

Physics Section-A

1. Young's double slit interference apparatus is immersed in a liquid of refractive index 1.44. It has slit separation of 1.5 mm . The slits are illuminated by a parallel beam of light whose wavelength in air is 690 nm . The fringe-width on a screen placed behind the plane of slits at a distance of 0.72 m , will be :

(a) 0.23 mm (b) 0.33 mm
(c) 0.63 mm (d) 0.46 mm

2. Arrange the following in the ascending order of wavelength (λ) :

(A) Microwaves (λ_1)
(B) Ultraviolet rays (λ_2)
(C) Infrared rays (λ_3)
(D) X-rays (λ_4)

Choose the most appropriate answer from the options given below :-

(a) $\lambda_4 < \lambda_3 < \lambda_2 < \lambda_1$
(b) $\lambda_3 < \lambda_4 < \lambda_2 < \lambda_1$
(c) $\lambda_4 < \lambda_2 < \lambda_3 < \lambda_1$
(d) $\lambda_4 < \lambda_3 < \lambda_1 < \lambda_2$

3. Given below are two statements. One is labelled as Assertion (A) and the other is labelled as Reason(R).

Assertion (A) : A electron in a certain region of uniform magnetic field is moving with constant velocity in a straight- line path.

Reason (A) : The magnetic field in that region is along the direction of velocity of the electron.

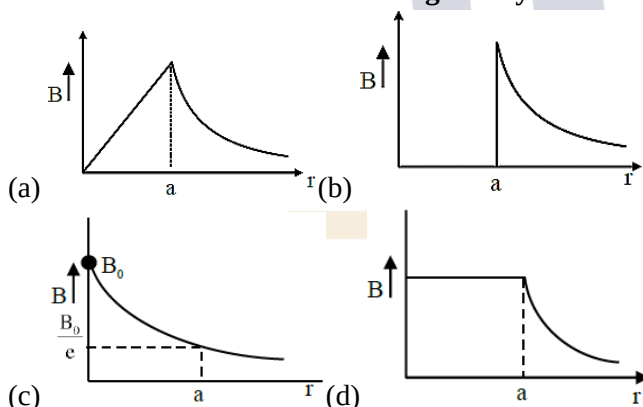
In the light of the above statements, choose the correct answer from the options given below :

(a) (A) is false but (R) is true
(b) Both (A) and (R) are true and (R) is the correct explanation of (A)
(c) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
(d) (A) is true but (R) is false

4. A solid sphere is rolling without slipping on a horizontal plane. The ratio of the linear kinetic energy of the centre of mass of the sphere and rotational kinetic energy is :

(a) $\frac{2}{5}$ (b) $\frac{5}{2}$ (c) $\frac{3}{4}$ (d) $\frac{4}{3}$

5. A long straight wire of a circular cross-section with radius ' a ' carries a steady current I. The current I is a uniformly distributed across this cross-section The plot of magnitude of magnetic field B with distance r from the centre of the wire is given by



6. Given below are two statements. One is labelled as

Assertion (A) and the other is labelled as Reason(R).

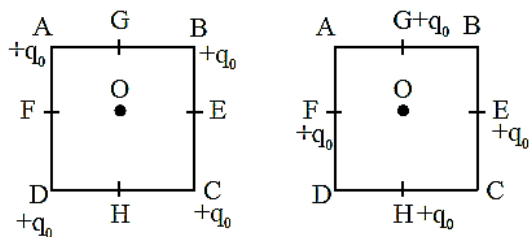
Assertion (A) : In an insulated container, a gas is adiabatically shrunk to half of its initial volume. The temperature of the gas decreases.

Reason (R) : Free expansion of an ideal gas is an irreversible and an adiabatic process.

In the light of the above statement, choose the correct answer from the options given below :

(a) Both (A) and (R) are true and (R) is the correct explanation of (A)
(b) (A) is true but (R) is false
(c) (A) is false but (R) is true
(d) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)

7.



Configuration(1) **Configuration(2)**

In the first configuration (1) as shown in the figure, four identical charges (q_0) are kept at the corners A, B, C and D of square of side length 'a'. In the second configuration (2), the same charges are shifted to mid points G, E, H and F, of the square, If $K = \frac{1}{4\pi\epsilon_0}$, the difference between the potential energies of configuration (2) and

(1) is given by :

- (a) $\frac{Kq_0^2}{a}(4\sqrt{2} - 2)$ (b) $\frac{Kq_0^2}{a}(3 - \sqrt{2})$
(c) $\frac{Kq_0^2}{a}(4 - 2\sqrt{2})$ (d) $\frac{Kq_0^2}{a}(3\sqrt{2} - 2)$

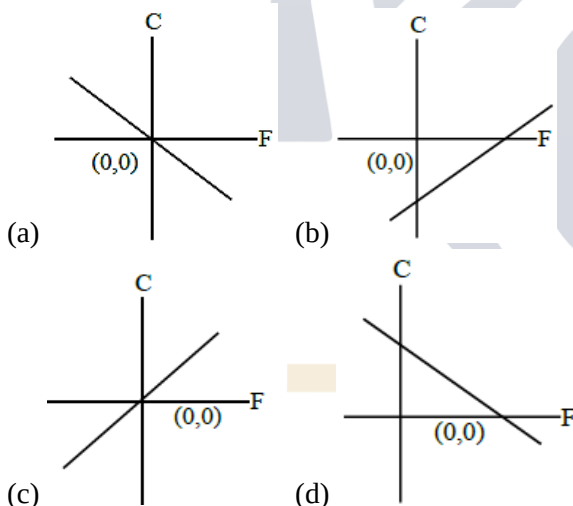
8. The position vector of a moving body at any instant of time is given as $\vec{r} = (5t^2\hat{i} - 5t\hat{j})\text{m}$. The magnitude and direction of velocity at $t = 2\text{ s}$ is,

- (a) $5\sqrt{15}\text{ m/s}$, making an angle of $\tan^{-1} 4$ with -ve Y axis
(b) $5\sqrt{15}\text{ m/s}$, making an angle of $\tan^{-1} 4$ with +ve X axis
(c) $5\sqrt{17}\text{ m/s}$, making an angle of $\tan^{-1} 4$ with -ve Y axis
(d) $5\sqrt{17}\text{ m/s}$, making an angle of $\tan^{-1} 4$ with +ve X axis

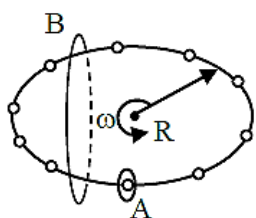
9. A solid sphere and a hollow sphere of the same mass and of same radius are rolled on an inclined plane. Let the time taken to reach the bottom by the solid sphere and the hollow sphere be t_1 and t_2 , respectively, then

- (a) $t_1 < t_2$ (b) $t_1 = t_2$
(c) $t_1 = 2t_2$ (d) $t_1 > t_2$

10. Which of the following figure represents the relation between Celsius and Fahrenheit temperatures?



11.



N equally spaced charges each of value q , are placed on a circle of radius R . The circle rotates about its axis with an angular velocity ω as shown in the figure. A bigger Amperian loop B encloses the whole circle where as a smaller Amperian loop A encloses a small segment. The difference between enclosed currents, $I_A - I_B$, for the given Amperian loops is

- (a) $\frac{N^2}{2\pi} q\omega$ (b) $\frac{2\pi}{N} q\omega$
(c) $\frac{N}{2\pi} q\omega$ (d) $\frac{N}{\pi} q\omega$

12. In photoelectric effect, the stopping potential (V_0) v/s frequency (ν) curve is plotted.

(h is the Planck's constant and ϕ_0 is work function of metal)

(A) $V_0 \nu / \nu$ is linear

(B) The slope of $V_0 \nu / \nu$ curve = $\frac{\phi_0}{h}$

(C) h constant is related to the slope of $V_0 \nu / \nu$ line

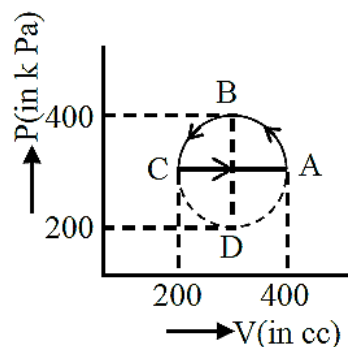
(D) The value of electric charge of electron is not required to determine h using the $V_0 \nu / \nu$ curve.

(E) The work function can be estimated without knowing the value of h .

Choose the correct answer from the options given below :

- (a) (A), (B) and (C) only
(b) (C) and (D) only
(c) (A), (C) and (E) only
(d) (D) and (E) only

13. The magnitude of heat exchanged by a system for the given cyclic process ABCA (as shown in figure) is (in SI unit)

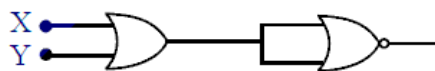


- (a) 10π (b) 5π
(c) zero (d) 40π

14. A photograph of a landscape is captured by a drone camera at a height of 18 km . The size of the camera film is 2 cm $\times$ 2 cm and the area of the landscape photographed is 400 km². The focal length of the lens in the drone camera is :

- (a) 1.8 cm (b) 2.8 cm
(c) 2.5 cm (d) 0.9 cm

15. The output of the circuit is low (zero) for :



- (A) $X = 0, Y = 0$ (B) $X = 0, Y = 1$
(C) $X = 1, Y = 0$ (D) $X = 1, Y = 1$

Choose the correct answer from the options given below :

- (a) (A), (C) and (D) only
(b) (A), (B) and (C) only
(c) (B), (C) and (D) only
(d) (A), (B) and (D) only

16. The temperature of a body in air falls from 40°C to 24°C in 4 minutes. The temperature of the air is 16°C.

The temperature of the body in the next 4 minutes will be :

- (a) $\frac{14}{3}^\circ\text{C}$ (b) $\frac{28}{3}^\circ\text{C}$
(c) $\frac{56}{3}^\circ\text{C}$ (d) $\frac{42}{3}^\circ\text{C}$

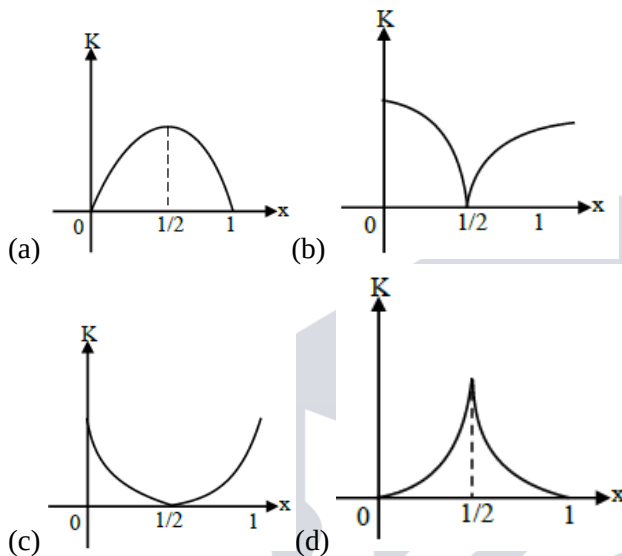
17. The energy E and momentum p of a moving body of mass m are related by some equation. Given that c represents the speed of light, identify the correct equation.

- (a) $E^2 = pc^2 + m^2c^4$
 (b) $E^2 = pc^2 + m^2c^2$
 (c) $E^2 = p^2c^2 + m^2c^2$
 (d) $E^2 = p^2c^2 + m^2c^4$

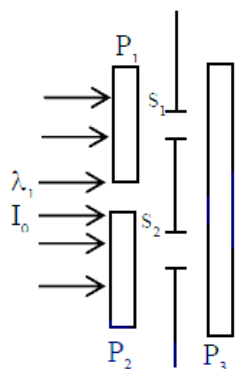
18. A small uncharged conducting sphere is placed in contact with an identical sphere but having 4×10^{-8} C charge and then removed to a distance such that the force of repulsion between them is 9×10^{-3} N. The distance between them is (Take $\frac{1}{4\pi\epsilon_0}$ as 9×10^9 in SI units)

- (a) 2 cm (b) 3 cm
 (c) 4 cm (d) 1 cm

19. A particle oscillates along the x-axis according to the law, $x(t) = x_0 \sin^2\left(\frac{t}{2}\right)$ where $x_0 = 1$ m. The kinetic energy (K) of the particle as a function of x is correctly represented by the graph.



20. In a Young's double slit experiment, three polarizers are kept as shown in the figure. The transmission axes of P_1 and P_2 are orthogonal to each other. The polarizer P_3 covers both the slits with its transmission axis at 45° to those of P_1 and P_2 . An unpolarized light of wavelength λ and intensity I_0 is incident on P_1 and P_2 . The intensity at a point after P_3 where the path difference between the light waves from s_1 and s_2 is $\frac{\lambda}{3}$, is



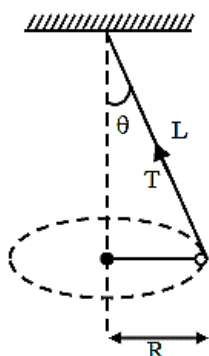
- (a) $\frac{I_0}{2}$ (b) $\frac{I_0}{4}$ (c) I_0 (d) $\frac{I_0}{3}$

Section - B

21. A tightly wound long solenoid carries a current of 1.5 A. An electron is executing uniform circular motion inside the solenoid with a time period of 75 ns. The number of turns per metre in the solenoid is ____.

[Take mass of electron $m_0 = 9 \times 10^{-31}$ kg, charge of electron $|q_0| = 1.6 \times 10^{-19}$ C, $\mu_0 = 4\pi \times 10^{-7} \frac{N}{A^2}$, $1 \text{ ns} = 10^{-9} \text{ s}$]

22.



A string of length L is fixed at one end and carries a mass of M at the other end. The mass makes $\left(\frac{3}{\pi}\right)$ rotations per second about the vertical axis passing through end of the string as shown. The tension in the string is ____ ML.

23. The ratio of the power of a light source S_1 to that the light source S_2 is 2 . S_1 is emitting 2×10^{15} photons per second at 600 nm . If the wavelength of the source S_2 is 300 nm , then the number of photons per second emitted by S_2 is ____ $\times 10^{14}$.
24. The increase in pressure required to decrease the volume of a water sample by 0.2% is $P \times 10^5 \text{ Nm}^{-2}$. Bulk modulus of water is $2.15 \times 10^9 \text{ Nm}^{-2}$. The value of P is ____
25. Acceleration due to gravity on the surface of earth is ' g ' . If the diameter of earth is reduced to one third of its original value and mass remains unchanged, then the acceleration due to gravity on the surface of the earth is ____ g .

Chemistry Section - A

26. Based on the data given below:

$$E_{\text{C}_2\text{O}_7^{2-}/\text{Cr}^{3+}}^0 = 1.33 \text{ V} \quad E_{\text{Cl}_2/\text{Cl}^{(-)}}^0 = 1.36 \text{ V}$$

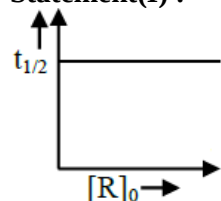
$$E_{\text{MnO}_4^-/\text{Mn}^{2+}}^0 = 1.51 \text{ V} \quad E_{\text{Cr}^{3+}/\text{Cr}^{2+}}^0 = -0.74 \text{ V}$$

the strongest reducing agent is :

- (a) Mn^{2+} (b) Cr
(c) MnO_4^- (d) Cl^-

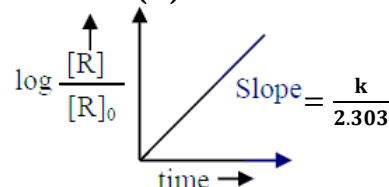
27. Given below are two statements :

Statement(I) :



is valid for first order reaction.

Statement(II) :

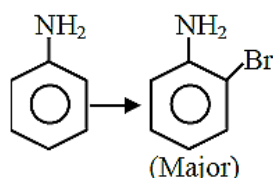


is valid for first order reaction

In the light of the above statements, choose the correct answer from the options given below :

- (a) Both Statement I and Statement II are false
(b) Statement I is false but Statement II is true
(c) Both Statement I and Statement II are true
(d) Statement I is true but Statement II is false

28. For reaction



The correct order of set of reagents for the above conversion is :

- (a) $\text{Br}_2 \mid \text{FeBr}_3, \text{H}_2\text{O}(\Delta), \text{NaOH}$
 (b) $\text{H}_2\text{SO}_4, \text{Ac}_2\text{O}, \text{Br}_2, \text{H}_2\text{O}(\Delta), \text{NaOH}$
 (c) $\text{Ac}_2\text{O}, \text{Br}_2, \text{H}_2\text{O}(\Delta), \text{NaOH}$
 (d) $\text{Ac}_2\text{O}, \text{H}_2\text{SO}_4, \text{Br}_2, \text{NaOH}$

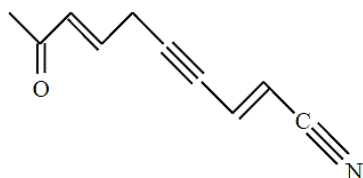
29. For hydrogen atom, the orbital/s with lowest energy is/are :

- (A) $4s$ (B) $3p_x$
(C) $3d_{x^2-y^2}$ (D) $3d_{z^2}$
(E) $4p_z$

Choose the correct answer from the options given below :

- (a) (A) and (E) only (b) (B) only
(c) (A) only (d) (B), (C) and (D) only

30. In the given structure, number of sp and sp^2 hybridized carbon atoms present respectively are :



- (a) 3 and 6 (b) 3 and 5
(c) 4 and 6 (d) 4 and 5

31. Which of the following mixing of 1 M base and 1 M acid leads to the largest increase in temperature?

- (a) 30 mL HCl and 30 mL NaOH
(b) 30 mL CH_3COOH and 30 mL NaOH
(c) 50 mL HCl and 20 mL NaOH
(d) 45 mL CH_3COOH and 25 mL NaOH

32. Given below are two statements:

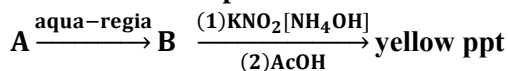
Statement(I) : Experimentally determined oxygen-oxygen bond lengths in the O_3 are found to be same and the bond length is greater than that of a $O = O$ (double bond) but less than that of a single ($O - O$) bond.

Statement (II) : The strong lone pair-lone pair repulsion between oxygen atoms is solely responsible for the fact that the bond length in ozone is smaller than that of a double bond ($\text{O}=\text{O}$) but more than that of a single bond ($\text{O}-\text{O}$).

In the light of the above statements, choose the correct answer from the options given below:

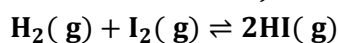
- (a) Statement I is true but Statement II is false
(b) Both Statement I and Statement II are true
(c) Both Statement I and Statement II are false
(d) Statement I is false but Statement II is true

33. Find the compound 'A' from the following reaction sequences.

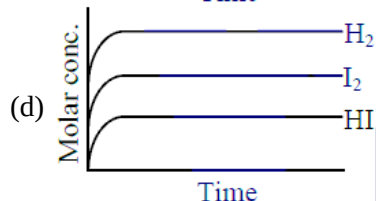
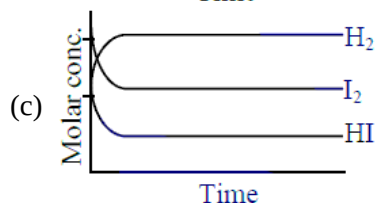
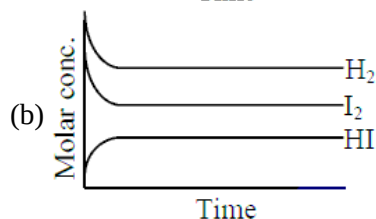
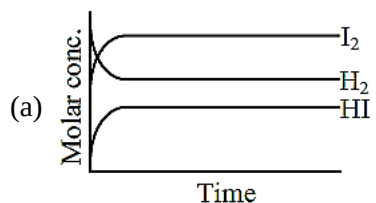


- (a) ZnS (b) CoS
(c) MnS (d) NiS

34. For the reaction,



Attainment of equilibrium is predicted correctly by:



35. Match List-I with List-II.

List-I		List-II	
(Transition metal ion)		(Spin only magnetic moment (B.M.))	
(A)	Ti ³⁺	(I)	3.87
(B)	V ²⁺	(II)	0.00
(C)	Ni ²⁺	(III)	1.73
(D)	Sc ³⁺	(IV)	2.84

Choose the correct answer from the options given below :

- (a) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)
 (b) (A)-(III), (B)-(I), (C)-(IV), (D)-(II)
 (c) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)
 (d) (A)-(II), (B)-(IV), (C)-(I), (D)-(III)

36. The elemental composition of a compound is 54.2% C, 9.2% H and 36.6% O. If the molar mass of the compound is 132 g mol⁻¹, the molecular formula of the compound is :

[Given : The relative atomic mass of C: H: O = 12: 1: 16]

- (a) C₄H₉O₃ (b) C₆H₁₂O₆
 (c) C₆H₁₂O₃ (d) C₄H₈O₂

37. When Ethane-1,2-diamine is added progressively to an aqueous solution of Nickel (II) chloride, the sequence of colour change observed will be :

- (a) Pale Blue → Blue → Green → Violet
 (b) Pale Blue → Blue → Violet → Green
 (c) Green → Pale Blue → Blue → Violet
 (d) Violet → Blue → Pale Blue → Green

38. The conditions and consequence that favours the t_{2g}³, e_g¹ configuration in a metal complex are :

- (a) weak field ligand, high spin complex
 (b) strong field ligand, high spin complex
 (c) strong field ligand, low spin complex
 (d) weak field ligand, low spin complex

39. Identify correct statement/s :

- (A) $-\text{OCH}_3$ and $-\text{NHCOCH}_3$ are activating group
 (B) $-\text{CN}$ and $-\text{OH}$ are meta directing group
 (C) $-\text{CN}$ and $-\text{SO}_3\text{H}$ are meta directing group
 (D) Activating groups act as ortho - and para directing groups
 (E) Halides are activating groups

Choose the correct answer from the options given below :

- (a) (A), (C) and (D) only
 (b) (A), (B) and (E) only
 (c) (A) only
 (d) (A) and (C) only

40. Given below are two statements :

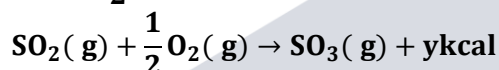
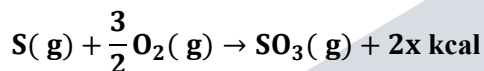
Statement (I): The first ionization energy of Pb is greater than that of Sn

Statement(II) : The first ionization energy of Ge is greater than that of Si .

In the light of the above statements, choose the correct answer from the options given below :

- (a) Statement I is true but Statement II is false
 (b) Both Statement I and Statement II are false
 (c) Statement I is false but Statement II is true
 (d) Both Statement I and Statement II are true

41.

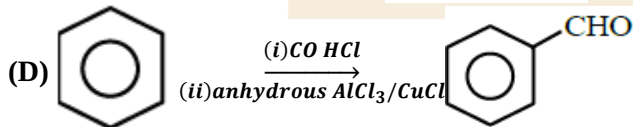
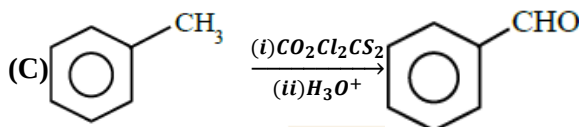
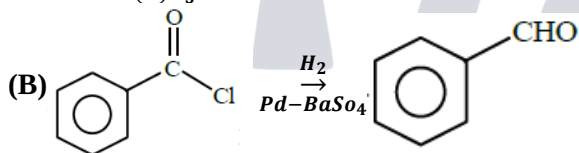
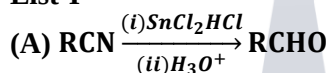


The heat of formation of $\text{SO}_2(\text{g})$ is given by :

- (a) $\frac{2x}{y}$ kcal (b) $y - 2x$ kcal
 (c) $2x + y$ kcal (d) $x + y$ kcal

42. Match List-I with List-II

List-I



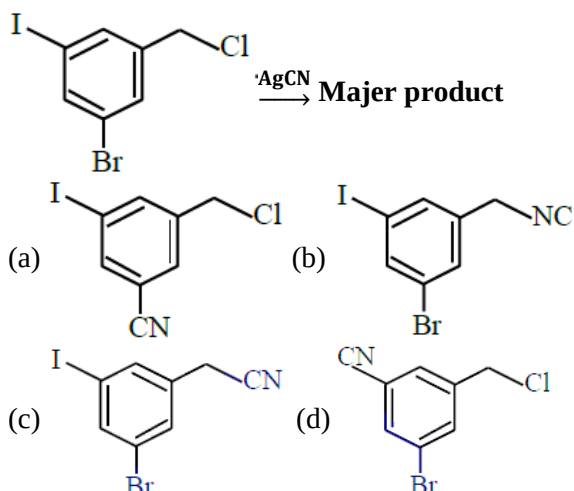
List-II

- (I) Etard reaction
 (II) Gatterman -Koch reaction
 (III) Rosenmund reduction
 (IV) Stephen reaction

Choose the correct answer from the options given below :

- (a) (A)-(IV), (B)-(III), (C)-(I), (D)-(II)
 (b) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
 (c) (A)-(I), (B)-(III), (C)-(II), (D)-(IV)
 (d) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

43. The structure of the major product formed in the following reaction is :

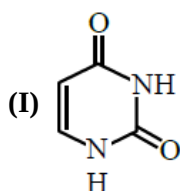


44. Match List-I with List-II.

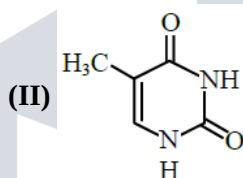
List-I

List-II

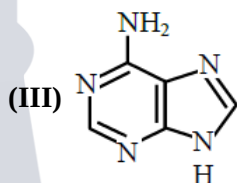
(A) Adenine



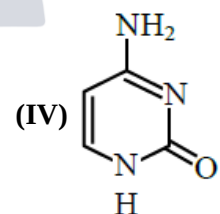
(B) Cytosine



(C) Thymine



(D) Uracil



Choose the correct answer from the options given below :

- (a) (A)-(III), (B)-(IV), (C)-(II), (D)-(I)
 (b) (A)-(III), (B)-(I), (C)-(IV), (D)-(II)
 (c) (A)-(IV), (B)-(III), (C)-(II), (D)-(I)
 (d) (A)-(III), (B)-(IV), (C)-(I), (D)-(II)

45. The successive 5 ionisation energies of an element are 800, 2427, 3658, 25024 and 32824 kJ/mol, respectively. By using the above values predict the group in which the above element is present :

- (a) Group 2 (b) Group 13
 (c) Group 4 (d) Group 14

Section - B

46. The observed and normal masses of compound MX_2 are 65.6 and 164 respectively. The percent degree of ionisation of MX_2 is ____ %. (Nearest integer)

47. The possible number of stereoisomers for 5-phenylpent-4-en-2-ol is ____ .

48. Consider a complex reaction taking place in three steps with rate constants k_1 , k_2 and k_3 respectively. The overall rate constant k is given by the expression $k = \sqrt{\frac{k_1 k_3}{k_2}}$. If the activation energies of the three steps are 60, 30 and 10 kJ mol^{-1} respectively, then the overall energy of activation in kJ mol^{-1} is _____. (Nearest integer)
49. The hydrocarbon (X) with molar mass 80 g mol^{-1} and 90% carbon has _____ degree of unsaturation.
50. In Carius method of estimation of halogen, 0.25 g of an organic compound gave 0.15 g of silver bromide (AgBr). The percentage of Bromine in the organic compound is _____ $\times 10^{-1}\%$ (Nearest integer). (Given : Molar mass of Ag is 108 and Br is 80 g mol^{-1})

Mathematics

Section - A

51. The equation of the chord, of the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$, whose mid-point is (3, 1) is :
 (a) $48x + 25y = 169$
 (b) $4x + 122y = 134$
 (c) $25x + 101y = 176$
 (d) $5x + 16y = 31$
52. The function $f: (-\infty, \infty) \rightarrow (-\infty, 1)$, defined by $f(x) = \frac{2^x - 2^{-x}}{2^x + 2^{-x}}$ is :
 (a) One-one but not onto
 (b) Onto but not one-one
 (c) Both one-one and onto
 (d) Neither one-one nor onto
53. If $\alpha > \beta > \gamma > 0$, then the expression $\cot^{-1} \left\{ \beta + \frac{(1 + \beta^2)}{(\alpha - \beta)} \right\} + \cot^{-1} \left\{ \gamma + \frac{(1 + \gamma^2)}{(\beta - \gamma)} \right\} + \cot^{-1} \left\{ \alpha + \frac{(1 + \alpha^2)}{(\gamma - \alpha)} \right\}$ is equal to:
 (a) $\frac{\pi}{2} - (\alpha + \beta + \gamma)$ (b) 3π
 (c) 0 (d) π
54. Let $f: (0, \infty) \rightarrow \mathbb{R}$ be a function which is differentiable at all points of its domain and satisfies the condition $x^2 f'(x) = 2xf(x) + 3$, with $f(1) = 4$. Then $2f(2)$ is equal to:
 (a) 29 (b) 19 (c) 39 (d) 23
55. Let $A = \left\{ x \in (0, \pi) - \left\{ \frac{\pi}{2} \right\} : \log_{(2/\pi)} |\sin x| + \log_{(2/\pi)} |\cos x| = 2 \right\}$
 And $B = \{ x \geq 0 : \sqrt{x}(\sqrt{x} - 4) - 3|\sqrt{x} - 2| + 6 = 0 \}$. Then $n(A \cup B)$ is equal to:
 (a) 4 (b) 2 (c) 8 (d) 6
56. Let the position vectors of three vertices of a triangle be $4\vec{p} + \vec{q} - 3\vec{r}$, $-5\vec{p} + \vec{q} + 2\vec{r}$ and $2\vec{p} - \vec{q} + 2\vec{r}$. If the position vectors of the orthocenter and the circumcenter of the triangle are $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$ and $\alpha\vec{p} + \beta\vec{q} + \gamma\vec{r}$ respectively, then $\alpha + 2\beta + 5\gamma$ is equal to:
 (a) 3 (b) 1 (c) 6 (d) 4
57. Let $[x]$ denote the greatest integer function, and let m and n respectively be the numbers of the points, where the function $f(x) = [x] + |x - 2|$, $-2 < x < 3$, is not continuous and not differentiable. Then $m + n$ is equal to:
 (a) 6 (b) 9 (c) 8 (d) 7
58. Let the points $\left(\frac{11}{2}, \alpha \right)$ lie on or inside the triangle with sides $x + y = 11$, $x + 2y = 16$ and $2x + 3y = 29$. Then the product of the smallest and the largest values of α is equal to :
 (a) 22 (b) 44 (c) 33 (d) 55

59. In an arithmetic progression, if $S_{40} = 1030$ and $S_{12} = 57$, then $S_{30} - S_{10}$ is equal to:

- (a) 510 (b) 515
(c) 525 (d) 505

60. If $7 = 5 + \frac{1}{7}(5 + \alpha) + \frac{1}{7^2}(5 + 2\alpha) + \frac{1}{7^3}(5 + 3\alpha) + \dots$, then the value of α is:

- (a) 1 (b) $\frac{6}{7}$ (c) 6 (d) $\frac{1}{7}$

61. If the system of equations

$$x + 2y - 3z = 2$$

$$2x + \lambda y + 5z = 5$$

$$14x + 3y + \mu z = 33$$

has infinitely many solutions, then $\lambda + \mu$ is equal to:

- (a) 13 (b) 10 (c) 11 (d) 12

62. Let $(2, 3)$ be the largest open interval in which the function $f(x) = 2\log_e(x - 2) - x^2 + ax + 1$ is strictly increasing and (b, c) be the largest open interval, in which the function $g(x) = (x - 1)^3(x + 2 - a)^2$ is strictly decreasing. Then $100(a + b - c)$ is equal to:

- (a) 280 (b) 360
(c) 420 (d) 160

63. Suppose A and B are the coefficients of 30^{th} and 12^{th} terms respectively in the binomial expansion of $(1 + x)^{2n-1}$. If $2A = 5B$, then n is equal to:

- (a) 22 (b) 21 (c) 20 (d) 19

64. Let $\vec{a} = 3\hat{i} - \hat{j} + 2\hat{k}$, $\vec{b} = \vec{a} \times (\hat{i} - 2\hat{k})$ and $\vec{c} = \vec{b} \times \hat{k}$. Then the projection of $\vec{c} - 2\hat{j}$ on $\vec{a}$ is:

- (a) $3\sqrt{7}$ (b) $\sqrt{14}$
(c) $2\sqrt{14}$ (d) $2\sqrt{7}$

65. For some a, b, let

$$f(x) = \begin{vmatrix} a + \frac{\sin x}{x} & 1 & b \\ a & 1 + \frac{\sin x}{x} & b \\ a & 1 & b + \frac{\sin x}{x} \end{vmatrix}, x \neq 0$$

$\lim_{x \rightarrow 0} f(x) = \lambda + \mu a + \nu b$. Then $(\lambda + \mu + \nu)^2$ is equal to:

- (a) 25 (b) 9 (c) 36 (d) 16

66. Group A consists of 7 boys and 3 girls, while group B consists of 6 boys and 5 girls. The number of ways, 4 boys and 4 girls can be invited for a picnic if 5 of them must be from group A and the remaining 3 from group B, is equal to:

- (a) 8575 (b) 9100
(c) 8925 (d) 8750

67. The area of the region enclosed by the curves $y = e^x$, $y = |e^x - 1|$ and y-axis is:

- (a) $1 + \log_e 2$ (b) $\log_e 2$
(c) $2\log_e 2 - 1$ (d) $1 - \log_e 2$

68. The number of real solution(s) of the equation $x^2 + 3x + 2 = \min\{|x - 3|, |x + 2|\}$ is:

- (a) 2 (b) 0 (c) 3 (d) 1

69. Let $A = [a_{ij}]$ be a square matrix of order 2 with entries either 0 or 1. Let E be the event that A is an invertible matrix. Then the probability P(E) is:

- (a) $\frac{5}{8}$ (b) $\frac{3}{16}$ (c) $\frac{1}{8}$ (d) $\frac{3}{8}$

70. If the equation of the parabola with vertex $V\left(\frac{3}{2}, 3\right)$ and the directrix $x + 2y = 0$ is $\alpha x^2 + \beta y^2 - \gamma xy - 30x - 60y + 225 = 0$, then $\alpha + \beta + \gamma$ is equal to:

- (a) 6 (b) 8 (c) 7 (d) 9

Section - B

71. Number of functions $f: \{1, 2, \dots, 100\} \rightarrow \{0, 1\}$, that assign 1 to exactly one of the positive integers less than or equal to 98, is equal to ____.
72. Let P be the image of the point $Q(7, -2, 5)$ in the line $L: \frac{x-1}{2} = \frac{y+1}{3} = \frac{z}{4}$ and $R(5, p, q)$ be a point on L . Then the square of the area of $\triangle PQR$ is ____
73. Let $y = y(x)$ be the solution of the differential equation $2\cos x \frac{dy}{dx} = \sin 2x - 4y\sin x$, $x \in \left(0, \frac{\pi}{2}\right)$. If $y\left(\frac{\pi}{3}\right) = 0$, then $y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right)$ is equal to ____.
74. Let $H_1: \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ and $H_2: -\frac{x^2}{A^2} + \frac{y^2}{B^2} = 1$ be two hyperbolas having length of latus rectums $15\sqrt{2}$ and $12\sqrt{5}$ respectively. Let their eccentricities be $e_1 = \sqrt{\frac{5}{2}}$ and e_2 respectively. If the product of the lengths of their transverse axes is $100\sqrt{10}$, then $25e_2^2$ is equal to ____
75. If $\int \frac{2x^2+5x+9}{\sqrt{x^2+x+1}} dx = x\sqrt{x^2+x+1} + \alpha\sqrt{x^2+x+1} + \beta \log_e \left|x + \frac{1}{2} + \sqrt{x^2+x+1}\right| + C$, where C is the constant of integration, then $\alpha + 2\beta$ is equal to ____

