

PART-I PHYSICS

SECTION-A

- Two identical metallic spheres A and B when placed at certain distance in air repel each other with a force of F . Another identical uncharged sphere C is first placed in contact with A and then in contact with B and finally placed at midpoint between spheres A and B. The force experienced by sphere C will be:
 (a) $3F/2$ (b) $3F/4$
 (c) F (d) $2F$
- Match List I with List II.

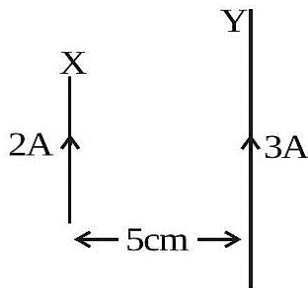
List I		List II	
A.	Torque	I.	Nms^{-1}
B.	Stress	II.	Jkg^{-1}
C.	Latent Heat	III.	Nm
D.	Power	IV.	Nm^{-2}

Choose the correct answer from the options given below:

- A-III, B-II, C-I, D-IV
 - A-III, B-IV, C-II, D-I
 - A-IV, B-I, C-III, D-II
 - A-II, B-III, C-I, D-IV
- Two identical thin metal plates has charge q_1 and q_2 respectively such that $q_1 > q_2$. The plates were brought close to each other to form a parallel plate capacitor of capacitance C . The potential difference between them is :
 (a) $\frac{(q_1+q_2)}{C}$ (b) $\frac{(q_1-q_2)}{C}$
 (c) $\frac{(q_1-q_2)}{2C}$ (d) $\frac{2(q_1-q_2)}{C}$
 - Given below are two statements: one is labelled as Assertion A and the other is labelled as Reason R.
 Assertion A: Alloys such as constantan and manganin are used in making standard resistance coils.
 Reason R: Constantan and manganin have very small value of temperature coefficient of resistance.
 In the light of the above statements, choose the correct answer from the options given below.
 (a) Both A and R are true and R is the correct explanation of A.
 (b) Both A and R are true but R is NOT the correct explanation of A.
 (c) A is true but R is false.
 (d) A is false but R is true.
 - A 1 m long wire is broken into two unequal parts X and Y. The X part of the wire is stretched into another wire W. Length of W is twice the length of X and the resistance of W is twice that of Y. Find the ratio of length of X and Y.

- (a) 1: 4 (b) 1: 2
(c) 4: 1 (d) 2: 1

6. A wire X of length 50 cm carrying a current of 2 A is placed parallel to a long wire Y of length 5 m. The wire Y carries a current of 3 A. The distance between two wires is 5 cm and currents flow in the same direction. The force acting on the wire Y is:



- (a) 1.2×10^{-5} N directed towards wire X.
(b) 1.2×10^{-4} N directed away from wire X.
(c) 1.2×10^{-4} N directed towards wire X.
(d) 2.4×10^{-5} N directed towards wire X.
7. A juggler throws balls vertically upwards with same initial velocity in air. When the first ball reaches its highest position, he throws the next ball. Assuming the juggler throws n balls per second, the maximum height the balls can reach is
(a) $g/2n$ (b) g/n
(c) $2gn$ (d) $g/2n^2$
8. A circuit element X when connected to an a.c. supply of peak voltage 100 V gives a peak current of 5 A which is in phase with the voltage. A second element Y when connected to the same a.c. supply also gives the same value of peak current which lags behind the voltage by $\frac{\pi}{2}$. If X and Y are connected in series to the same supply, what will be the rms value of the current in ampere?
(a) $\frac{10}{\sqrt{2}}$ (b) $\frac{5}{\sqrt{2}}$
(c) $5\sqrt{2}$ (d) $\frac{5}{2}$
9. An unpolarised light beam of intensity $2I_0$ is passed through a polaroid P and then through another polaroid Q which is oriented in such a way that its passing axis makes an angle of 30° relative to that of P. The intensity of the emergent light is
(a) $\frac{I_0}{4}$ (b) $\frac{I_0}{2}$
(c) $\frac{3I_0}{4}$ (d) $\frac{3I_0}{2}$
10. An α particle and a proton are accelerated from rest through the same potential difference. The ratio of linear momenta acquired by above two particles will be:
(a) $\sqrt{2}: 1$ (b) $2\sqrt{2}: 1$
(c) $4\sqrt{2}: 1$ (d) $8: 1$
11. Read the following statements:
- (A) Volume of the nucleus is directly proportional to the mass number.
(B) Volume of the nucleus is independent of mass number.
(C) Density of the nucleus is directly proportional to the mass number.
(D) Density of the nucleus is directly proportional to the cube root of the mass number.

(E) Density of the nucleus is independent of the mass number.

Choose the correct option from the following options.

- (a) (A) and (D) only. (b) (A) and (E) only.
(c) (B) and (E) only. (d) (A) and (C) only

12. An object of mass 1 kg is taken to a height from the surface of earth which is equal to three times the radius of earth. The gain in potential energy of the object will be

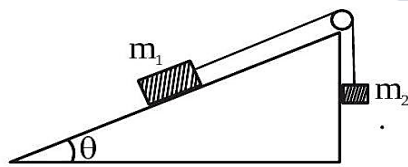
[If, $g = 10 \text{ ms}^{-2}$ and radius of earth = 6400 km]

- (a) 48MJ (b) 24MJ
(c) 36MJ (d) 12MJ

13. A ball is released from a height h . If t_1 and t_2 be the time required to complete first half and second half of the distance respectively. Then, choose the correct relation between t_1 and t_2 .

- (a) $t_1 = (\sqrt{2})t_2$ (b) $t_1 = (\sqrt{2} - 1)t_2$
(c) $t_2 = (\sqrt{2} + 1)t_1$ (d) $t_2 = (\sqrt{2} - 1)t_1$

14. Two bodies of masses $m_1 = 5 \text{ kg}$ and $m_2 = 3 \text{ kg}$ are connected by a light string going over a smooth light pulley on a smooth inclined plane as shown in the figure. The system is at rest. The force exerted by the inclined plane on the body of mass m_1 will be: [Take $g = 10 \text{ ms}^{-2}$]



- (a) 30 N (b) 40 N
(c) 50 N (d) 60 N

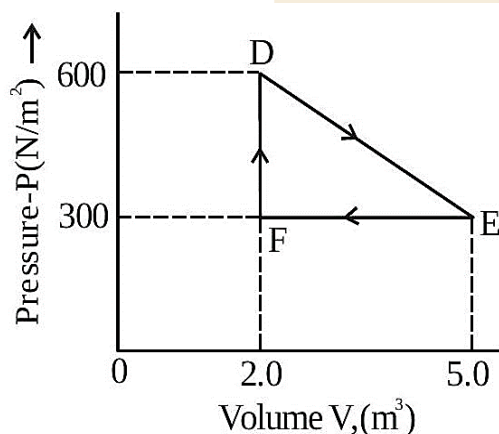
15. If momentum of a body is increased by 20%, then its kinetic energy increases by :

- (a) 36% (b) 40%
(c) 44% (d) 48%

16. The torque of a force $5\hat{i} + 3\hat{j} - 7\hat{k}$ about the origin is τ . If the force acts on a particle whose position vector is $2\hat{i} + 2\hat{j} + \hat{k}$, then the value of τ will be :

- (a) $11\hat{i} + 19\hat{j} - 4\hat{k}$ (b) $-11\hat{i} + 9\hat{j} - 16\hat{k}$
(c) $-17\hat{i} + 19\hat{j} - 4\hat{k}$ (d) $17\hat{i} + 9\hat{j} + 16\hat{k}$

17. A thermodynamic system is taken from an original state D to an intermediate state E by the linear process shown in the figure. Its volume is then reduced to the original volume from E to F by an isobaric process. The total work done by the gas from D to E to F will be

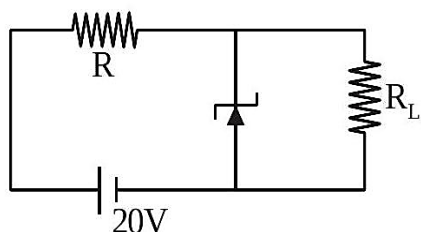


- (a) -450 J (b) 450 J
(c) 900 J (d) 1350 J

18. The vertical component of the earth's magnetic field is 6×10^{-5} T at any place where the angle of dip is 37° . The earth's resultant magnetic field at that place will be (Given $\tan 37^\circ = \frac{3}{4}$)
- (a) 8×10^{-5} T (b) 6×10^{-5} T
(c) 5×10^{-4} T (d) 1×10^{-4} T
19. The root mean square speed of smoke particles of mass 5×10^{-17} kg in their Brownian motion in air at NTP is approximately. [Given $k = 1.38 \times 10^{-23} \text{ JK}^{-1}$]
- (a) 60 mm s^{-1} (b) 12 mm s^{-1}
(c) 15 mm s^{-1} (d) 36 mm s^{-1}
20. Light enters from air into a given medium at an angle of 45° with interface of the air-medium surface. After refraction, the light ray is deviated through an angle of 15° from its original direction. The refractive index of the medium is:
- (a) 1.732 (b) 1.333
(c) 1.414 (d) 2.732

SECTION-B

21. A tube of length 50 cm is filled completely with an incompressible liquid of mass 250 g and closed at both ends. The tube is then rotated in horizontal plane about one of its ends with a uniform angular velocity $x\sqrt{6} \text{ rad s}^{-1}$. If F be the force exerted by the liquid at the other end then the value of x will be
22. Nearly 10% of the power of a 110 W light bulb is converted to visible radiation. The change in average intensities of visible radiation, at a distance of 1 m from the bulb to a distance of 5 m is $a \times 10^{-2} \text{ W/m}^2$. The value of 'a' will be
23. A metal wire of length 0.5 m and cross-sectional area 10^{-4} m^2 has breaking stress $5 \times 10^8 \text{ Nm}^{-2}$. A block of 10 kg is attached at one end of the string and is rotating in a horizontal circle. The maximum linear velocity of block will be ms^{-1} .
24. The velocity of a small ball of mass 0.3 g and density 8 g/cc when dropped in a container filled with glycerine becomes constant after some time. If the density of glycerine is 1.3 g/cc, then the value of viscous force acting on the ball will be $x \times 10^{-4} \text{ N}$, the value of x is. [use $g = 10 \text{ m/s}^2$]
25. A modulating signal $2\sin(6.28 \times 10^6)t$ is added to the carrier signal $4\sin(12.56 \times 10^9)t$ for amplitude modulation. The combined signal is passed through a non-linear square law device. The output is then passed through a band pass filter. The bandwidth of the output signal of band pass filter will be MHz.
26. The speed of a transverse wave passing through a string of length 50 cm and mass 10 g is 60 ms^{-1} . The area of cross-section of the wire is 2.0 mm^2 and its Young's modulus is $1.2 \times 10^{11} \text{ Nm}^{-2}$. The extension of the wire over its natural length due to its tension will be $x \times 10^{-5} \text{ m}$. The value of x is
27. The metallic bob of simple pendulum has the relative density 5. The time period of this pendulum is 10 s. If the metallic bob is immersed in water, then the new time period becomes $5\sqrt{x}$ s. The value of x will be
28. A 8 V Zener diode along with a series resistance R is connected across a 20 V supply (as shown in the figure). If the maximum Zener current is 25 mA, then the minimum value of R will be Ω .

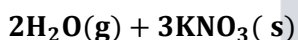
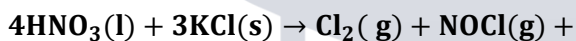


29. Two radioactive materials A and B have decay constants 25λ and 16λ respectively. If initially they have the same number of nuclei, then the ratio of the number of nuclei of B to that of A will be "e" after a time $\frac{1}{a\lambda}$. The value of a is
30. A capacitor of capacitance $500\mu\text{F}$ is charged completely using a dc supply of 100 V. It is now connected to an inductor of inductance 50mH to form an LC circuit. The maximum current in LC circuit will be A.

PART-II CHEMISTRY

SECTION-A

31. Consider the reaction



The amount of HNO_3 required to produce 110.0 g of KNO_3 is:

(Given: Atomic masses of H, O, N and K are 1, 16, 14 and 39, respectively.)

- (a) 32.2 g (b) 69.4 g
(c) 91.5 g (d) 162.5 g

32. Given below are the quantum numbers for 4 electrons.

A. $n = 3, l = 2, m_l = 1, m_s = +1/2$

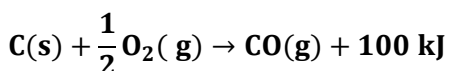
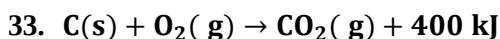
B. $n = 4, l = 1, m_l = 0, m_s = +1/2$

C. $n = 4, l = 2, m_l = -2, m_s = -1/2$

D. $n = 3, l = 1, m_l = -1, m_s = +1/2$

The correct order of increasing energy is:

- (a) $D < B < A < C$ (b) $D < A < B < C$
(c) $B < D < A < C$ (d) $B < D < C < A$



When coal of purity 60% is allowed to burn in presence of insufficient oxygen, 60% of carbon is converted into 'CO' and the remaining is converted into 'CO₂'.

The heat generated when 0.6 kg of coal is burnt is ____

- (a) 1600 kJ (b) 3200 kJ
(c) 4400 kJ (d) 6600 kJ

34. 200 mL of 0.01M HCl is mixed with 400 mL of 0.01M H_2SO_4 . The pH of the mixture is

- (a) 1.14 (b) 1.78
(c) 2.34 (d) 3.02

35. Given below are the critical temperatures of some of the gases:

Gas	Critical temperature (K)
He	5.2
CH_4	190
CO_2	304.2
NH_3	405.5

The gas showing least adsorption on a definite amount of charcoal is:

- (a) He (b) CH_4
(c) CO_2 (d) NH_3

36. In liquation process used for tin (Sn), the metal:

- (a) is reacted with acid
(b) is dissolved in water
(c) is brought to molten form which is made to flow on a slope
(d) is fused with NaOH.

37. Given below are two statements.

Statement I: Stannane is an example of a molecular hydride.

Statement II: Stannane is a planar molecule.

In the light of the above statement, choose the most appropriate answer from the options given below:

- (a) Both Statement I and Statement II are true.
(b) Both Statement I and Statement II are false.
(c) Statement I is true but Statement II is false.
(d) Statement I is false but Statement II is true.

38. Portland cement contains 'X' to enhance the setting time. What is 'X'?

- (a) $\text{CaSO}_4 \cdot \frac{1}{2} \text{H}_2\text{O}$ (b) $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$
(c) CaSO_4 (d) CaCO_3

39. When borax is heated with CoO on a platinum loop, blue coloured bead formed is largely due to :

- (a) B_2O_3 (b) $\text{Co}(\text{BO}_2)_2$
(c) CoB_4O_7 (d) $\text{Co}[\text{B}_4\text{O}_5(\text{OH})_4]$

40. Which of the following 3 d-metal ion will give the lowest enthalpy of hydration ($\Delta_{\text{hyd}} H$) when dissolved in water?

- (a) Cr^{2+} (b) Mn^{2+}
(c) Fe^{2+} (d) Co^{2+}

41. Octahedral complexes of copper (II) undergo structural distortion (Jahn-Teller). Which one of the given copper (II) complexes will show the maximum structural distortion?

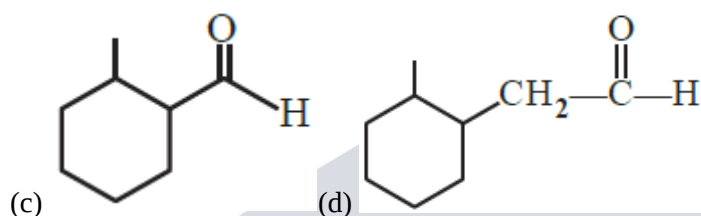
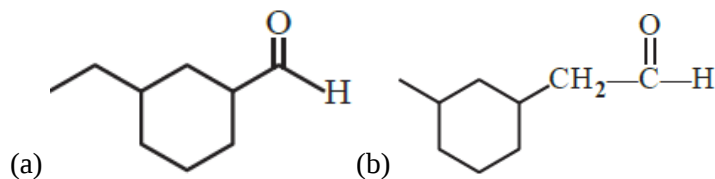
(en-ethylenediamine; $\text{H}_2\text{N}-\text{CH}_2-\text{CH}_2-\text{NH}_2$)

- (a) $[\text{Cu}(\text{H}_2\text{O})_6]\text{SO}_4$ (b) $[\text{Cu}(\text{en})(\text{H}_2\text{O})_4]\text{SO}_4$
(c) cis- $[\text{Cu}(\text{en})_2\text{Cl}_2]$ (d) trans- $[\text{Cu}(\text{en})_2\text{Cl}_2]$

42. Dinitrogen is a robust compound, but reacts at high altitude to form oxides. The oxide of nitrogen that can damage plant leaves and retard photosynthesis is:

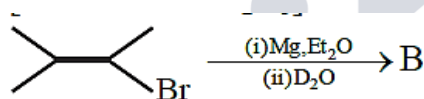
- (a) NO (b) NO_3^-
(c) NO_2 (d) NO_2^-

43. Correct structure of γ -methylcyclohexane carbaldehyde is:

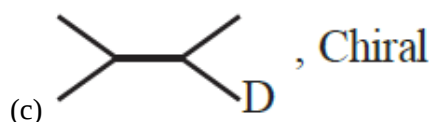
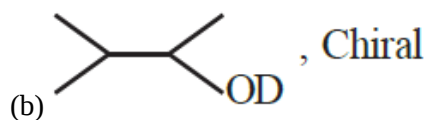
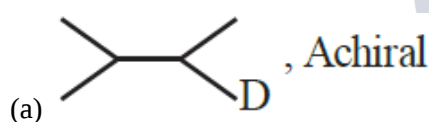


44. Compound 'A' undergoes following sequence of reactions to give compound 'B'. The correct structure and chirality of compound 'B' is:

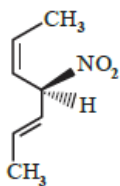
[where Et is $-\text{C}_2\text{H}_5$]



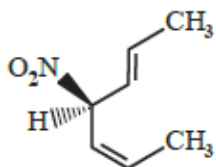
Compound 'A'



45. Given below are two statements.



Statement I: The compound is optically active.



Statement II is mirror image of above compound A.

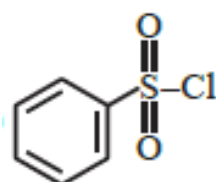
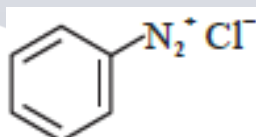
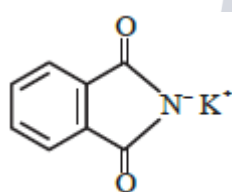
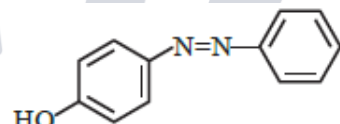
In the light of the above statement, choose the most appropriate answer from the options given below.

- (a) Both Statement I and Statement II are correct
- (b) Both Statement I and Statement II are incorrect.
- (c) Statement I is correct but Statement II is incorrect.
- (d) Statement I is incorrect but Statement II is correct.

46. When ethanol is heated with conc. H_2SO_4 , a gas is produced. The compound formed, when this gas is treated with cold dilute aqueous solution of Baeyer's reagent, is :

- (a) Formaldehyde
- (b) Formic acid
- (c) Glycol
- (d) Ethanoic acid

47. The Hinsberg reagent is:

- (a) 
- (b) 
- (c) 
- (d) 

48. Which of the following is NOT a natural polymer?

- (a) Protein
- (b) Starch
- (c) Rubber
- (d) Rayon

49. Given below are two statements. One is labelled as Assertion A and the other is labelled as Reason R.

Assertion A: Amylose is insoluble in water.

Reason R: Amylose is a long linear molecule with more than 200 glucose units.

In the light of the above statements, choose the correct answer from the options given below.

- (a) Both A and R are correct and R is the correct explanation of A.
- (b) Both A and R are correct and R is NOT the correct explanation of A.
- (c) A is correct but R is not correct.

(d) A is not correct but R is correct.

50. A compound 'X' is a weak acid and it exhibits colour change at pH close to the equivalence point during neutralization of NaOH with CH_3COOH . Compound 'X' exists in ionized form in basic medium. The compound 'X' is:

- (a) methyl orange (b) methyl red
(c) phenolphthalein (d) erichrome Black T

SECTION-B

51. 'x' g of molecular oxygen (O_2) is mixed with 200 g of neon (Ne). The total pressure of the nonreactive mixture of O_2 and Ne in the cylinder is 25 bar. The partial pressure of Ne is 20 bar at the same temperature and volume. The value of 'x' is [Given: Molar mass of $\text{O}_2 = 32 \text{ g mol}^{-1}$. Molar mass of Ne = 20 g mol^{-1}]

52. Consider, PF_5 , BrF_5 , PCl_3 , SF_6 , $[\text{ICl}_4]^-$, ClF_3 and IF_5 . Amongst the above molecule(s)/ion(s), the number of molecule(s)/ion(s) having $\text{sp}^3 \text{d}^2$ hybridisation is _____

53. 1.80 g of solute A was dissolved in 62.5 cm^3 of ethanol and freezing point of the solution was found to be 155.1 K. The molar mass of solute A is g mol^{-1} .

[Given: Freezing point of ethanol is 156.0 K.

Density of ethanol is 0.80 g cm^{-3} .

Freezing point depression constant of ethanol is $2.00 \text{ K kg mol}^{-1}$]

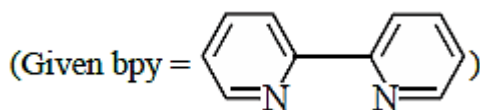
54. For a cell, $\text{Cu(s)} | \text{Cu}^{2+}(0.001\text{M}) || \text{Ag}^+(0.01\text{M}) | \text{Ag(s)}$ the cell potential is found to be 0.43 V at 298 K.

The magnitude of standard electrode potential for Cu^{2+}/Cu is $_ \times 10^{-2} \text{ V}$. [Given : $E_{\text{Ag}^+/\text{Ag}}^\ominus = 0.80 \text{ V}$ and $\frac{2.303RT}{F} = 0.06 \text{ V}$]

55. Assuming $1 \mu\text{g}$ of trace radioactive element X with a half life of 30 years is absorbed by a growing tree. The amount of X remaining in the tree after 100 years is $_ \times 10^{-1} \mu\text{g}$.

[Given: $\ln 10 = 2.303$; $\log 2 = 0.30$]

56. Sum of oxidation state (magnitude) and coordination number of cobalt in $\text{Na}[\text{Co}(\text{bpy})\text{Cl}_4]$ is



57. Consider the following sulphur based oxoacids.

H_2SO_3 , H_2SO_4 , $\text{H}_2\text{S}_2\text{O}_8$ and $\text{H}_2\text{S}_2\text{O}_7$. Amongst these oxoacids, the number of those with peroxo ($\text{O}-\text{O}$) bond is _

58. A 1.84mg sample of polyhydric alcoholic compound 'X' of molar mass 92.0 g/mol gave 1.344 mL of H_2 gas at STP. The number of alcoholic hydrogens present in compound 'X' is _

59. The number of chlorine atoms in bithionol is _

60. The number of stereoisomers formed in a reaction of $(\pm)\text{Ph}(\text{C}=\text{O})\text{C}(\text{OH})(\text{CN})\text{Ph}$ with HCN is

PART-III MATHEMATICS

SECTION-A

61. If $z \neq 0$ be a complex number such that $\left|z - \frac{1}{z}\right| = 2$, then the maximum value of $|z|$ is:

- (a) $\sqrt{2}$ (b) 1
(c) $\sqrt{2} - 1$ (d) $\sqrt{2} + 1$

62. Which of the following matrices can NOT be obtained from the matrix $\begin{bmatrix} -1 & 2 \\ 1 & -1 \end{bmatrix}$ by a single elementary row operation?

- (a) $\begin{bmatrix} 0 & 1 \\ 1 & -1 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & -1 \\ -1 & 2 \end{bmatrix}$
(c) $\begin{bmatrix} -1 & 2 \\ -2 & 7 \end{bmatrix}$ (d) $\begin{bmatrix} -1 & 2 \\ -1 & 3 \end{bmatrix}$

63. If the system of equations

$$x + y + z = 6$$

$$2x + 5y + \alpha z = \beta$$

$$x + 2y + 3z = 14$$

has infinitely many solutions, then $\alpha + \beta$ is equal to:

- (a) 8 (b) 36
(c) 44 (d) 48

64. Let the function

$$f(x) = \begin{cases} \frac{\log_e(1+5x) - \log_e(1+\alpha x)}{x} & \text{if } x \neq 0 \\ 10 & \text{if } x = 0 \end{cases}$$

be continuous at $x = 0$.

The α is equal to:

- (a) 10 (b) -10
(c) 5 (d) -5

65. If $[t]$ denotes the greatest integer $\leq t$, then the value of $\int_0^1 [2x - |3x^2 - 5x + 2| + 1] dx$ is:

- (a) $\frac{\sqrt{37} + \sqrt{13} - 4}{6}$ (b) $\frac{\sqrt{37} - \sqrt{13} - 4}{6}$
(c) $\frac{-\sqrt{37} - \sqrt{13} + 4}{6}$ (d) $\frac{-\sqrt{37} + \sqrt{13} + 4}{6}$

66. Let $\{a_n\}_{n=0}^{\infty}$ be a sequence such that $a_0 = a_1 = 0$ and $a_{n+2} = 3a_{n+1} - 2a_n + 1, \forall n \geq 0$.

Then $a_{25}a_{23} - 2a_{25}a_{22} - 2a_{23}a_{24} + 4a_{22}a_{24}$ is equal to:

- (a) 483 (b) 528
(c) 575 (d) 624

67. $\sum_{r=1}^{20} (r^2 + 1)(r!)$ is equal to:

- (a) $22! - 21!$ (b) $22! - 2(21!)$
(c) $21! - 2(20!)$ (d) $21! - 20!$

68. For $I(x) = \int \frac{\sec^2 x - 2022}{\sin^{2022} x} dx$, if $I\left(\frac{\pi}{4}\right) = 2^{1011}$, then

- (a) $3^{1010} I\left(\frac{\pi}{3}\right) - I\left(\frac{\pi}{6}\right) = 0$ (b) $3^{1010} I\left(\frac{\pi}{6}\right) - I\left(\frac{\pi}{3}\right) = 0$
(c) $3^{1011} I\left(\frac{\pi}{3}\right) - I\left(\frac{\pi}{6}\right) = 0$ (d) $3^{1011} I\left(\frac{\pi}{6}\right) - I\left(\frac{\pi}{3}\right) = 0$

69. If the solution curve of the differential equation $\frac{dy}{dx} = \frac{x+y-2}{x-y}$ passes through the point $(2, 1)$ and $(k + 1, 2)$, $k > 0$, then
- (a) $2\tan^{-1}\left(\frac{1}{k}\right) = \log_e(k^2 + 1)$
- (b) $\tan^{-1}\left(\frac{1}{k}\right) = \log_e(k^2 + 1)$
- (c) $2\tan^{-1}\left(\frac{1}{k+1}\right) = \log_e(k^2 + 2k + 2)$
- (d) $2\tan^{-1}\left(\frac{1}{k}\right) = \log_e\left(\frac{k^2+1}{k^2}\right)$
70. Let $y = y(x)$ be the solution curve of the differential equation $\frac{dy}{dx} + \left(\frac{2x^2+11x+13}{x^3+6x^2+11x+6}\right)y = \frac{(x+3)}{x+1}$, $x > -1$, which passes through the point $(0, 1)$. Then $y(1)$ is equal to:
- (a) $\frac{1}{2}$ (b) $\frac{3}{2}$
- (c) $\frac{5}{2}$ (d) $\frac{7}{2}$
71. Let m_1, m_2 be the slopes of two adjacent sides of a square of side a such that $a^2 + 11a + 3(m_1^2 + m_2^2) = 220$. If one vertex of the square is $(10(\cos \alpha - \sin \alpha), 10(\sin \alpha + \cos \alpha))$, where $\alpha \in \left(0, \frac{\pi}{2}\right)$ and the equation of one diagonal is $(\cos \alpha - \sin \alpha)x + (\sin \alpha + \cos \alpha)y = 10$, then $72(\sin^4 \alpha + \cos^4 \alpha) + a^2 - 3a + 13$ is equal to:
- (a) 119 (b) 128
- (c) 145 (d) 155
72. The number of elements in the set $S = \left\{x \in \mathbb{R} : 2\cos\left(\frac{x^2+x}{6}\right) = 4^x + 4^{-x}\right\}$ is:
- (a) 1 (b) 3
- (c) 0 (d) infinite
73. Let $A(\alpha, -2)$, $B(\alpha, 6)$ and $C\left(\frac{\alpha}{4}, -2\right)$ be vertices of a $\triangle ABC$. If $\left(5, \frac{\alpha}{4}\right)$ is the circumcentre of $\triangle ABC$, then which of the following is NOT correct about $\triangle ABC$:
- (a) area is 24 (b) perimeter is 25
- (c) circumradius is 5 (d) inradius is 2
74. Let Q be the foot of perpendicular drawn from the point $P(1, 2, 3)$ to the plane $x + 2y + z = 14$. If R is a point on the plane such that $\angle PRQ = 60^\circ$, then the area of $\triangle PQR$ is equal to:
- (a) $\frac{\sqrt{3}}{2}$ (b) $\sqrt{3}$
- (c) $2\sqrt{3}$ (d) 3
75. If $(2, 3, 9)$, $(5, 2, 1)$, $(1, \lambda, 8)$ and $(\lambda, 2, 3)$ are coplanar, then the product of all possible values of λ is:
- (a) $\frac{21}{2}$ (b) $\frac{59}{8}$
- (c) $\frac{57}{8}$ (d) $\frac{95}{8}$
76. Bag I contains 3 red, 4 black and 3 white balls and Bag II contains 2 red, 5 black and 2 white balls. One ball is transferred from Bag I to Bag II and then a ball is drawn from Bag II. The ball so drawn is found to be black in colour. Then the probability, that the transferred ball is red, is:
- (a) $\frac{4}{9}$ (b) $\frac{5}{18}$
- (c) (d) $\frac{3}{10}$
77. Let $S = \{z = x + iy : |z - 1 + i| \geq |z|, |z| < 2, |z + i| = |z - 1|\}$. Then the set of all values of x , for which $w = 2x + iy \in S$ for some $y \in \mathbb{R}$, is
- (a) $\left(-\sqrt{2}, \frac{1}{2\sqrt{2}}\right]$ (b) $\left(-\frac{1}{\sqrt{2}}, \frac{1}{4}\right]$
- (c) $\left(-\sqrt{2}, \frac{1}{2}\right]$ (d) $\left(-\frac{1}{\sqrt{2}}, \frac{1}{2\sqrt{2}}\right]$

78. Let $\vec{a}, \vec{b}, \vec{c}$ be three coplanar concurrent vectors such that angles between any two of them is same. If the product of their magnitudes is 14 and $(\vec{a} \times \vec{b}) \cdot (\vec{b} \times \vec{c}) + (\vec{b} \times \vec{c}) \cdot (\vec{c} \times \vec{a}) + (\vec{c} \times \vec{a}) \cdot (\vec{a} \times \vec{b}) = 168$ then $|\vec{a}| + |\vec{b}| + |\vec{c}|$ is equal to:
- (a) 10 (b) 14
(c) 16 (d) 18
79. The domain of the function $f(x) = \sin^{-1} \left(\frac{x^2 - 3x + 2}{x^2 + 2x + 7} \right)$ is :
- (a) $[1, \infty)$ (b) $(-1, 2]$
(c) $[-1, \infty)$ (d) $(-\infty, 2]$
80. The statement $(p \Rightarrow q) \vee (p \Rightarrow r)$ is NOT equivalent to:
- (a) $(p \wedge (\sim r)) \Rightarrow q$ (b) $(\sim q) \Rightarrow ((\sim r) \vee p)$
(c) $p \Rightarrow (q \vee r)$ (d) $(p \wedge (\sim q)) \Rightarrow r$

SECTION-B

81. The sum and product of the mean and variance of a binomial distribution are 82.5 and 1350 respectively. They the number of trials in the binomial distribution is:
82. Let $\alpha, \beta (\alpha > \beta)$ be the roots of the quadratic equation $x^2 - x - 4 = 0$. If $P_n = \alpha^n - \beta^n, n \in \mathbb{N}$, then $\frac{P_{15}P_{16} - P_{14}P_{16} - P_{15}^2 + P_{14}P_{15}}{P_{13}P_{14}}$ is equal to_____
83. Let $x = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ and $A = \begin{bmatrix} -1 & 2 & 3 \\ 0 & 1 & 6 \\ 0 & 0 & -1 \end{bmatrix}$. For $k \in \mathbb{N}$, if $X' A^k X = 33$, then k is equal to:
84. The number of natural numbers lying between 1012 and 23421 that can be formed using the digits 2, 3, 4, 5, 6 (repetition of digits is not allowed) and divisible by 55 is_____
85. If $\sum_{k=1}^{10} K^2 (10C_k)^2 = 22000L$, then L is equal to
86. If $[t]$ denotes the greatest integer $\leq t$, then number of points, at which the function $f(x) = 4|2x + 3| + 9 \left[x + \frac{1}{2} \right] - 12[x + 20]$ is not differentiable in the open interval $(-20, 20)$, is
87. If the tangent to the curve $y = x^3 - x^2 + x$ at the point (a, b) is also tangent to the curve $y = 5x^2 + 2x - 25$ at the point $(2, -1)$, then $|2a + 9b|$ is equal to_____
88. Let AB be a chord of length 12 of the circle $(x - 2)^2 + (y + 1)^2 = \frac{169}{4}$. If tangents drawn to the circle at points A and B intersect at the point P, then five times the distance of point P from chord AB is equal to_____
89. Let $\vec{a}$ and $\vec{b}$ be two vectors such that $|\vec{a} + \vec{b}|^2 = |\vec{a}|^2 + 2|\vec{b}|^2, \vec{a} \cdot \vec{b} = 3$ and $|\vec{a} \times \vec{b}|^2 = 75$. Then $|\vec{a}|^2$ is equal to_____
90. Let $S = \{(x, y) \in \mathbb{N} \times \mathbb{N} : 9(x - 3)^2 + 16(y - 4)^2 \leq 144\}$ and $T = \{(x, y) \in \mathbb{R} \times \mathbb{R} : (x - 7)^2 + (y - 4)^2 \leq 36\}$. The $n(S \cap T)$ is equal to_____