- (d) Capillary action.

**43. At 300 K and 1 atmospheric pressure, 10 mL of a hydrocarbon required 55 mL of  $O_2$  for complete combustion, and 40 mL of  $CO_2$  is formed. The formula of the hydrocarbon is:**

- (a)  $C_4H_{10}$  (b)  $C_4H_6$
- (c)  $C_4H_7Cl$  (d)  $C_4H_8$

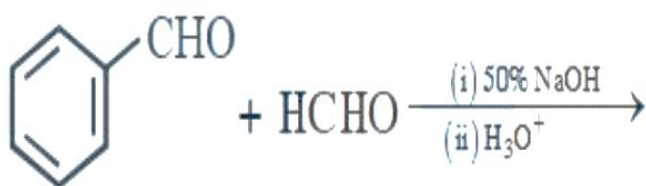
**44. Three complexes,**

$[CoCl(NH_3)_5]^{2+}$  (I),  $[Co(NH_3)_5H_2O]^{3+}$  (II) and  $[Co(NH_3)_6]^{3+}$  (III)

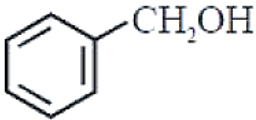
**Absorb light in the visible region. The correct order of the wavelength of light absorbed by them is**

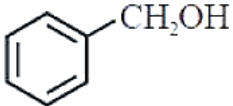
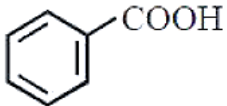
- (a) (II) > (I) > (III) (b) (III) > (II) > (I)
- (c) (I) > (II) > (III) (d) (III) > (I) > (II)

**45. Major products of the following reaction are:**

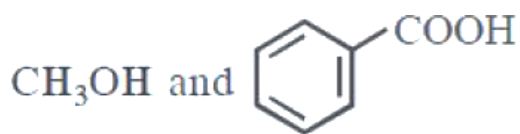


- (a)  $CH_3OH$  and  $HCO_2H$

- (b)  $HCOOH$  and 

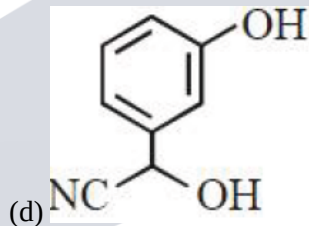
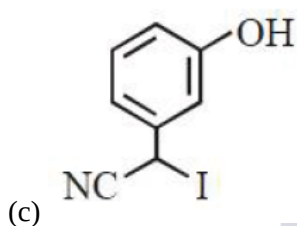
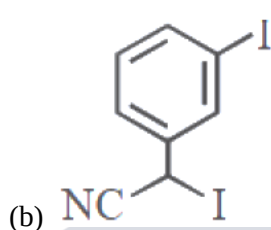
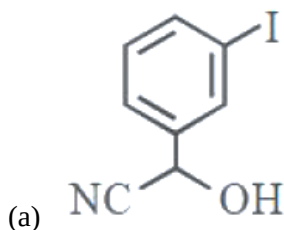
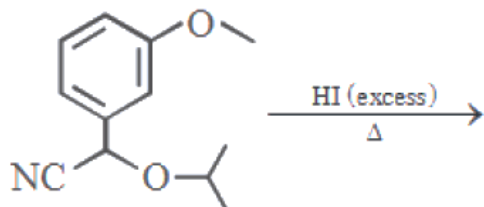
- (c)  and 





(d)

46. The major product of the following reaction is



47. Match the refining methods (Column I) with metals (Column II).

Column I

(Refining methods)

(I) Liquation

(II) zone Refining

(III) Mond process

(IV) Van Arkel Method

Column II

(Metals)

(a) Zr

(b) Ni

(c) Sn

(d) Ga

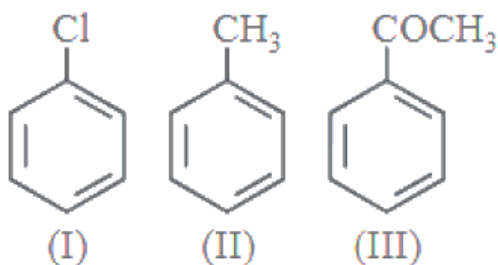
(a) (I) - (b); (II) - (c); (III) - (d); (IV) - (a)

(b) (I) - (b); (II) - (d); (III) - (a); (IV) - (c)

(c) (I) - (c); (II) - (a); (III) - (b); (IV) - (d)

(d) (I) - (c); (II) - (d); (III) - (b); (IV) - (a)

48. The increasing order of the reactivity of the following compounds towards electrophilic aromatic substitution reaction is:



- (a) (III) < (I) < (II)                      (b) (III) < (II) < (I)  
(c) (II) < (I) < (III)                      (d) (I) < (III) < (II)

49. A process will be spontaneous at all temperatures if:

- (a)  $\Delta H < 0$  and  $\Delta S < 0$   
(b)  $\Delta H < 0$  and  $\Delta S > 0$   
(c)  $\Delta H > 0$  and  $\Delta S > 0$   
(d)  $\Delta H > 0$  and  $\Delta S < 0$

50. Consider the following statements

- (a) The pH of a mixture containing 400 mL of 0.1M  $\text{H}_2\text{SO}_4$  and 400 mL of 0.1M NaOH will be approximately 1.3 .  
(b) Ionic product of water is temperature dependent.  
(c) A monobasic acid with  $K_a = 10^{-5}$  has a pH = 5. the degree of dissociation of this acid is 50%.  
(d) The Le Chatelier's principle is not applicable to common-ion effect.

The correct statements are:

- (a) (a) and (b)                      (b) (a), (b) and (c)  
(c) (b) and (c)                      (d) (a), (b) and (d)

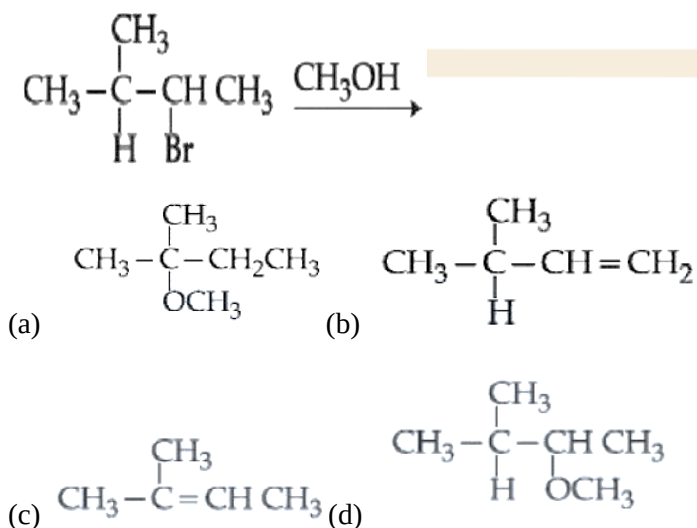
51. Ethylamine ( $\text{C}_2\text{H}_5\text{NH}_2$ ) can be obtained from N-ethylphthalimide on treatment with:

- (a)  $\text{CaH}_2$                       (b)  $\text{H}_2\text{O}$   
(c)  $\text{NaBH}_4$                       (d)  $\text{NH}_2\text{NH}_2$

52. The correct order of catenation is:

- (a)  $\text{C} > \text{Sn} > \text{Si} \approx \text{Ge}$                       (b)  $\text{Ge} > \text{Sn} > \text{Si} > \text{C}$   
(c)  $\text{Si} > \text{Sn} > \text{C} > \text{Ge}$                       (d)  $\text{C} > \text{Si} > \text{Ge} \approx \text{Sn}$

53. The major product of the following reaction is



54. Which of the following is a condensation polymer?

- (a) Nylon 6, 6 (b) Neoprene  
(c) Buna-S (d) Teflon

55. Consider the statements S1 and S2:

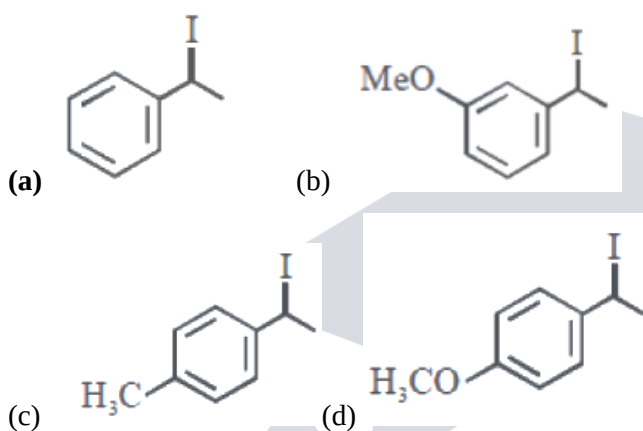
S1: Conductivity always increases with decrease in the concentration of electrolyte.

S2: Molar conductivity always increases with decrease in the concentration of electrolyte.

The correct option among the following is:

- (a) S1 is wrong and S2 is correct  
(b) Both S1 and S2 are wrong  
(c) S1 is correct and S2 is wrong  
(d) Both S1 and S2 are correct

56. Increasing rate of  $S_N1$  reaction in the following compounds is



- (a) (A) < (B) < (C) < (D)  
(b) (A) < (B) < (d) < (c)  
(c) (b) < (a) < (d) < (c)  
(d) (B) < (A) < (C) < (D)

57. The oxoacid of sulphur that does not contain bond between sulphur atoms is:

- (a)  $H_2 S_2 O_3$  (b)  $H_2 S_2 O_4$   
(c)  $H_2 S_2 O_7$  (d)  $H_2 S_4 O_6$

58. The isoelectronic set of ions is

- (a)  $Li^+$ ,  $Na^+$ ,  $O^{2-}$  and  $F^-$   
(b)  $F^-$ ,  $Li^+$ ,  $Na^+$  and  $Mg^{2+}$   
(c)  $N^{3-}$ ,  $O^{2-}$ ,  $F^-$  and  $Na^+$   
(d)  $N^{3-}$ ,  $Li^+$ ,  $Mg^{2+}$  and  $O^{2-}$

59. The alloy used in the construction of aircrafts is

- (a) Mg – Mn (b) Mg – Zn  
(c) Mg – Al (d) Mg – Sn

60. At room temperature, a dilute solution of urea is prepared by dissolving 0.60 g of urea in 360 g of water. If the vapour pressure of pure water at this temperature is 35 mmHg, lowering of vapour pressure will be: (molar mass of urea =  $60 \text{ g mol}^{-1}$ )

- (a) 0.027mmHg (b) 0.031mmHg  
(c) 0.028mmHg (d) 0.017mmHg

### PART-C (MATHEMATICS)

61. If  $Q(0, -1, -3)$  is the image of the point  $P$  in the plane  $3x - y, 1.4z = 2$  and  $R$  is the point  $(3, -1, -2)$ , then the area (in square units) of  $\triangle PQR$  is:

- (a)  $\frac{\sqrt{91}}{2}$  (b)  $2\sqrt{13}$   
 (c)  $\frac{\sqrt{65}}{2}$  (d)  $\frac{\sqrt{91}}{4}$

62. If the coefficients of  $x^2$  and  $x^3$  are both zero, in the expansion of the expression  $(1 + ax + bx^2)(1 - 3x)^{t5}$  in powers of  $x$ , then the ordered pair  $(a, b)$  is equal to

- (a)  $(-54, 315)$  (b)  $(28, 861)$   
 (c)  $(28, 315)$  (d)  $(-21, 714)$

63. The sum

$$\frac{3 \times 1}{1^2} + \frac{5 \times (1^3 + 2^3)}{1^2 + 2^2} + \frac{7 \times (1^3 + 2^3 + 3^3)}{1^2 + 2^2 + 3^2} + \dots \dots \dots$$

Upto  $10^{\text{th}}$  term, is

- (a) 620 (b) 660  
 (c) 680 (d) 600

64. If the length of the perpendicular from the point  $(\beta, 0, \beta)$  ( $\beta \neq 0$ ) to the line,  $\frac{x}{1} = \frac{y-1}{0} = \frac{z+1}{-1}$  is  $\sqrt{\frac{3}{2}}$ , then  $\beta$  is equal to:

- (a) 1 (b) -1  
 (c) 2 (d) -2

65. If  $f(x) = \begin{cases} \frac{\sin(p+1)x + \sin x}{x} & , x < 0 \\ q & , x = 0 \\ \frac{\sqrt{x+x^2} - \sqrt{x}}{x/2} & , x > 0 \end{cases}$

Is continuous at  $x = 0$ , then the ordered pair  $(p, d)$  is equal to

- (a)  $(-\frac{3}{2}, -\frac{1}{2})$  (b)  $(\frac{5}{2}, \frac{1}{2})$   
 (c)  $(-\frac{1}{2}, \frac{3}{2})$  (d)  $(-\frac{3}{2}, \frac{1}{2})$

66. Which one of the following Boolean expressions is a tautology?

- (a)  $(p \vee q) \wedge (p \vee \sim q)$   
 (b)  $(p \wedge q) \vee (p \wedge \sim q)$   
 (c)  $(p \vee q) \wedge (\sim p \vee \sim q)$   
 (d)  $(p \vee q) \vee (p \vee \sim q)$

67. If  $\alpha$  and  $\beta$  are the roots of the quadratic equation,  $x^2 + x \sin \theta - 2 \sin \theta = 0$ ,  $\theta \in (0, \frac{\pi}{2})$  then

$\frac{\alpha^{12} + \beta^{12}}{(\alpha^{-12} + \beta^{-12})(\alpha - \beta)^{24}}$  is equal to:

- (a)  $\frac{2^{12}}{(\sin \theta + 8)^{12}}$  (b)  $\frac{2^{12}}{(\sin \theta - 4)^{12}}$   
 (c)  $\frac{2^{12}}{(\sin \theta - 8)^6}$  (d)  $\frac{2^6}{(\sin \theta + 8)^{12}}$

68.  $ABC$  is a triangular park with  $AB = AC = 100$  metres. A vertical tower is situated at the mid-point of  $BC$ .

If the angles of elevation of the top of the tower at  $A$  and  $B$  are  $\cot^{-1}(3\sqrt{2})$  and  $\operatorname{cosec}^{-1}(2\sqrt{2})$  respectively, then the height of the tower (in metres) is:

- (a) 25 (b)  $10\sqrt{5}$   
 (c)  $\frac{100}{3\sqrt{3}}$  (d) 20

69. If  $a > 0$  and  $z = \frac{(1+i)^2}{a-i}$ , has magnitude  $\sqrt{\frac{2}{5}}$ , then  $\bar{z}$  is equal to:

- (a)  $-\frac{3}{5} - \frac{1}{5}i$  (b)  $-\frac{1}{5} - \frac{3}{5}i$   
 (c)  $-\frac{1}{5} + \frac{3}{5}i$  (d)  $\frac{1}{5} - \frac{3}{5}i$

70. If  $\Delta_1 = \begin{vmatrix} x & \sin \theta & \cos \theta \\ \sin \theta & -x & 1 \\ \cos \theta & 1 & x \end{vmatrix}$  and

$\Delta_2 = \begin{vmatrix} x & \sin 2\theta & \cos 2\theta \\ \sin 2\theta & -x & 1 \\ \cos 2\theta & 1 & x \end{vmatrix}, x \neq 0$ ; then

for all  $\theta \in \left(0, \frac{\pi}{2}\right)$ :

(a)  $\Delta_1 - \Delta_2 = -2x^3$

(b)  $\Delta_1 + \Delta_2 = -2(x^3 + x - 1)$

(c)  $\Delta_1 - \Delta_2 = x(\cos 2\theta - \cos 4\theta)$

(d)  $\Delta_1 + \Delta_2 = -2x^3$

71. If  $y = 1f(x)$  is the solution of the differential equation  $\frac{dy}{dx} = (\tan x - y)\sec^2 x, x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ , such that

$y(0) = 0$ , then  $y\left(-\frac{\pi}{4}\right)$  is equal to

(a)  $\frac{1}{2} - e$

(b)  $\frac{1}{e} - 2$

(c)  $e - 2$

(d)  $2 + \frac{1}{e}$

72. Let  $f: R \rightarrow R$  be differentiable at  $c \in R$  and  $f(c) = 0$ . If  $g(x) = |f(x)|$ , then at  $x = c$ ,  $g$  is:

(a) differentiable if  $f'(c) = 0$

(b) differentiable if  $f'(c) \neq 0$

(c) not differentiable

(d) not differentiable if  $f'(c) = 0$

73. Let  $f(x) = x^2, x \in R$ . For any  $A \subseteq R$ , define  $g(A) = \{x \in R: f(x) \in A\}$ . If  $S = [0, 4]$ , then which one of the following statements is not true?

(a)  $f(g(S)) \neq f(S)$

(b)  $f(g(S)) = S$

(c)  $g(f(S)) \neq S$

(d)  $g(f(S)) = g(S)$

74. If the system of linear equations

$x + y + z = 5$

$x = 2y + 2z = 6$

$x + 3y + \lambda z = u (\lambda, \mu \in R)$ , has infinitely many solutions then the value of  $\lambda + \mu$  is:

(a) 12

(b) 7

(c) 10

(d) 9

75. The number of 6 digit numbers hat can be formed using the digits 0, 1, 2, 5, 7 and 9 which are divisible by 11 and no digits is repeated, is

(a) 36

(b) 60

(c) 72

(d) 48

76. The line  $x = y$  touches a circle at the point  $(1, 1)$ . If the circle also passes through the point  $(1, -3)$ , then its radius is

(a)  $3\sqrt{2}$

(b) 3

(c) 2

(d)  $2\sqrt{2}$

77. Let  $f(x) = e^x - x$  and  $g(x) = x^2 - x, \forall x \in R$ . Then the set of all  $x \in R$ , where the function  $h(x) = (f \circ g)(x)$  is increasing is:

(a)  $\left[0, \frac{1}{2}\right] \cup [1, \infty)$

(b)  $\left[1, \frac{1}{2}\right] \cup \left[\frac{1}{2}, \infty\right)$

(c)  $\left[\frac{-1}{2}, 0\right] \cup [1, \infty)$

(d)  $[0, \infty)$

78. The value of  $\int_0^{2\pi} [\sin 2x(1 + \cos 3x)]dx$  where  $[t]$  denotes the greatest integer function, is:

(a)  $\pi$

(b)  $-2\pi$

(c)  $2\pi$

(d)  $-\pi$

79. If the circles  $x^2 + y^2 + 5Kx + 2y + K = 0$  and  $2(x^2 + y^2) + 2Kx + 3y - 1 = 0$ , ( $K \in R$ ), intersect at the points  $P$  and  $Q$ , then the line  $4x + 5y - K = 0$  passes through  $P$  and  $Q$  for:

- (a) exactly one value of  $K$
- (b) not value of  $K$
- (c) infinitely many values of  $K$
- (d) exactly two values of  $K$

80. If the lines  $x - 2y = 12$  is tangent to the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  at the point  $(3, \frac{9}{2})$ , then the length of the latus rectum of the ellipse is

- (a)  $12\sqrt{2}$
- (b) 9
- (c)  $8\sqrt{3}$
- (d) 5

81. If  $a_1, a_2, a_3, \dots, a_n$  are in A.P and  $a_1 + a_4 + a_7 + \dots + a_{16} = 114$ , then  $a_1 + a_6 + a_{11} + a_{16}$  is equal to

- (a) 76
- (b) 64
- (c) 98
- (d) 38

82. If for some  $x \in R$ , the frequency distribution of the marks obtained by 20 students in a test is

| Marks     | 2           | 3        | 5          | 7   |
|-----------|-------------|----------|------------|-----|
| Frequency | $(x + 1)^2$ | $2x - 5$ | $x^2 - 3x$ | $x$ |

Then the mean of the marks is:

- (a) 2.8
- (b) 3.2
- (c) 2.5
- (d) 3.0

83. If  $\lim_{x \rightarrow 1} \frac{x^4 - 1}{x - 1} = \lim_{x \rightarrow k} \frac{x^3 - k^3}{x^2 - k^2}$ , then  $k$  is

- (a)  $\frac{3}{8}$
- (b)  $\frac{8}{3}$
- (c)  $\frac{4}{3}$
- (d)  $\frac{3}{2}$

84. All the pairs  $(x, y)$  that satisfy the inequality  $2^{\sqrt{\sin^2 x - 2\sin x + 5}} \cdot \frac{1}{4^{\sin^2 y}} \leq 1$  also

Satisfy the equation:

- (a)  $2|\sin x| = 3\sin y$
- (b)  $\sin x = |\sin y|$
- (c)  $2\sin x = \sin y$
- (d)  $\sin x = 2\sin y$

85.  $\lim_{n \rightarrow \infty} \left( \frac{(n+1)^{1/3}}{n^{4/3}} + \frac{(n+2)^{1/3}}{n^{4/3}} + \dots + \frac{(2n)^{1/3}}{n^{4/3}} \right)$

is equal to:

- (a)  $\frac{3}{4}(2)^{4/3} - \frac{3}{4}$
- (b)  $\frac{4}{3}(2)^{3/4}$
- (c)  $\frac{3}{4}(2)^{4/3} - \frac{4}{3}$
- (d)  $\frac{4}{3}(2)^{4/3}$

86. If a directrix of a hyperbola centered at the origin and passing through the point  $(4, -2\sqrt{3})$  is  $5x = 4\sqrt{5}$  and its eccentricity is  $e$ , then

- (a)  $4e^4 + 8e^2 - 35 = 0$
- (b)  $4e^4 - 24e^2 + 35 = 0$
- (c)  $4e^4 - 12e^2 - 27 = 0$
- (d)  $4e^4 - 24e^2 + 27 = 0$

87. The region represented by  $|x - y| \leq 2$  and  $|x + y| \leq 2$  is bounded by  $a$  :

- (a) rhombus of area  $8\sqrt{2}$  sq. units
- (b) square of area 16 sq. units
- (c) rhombus of side length 2 units
- (d) square of side length  $2\sqrt{2}$  units

88. Assume that each born child is equally likely to be a boy or a girl. If two families have two children each, then the conditional probability that all children are girls given that at least two are girls is:

- (a)  $\frac{1}{10}$  (b)  $\frac{1}{17}$   
(c)  $\frac{1}{12}$  (d)  $\frac{1}{11}$

89. Let  $A(3, 0, -1)$ ,  $B(2, 10, 6)$  and  $C(1, 2, 1)$  be the vertices of a triangle and  $M$  be the midpoint of  $AC$ . If  $G$  divides  $BM$  in the ratio, 2: 1, then  $\cos(\angle GOA)$  ( $O$  being the origin) is equal to:

- (a)  $\frac{1}{\sqrt{30}}$  (b)  $\frac{1}{2\sqrt{15}}$   
(c)  $\frac{1}{6\sqrt{10}}$  (d)  $\frac{1}{\sqrt{15}}$

90. If  $\int \frac{dx}{(x^2 - 2x + 10)^2}$

$$= A \left( \tan^{-1} \left( \frac{x-1}{3} \right) + \frac{f(x)}{x^2 - 2x + 10} \right) + C$$

Where  $C$  is a constant of integration, then:

- (a)  $A = \frac{1}{27}$  and  $f(x) = -(x-1)$   
(b)  $A = \frac{1}{54}$  and  $f(x) = 9(x-1)^2$   
(c)  $A = \frac{1}{54}$  and  $f(x) = 3(x-1)$   
(d)  $A = \frac{1}{81}$  and  $f(x) = 3(x-1)$

